

# Experimental Study of Time Series Forecasting Methods for Groundwater Level Prediction

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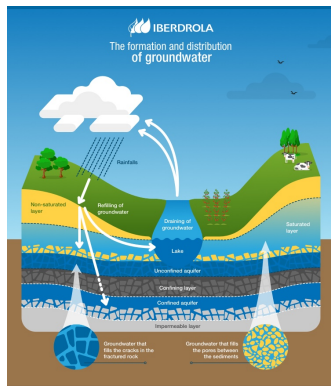
# Motivation: Water and groundwater

## Ground water

- ground water = water bodies entrapped in soil
- originate from rainfall that penetrates through soil, rocks, etc.
- preserved from pollutants  $\Rightarrow$  freshwater

## A very complex dynamic system

- complex flows of water (including evapotranspiration)
- complex interactions between water stocks
- depends on a lot of physic/geographic parameters



source:

<https://www.iberdrola.com/>

# Motivation: Manage the groundwater resource

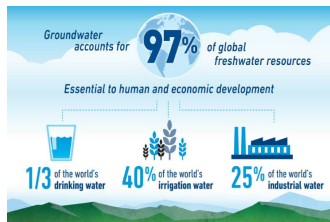
## Highly demanded resources

- for human consumption (1/3 of drinking water comes from groundwaters)
- for agriculture
- for industry (cooling, washing, etc.)

## A stressed common resources

- climate change and over-consumptions of water  $\rightsquigarrow$  drought
- different potential problems
  - sanity issues
  - continuous access to drinking water
  - economical activities

⇒ **Need for a better management of water resources**



source:

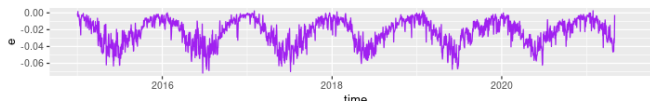
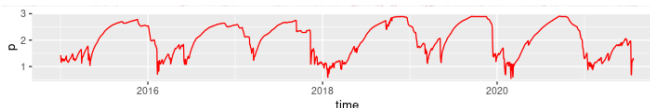
<https://www.worldbank.org/>



# Motivation: Forecasting groundwater level

## Need for a better management of water resources

- dynamically adapt consumption to available resources
  - depends on rainfalls, weather and human activities
- ⇒ **forecasting the groundwater level** is an essential tool to improve water management
  - long term forecasting are awaited (several months)



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## State of the art approaches

- hydrological modeling of water flows [1]
  - accurate forecasting
  - very time consuming (a new modeling for each location, require complex measurements)
- data driven modeling: [4, 2]
  - less time consuming ... only to get data about groundwater level
  - less accurate
  - only applied to small datasets of groundwater level measurements, with small horizons

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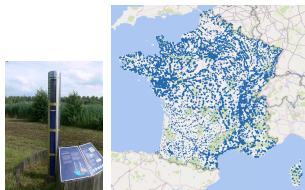
## Research questions

- ⇒ is it possible to make accurate long term predictions of groundwater levels (3 months)?
- ⇒ which time series forecasting model is the better?
- ⇒ would it be possible to learn a *global* model?

# Data sources

## Hub'eau network of sensors

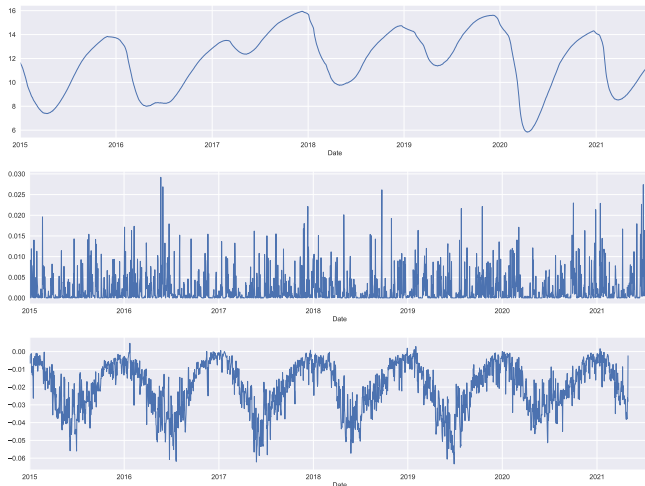
- sensor for groundwater level = *piezometer*
- hundreds of piezos make daily measurements all across the French mainland (see map)
- some sensors are installed since several decades
- data are freely available



## Our prepared dataset

- 1,026 sources all over the French mainland,
  - period from January 2015 to January 2021 (2,221 days) (with less than 50 missing data)
  - completed with daily climate variables (from Copernicus ERA5):
    - rainfall
    - evapotranspiration
- dataset available upon request

# Visualizations



**Figure:** Top to bottom: daily groundwater, rainfall and evapotranspiration time series for the piezometer BSS000EBL



# Formalization

## Data available for the $i$ -th piezometers

- Daily historical groundwater level:  $y_{t=1..n}^i$ .
- Daily exogenous data (rain, evapotranspiration):  $z_{t=1..n}^i$

## Predict groundwater level at horizon $h$

$$\hat{y}_{t=(n+1)..(n+h)}^i = \varphi(y_{t=1..n}^i, z_{t=1..n}^i, \tilde{z}_{t=n+1..n+h}^i)$$

- $\tilde{z}$ : exogenous data approximation for future dates, estimated by the mean of the previous years

## Root mean square scaled error

$$RMSSE = \sqrt{\frac{\frac{1}{h} \sum_{t=t_0+1}^{t_0+h} (y_t - \hat{y}_t)^2}{\frac{1}{t_0-1} \sum_{t=2}^{t_0} (y_t - y_{t-1})^2}}$$

# Time series forecasting models

## Tree types of forecasting models

- **Autoregressive models** (detailed later)
- **DeepAR-based models** [5]
- **Prophet-based models** [6, 7]: Prophet, NeuralProphet, NeuralProphet

# Time series forecasting models: auto-regressive models

## Generalization of autoregressive models

- forecasting the next value from the previous  $r$  values,

$$\hat{y}_{t_0+1}^i = \varphi(y_{t_0-r..t_0}^i, z_{t_0-r..t_0+1}^i)$$

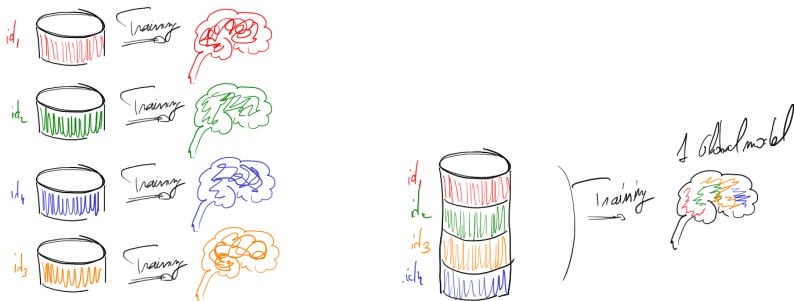
- different classes of  $\varphi$  functions
  - linear function (LM): classical AR model
  - XGB, LM, RF, SVR: modeling non-linear dependencies
- forecasting at horizon  $h$  apply recursively *varphi* for  $k = 1..h$ :

$$\hat{y}_{t_0+k}^i = \varphi(y_{t_0-(r-k)..t_0}^i \odot \hat{y}_{t_0..t_0+k-1}^i, z_{t_0-(r-k)..t_0}^i \odot \tilde{z}_{t_0..t_0+k}^i)$$

We experimentally found that an history length  $r = 100$  leads to better performance.

# Learning strategies

- **Local forecasting:** train a model for each piezometer and use it to predict the future values of this piezometer only.
- **Global forecasting** (or cross-learning) [3]: train a single "big" model from all piezometers and use it to forecast any piezometer level.



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## Pros/Cons

- *modeling capabilities*: local forecasting requires less modeling capabilities while the global model has to capture all dynamics
- *available data*: each local training has less available data than a global training
- *new piezometers*: a local model can not be used for newly installed piezometers
- global modeling requires more resource intensive training (local modeling can easily be distributed)
- global modeling can be feed with additional non-temporal descriptive features (soil nature)

# Experiments and results

## Settings

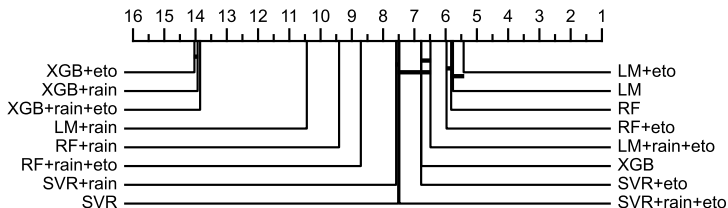
- 1,026 multivariate time series
- $t_0 = 2,221$  days (5 years and 9 months)
- $h = 93$  days (3 months)
- Critical difference diagrams of *RMSSE* ( $\alpha = 0.5$ )
- $r = 100$  for auto-regressive models (determined experimentally)
- approximated exogenous data: mean of the five first years

## Naming convention: [forecaster-L,G]+exo

- forecaster: XGB, LM, DeepAR, Prophet, etc.
- L: Local training, G: Global training
- $\text{exo} \in \emptyset, \text{eto}, \text{rain eto+rain}$  when exogenous data are considered.

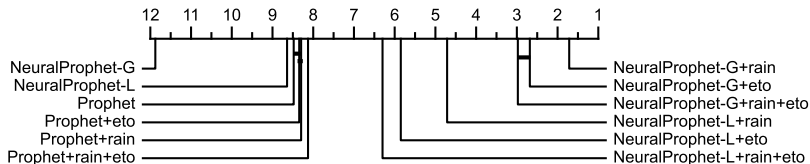
Example: NeuralProphet-G+exo

# Comparisons of generalized autoregressive models (local training)



- the best performing configurations use either only evapotranspiration, or no exogenous data at all,
- Linear models are among the best models

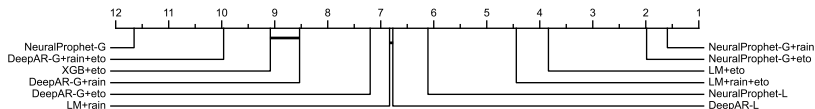
# Prophet-based models



- NeuralProphet-G is the worst approach, but the best when combined with exogenous data,
- Unlike DeepAR, NeuralPhophet works better when executed globally than locally, in particular when exogenous data are used,
- In the absence of exogenous data, Prophet significantly outperforms NeuralProphet

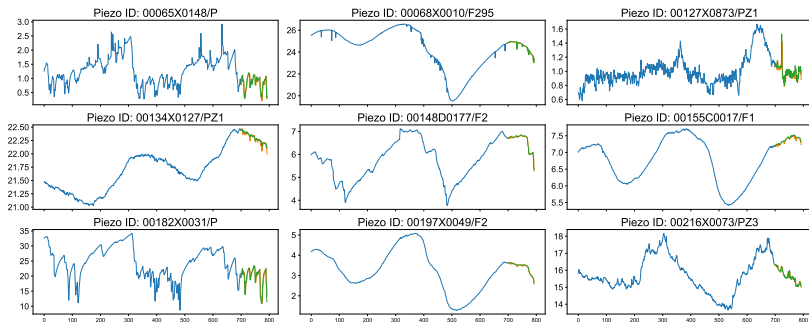


# Comparing the three groups of models



- LM and NeuralProphet-G respectively produce the most accurate and the least accurate forecasts when exogenous data are absent,
- NeuralProphet-G significantly outperforms the others when exogenous data are used,
- precipitations impact groundwater level more than ETO (see NeuralProphet-G+rain and NeuralProphet-G+eto).

# Visualization of some forecasts



- blue: historical data
- green: ground truth
- orange: forecasts

# Conclusion

## Conclusions

- We performed the most extensive experimental study of groundwater level forecasting (1,026 sources, 9 methods),
- globally trained forecasters seems to outperform the locally trained (but are more resource intensive consuming)
- precipitation tends to have more impact on the accuracy of the forecasts than evapotranspiration.

## Data preparation and source code available

<https://github.com/frankl1/piezoforecast>

## Perspectives

- making the dataset available in a standard format
- hybrid strategy: identify groups of piezometers with “similar” dynamics to make a concise, accurate and readily applicable model
- integrate additional exogenous data (water consumption) and features (soil nature)

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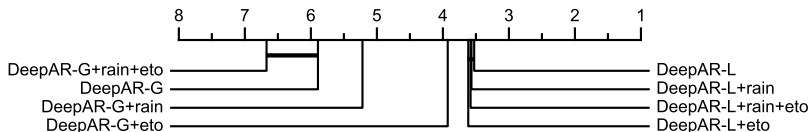
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# DeepAR-based models



- Local training strategy for DeepAR is better than a global one,
- Exogenous data improve global DeepAR, but have insignificant impact on local DeepAR.