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joint work with

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INVERSE ESTIMATES IN BEM AND THEIR APPLICATION TO ADAPTIVITY

We show polynomial inverse estimates for the classical boundary integral operators associated with the Laplacian on shape-regular meshes \mathcal{T}_h . For example, for the single-layer integral operator V on the boundary Γ of a polygon/polyhedron and \mathcal{T}_h -piecewise polynomials ψ of degree p , this inverse estimates takes the form

$$\|h_{\mathcal{T}}^{1/2} p^{-1} \nabla_{\Gamma} V \phi\|_{L^2(\Gamma)} \leq C \|\phi\|_{H^{-1/2}(\Gamma)}$$

Such an inverse estimate is a crucial ingredient for the convergence proof of adaptive BEM. Indeed, the work [Carstensen, Feischl, Page, Praetorius '14] identified four “axioms” that ensure rate-optimal adaptive algorithms. This inverse estimate is at the heart of the proof of two of these axioms, namely, the “stability on non-refined elements” and the “reduction on refined elements”.