

Additional 6-PACs



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Un-Expected Bernstein

- Learn a classifier $\hat{h}: \mathcal{X} \to \mathcal{Y} = \{0,1\}$ from i.i.d. training data $Z^n = (X_2, Y_2), ...(X_n, Y_n) \sim P$
- PAC-Bayes bound (McAllester '98): Error you make on future data bounded, with high probability, by error on training data plus complexity term:

$$\mathbf{E}_{(X,Y)\sim P}[\text{LOSS}(Y,\hat{h}_{|Z^n}(X))] \leq \frac{1}{n} \sum_{i=1}^n \text{LOSS}(Y_i,\hat{h}_{|Z^n}(X_i))] + \sqrt{\frac{\text{COMPLEXITY}(\hat{h}_{|Z^n})}{n}}$$

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WE:

$$\begin{split} \mathbf{E}_{(X,Y)\sim P}[\mathrm{LOSS}(Y,\hat{h}_{|Z^n}(X))] &\leq \frac{1}{n} \sum_{i=1}^n \mathrm{LOSS}(Y_i,\hat{h}_{|Z^n}(X_i))] \\ + &\mathrm{STABILITY\text{-}COEFFICIENT}(\hat{h}_{|Z^n}) \cdot \frac{\mathrm{COMPLEXITY}(\hat{h}_{|Z^n})}{n} + \sqrt{\frac{\mathrm{CONST.}}{n}} \end{split}$$