

# Perspectives (= Questions)

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I am working  
on Terminator 3

I approximate the  
galaxy as a sphere...



# Unexpected marriage?



# Deux Français reçoivent l'IgNobel pour leurs travaux sur les spaghettis

## DISTINCTION

Deux physiciens de l'université Paris-VI sont récompensés pour des études sur la résistance des pâtes !

« C'EST DE LA SCIENCE *qui fait rire et réfléchir* », dit toujours Marc Abrahams, rédacteur en chef des *Annales de la Recherche Improbable*. Chaque année, à l'époque de l'attribution des vrais prix Nobel, un comité autoproclamé de journalistes, d'anciens Nobel, de savants, réunis à l'université d'Harvard dans le « *Conseil des gouverneurs des prix IgNobel* » décerne à des VRAIS chercheurs, pour des travaux publiés dans des VRAIS journaux savants, des prix loufoques.

Cette année, l'IgNobel de physique récompense deux chercheurs français, Basile Audoly et Sébastien

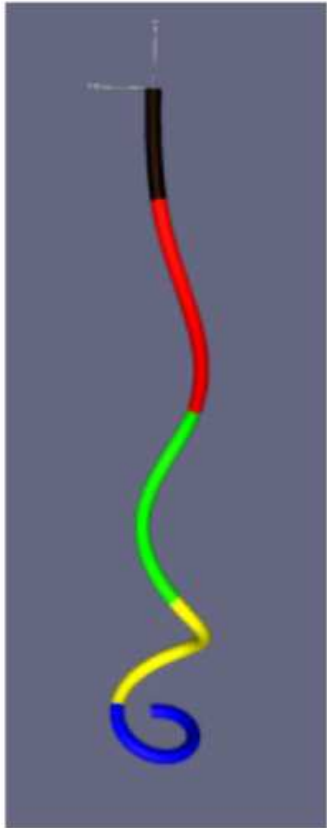


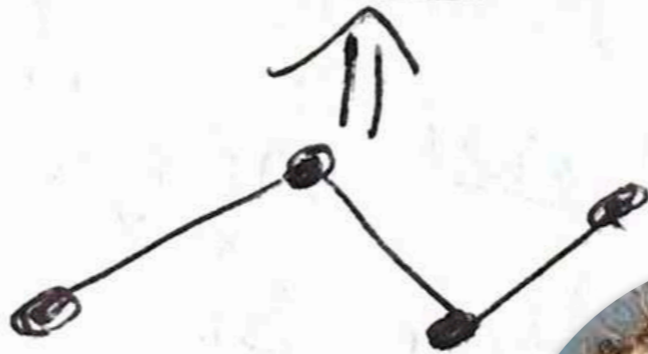
Basile Audoly et Sébastien Neukirch ont reçu le prix IgNobel, récompense loufoque décernée par un comité de savants, dont d'anciens Nobel. DR.

avant de le cuire, au-delà de sa résistance interne, il ne se casse pas en deux bouts nets et égaux. Pourquoi ?

C'est un problème de fragmentation et d'élasticité des matériaux. Alaudy et Neukirch ont maintenu

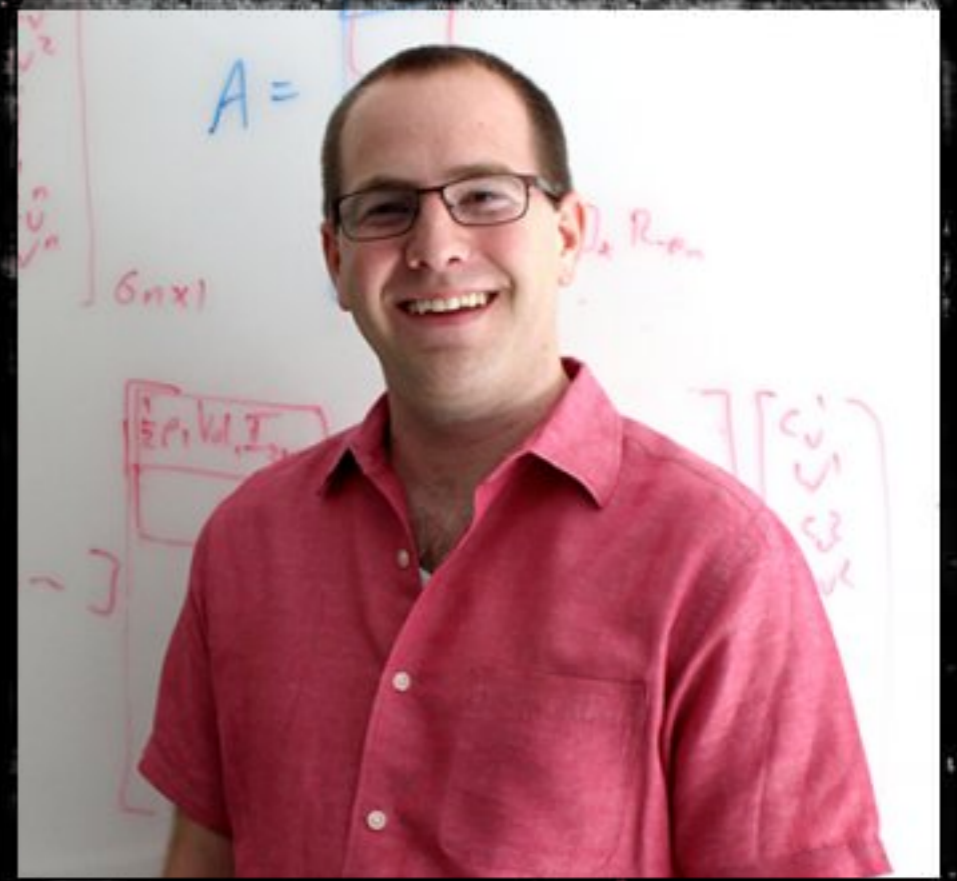
surcourbure et se recassent encore. Cette révélation dans le domaine de la fragmentation aura sans doute des conséquences pour les chercheurs, l'industrie de la défense, les sauteurs à la perche, et même pour

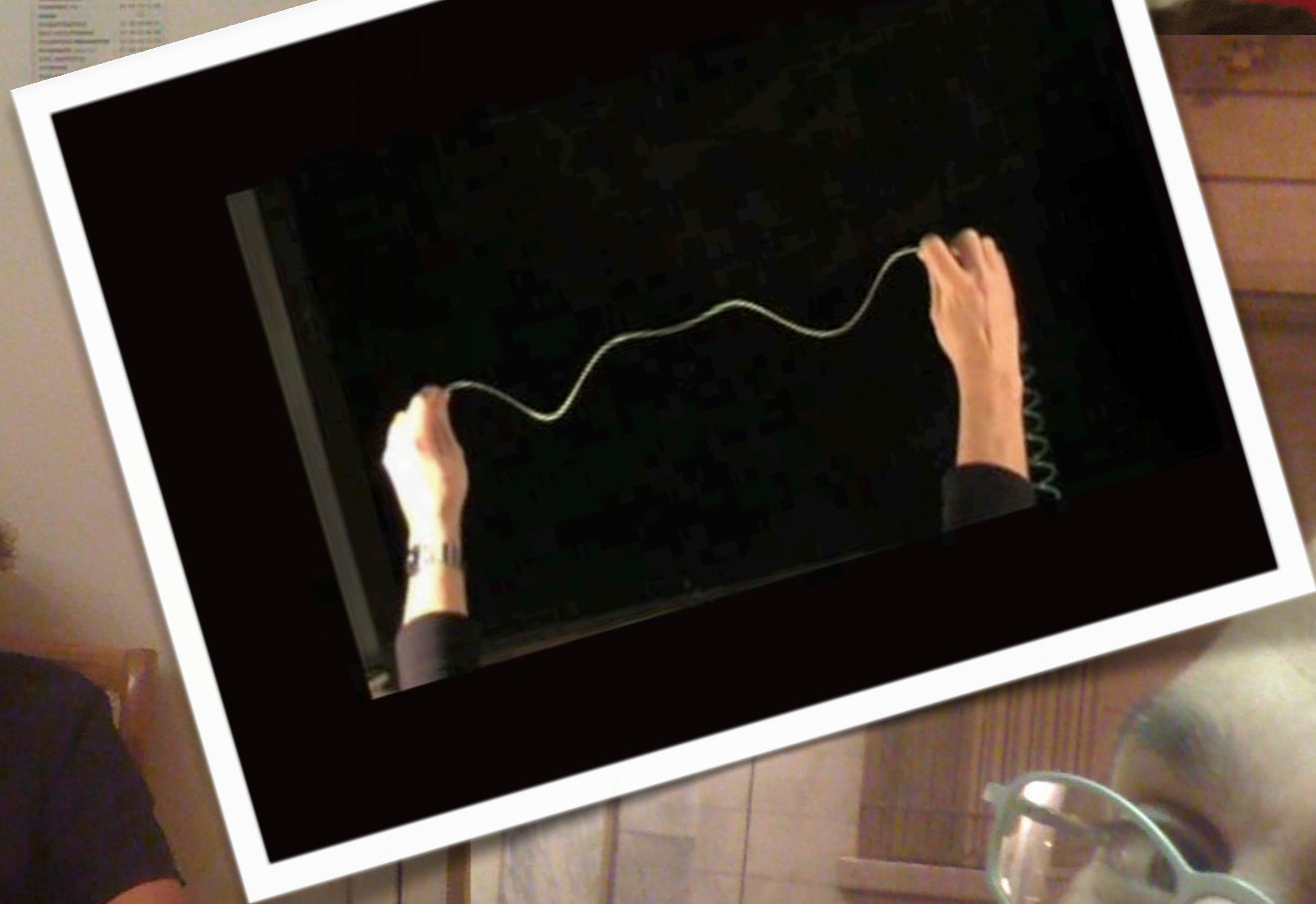






ER





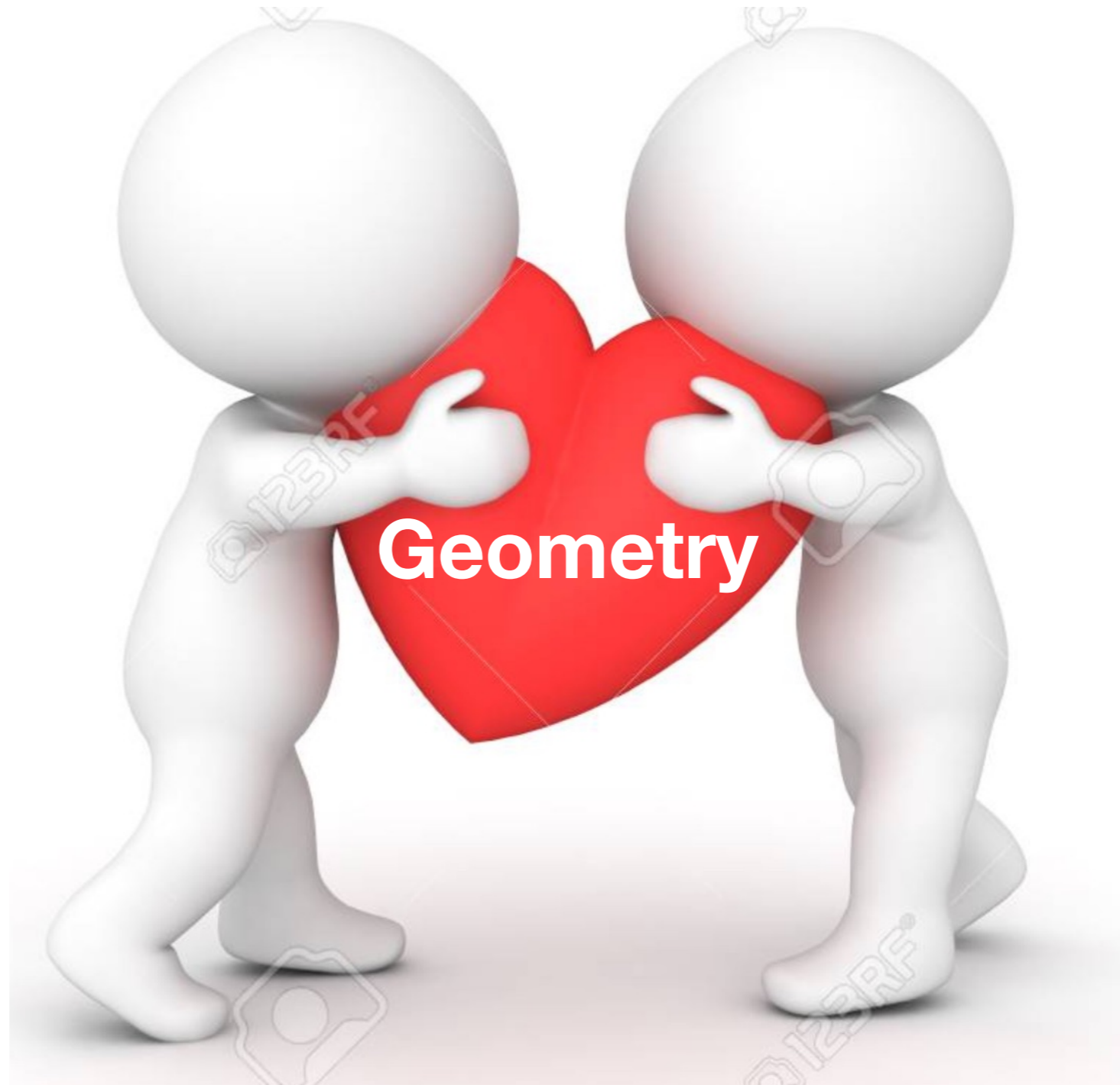




# Unexpected marriage?



**..from a common love...**



# ..from a common love...

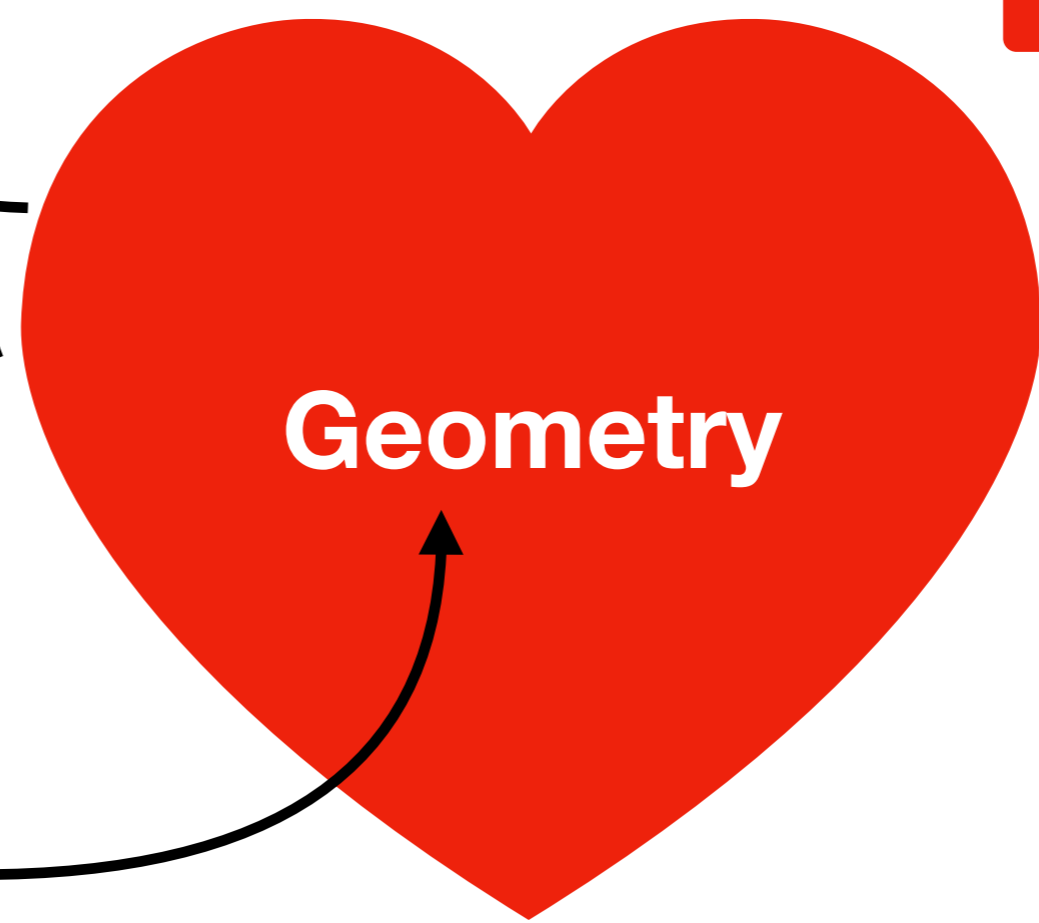
**shared language**

193 

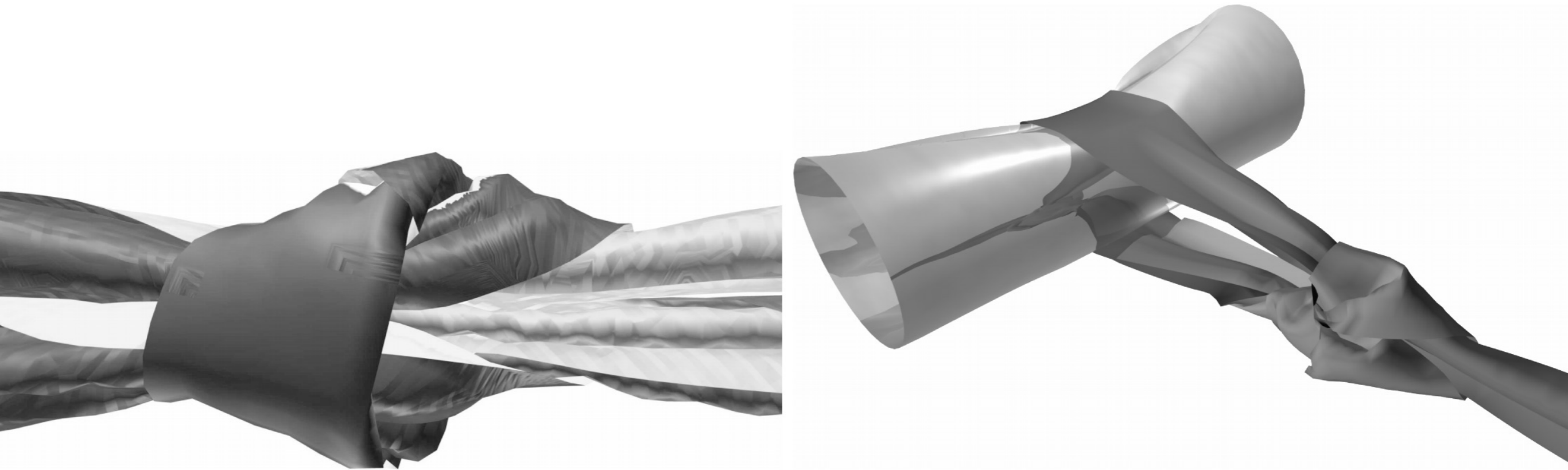
**shared taste  
for problems**

**Geometry**

**behavior  
dominated by**



# Bridge Culture & Language



- know the audience  
“good visual rendering is even negative” - Emanuel
- small steps – deeper citations

**Complementary approaches,  
from opposing beginnings,  
meet at shared picture**

**Experiments**

**Build up physics**

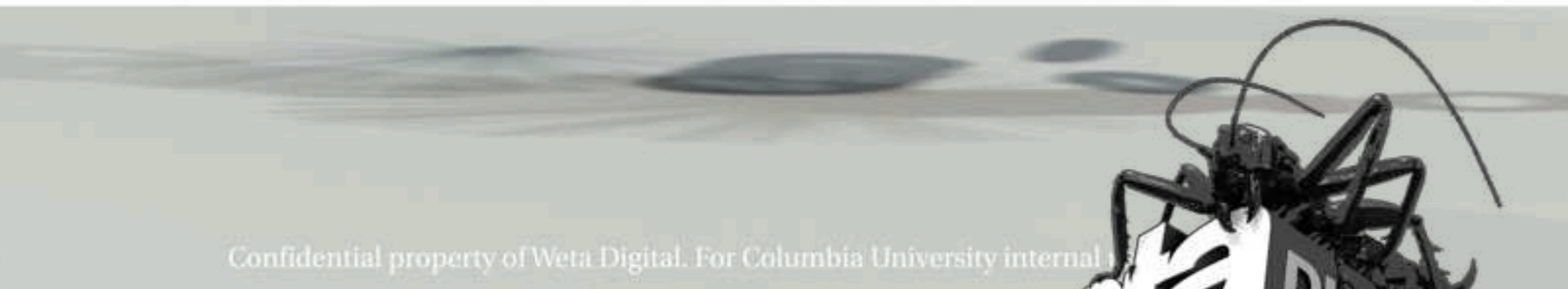
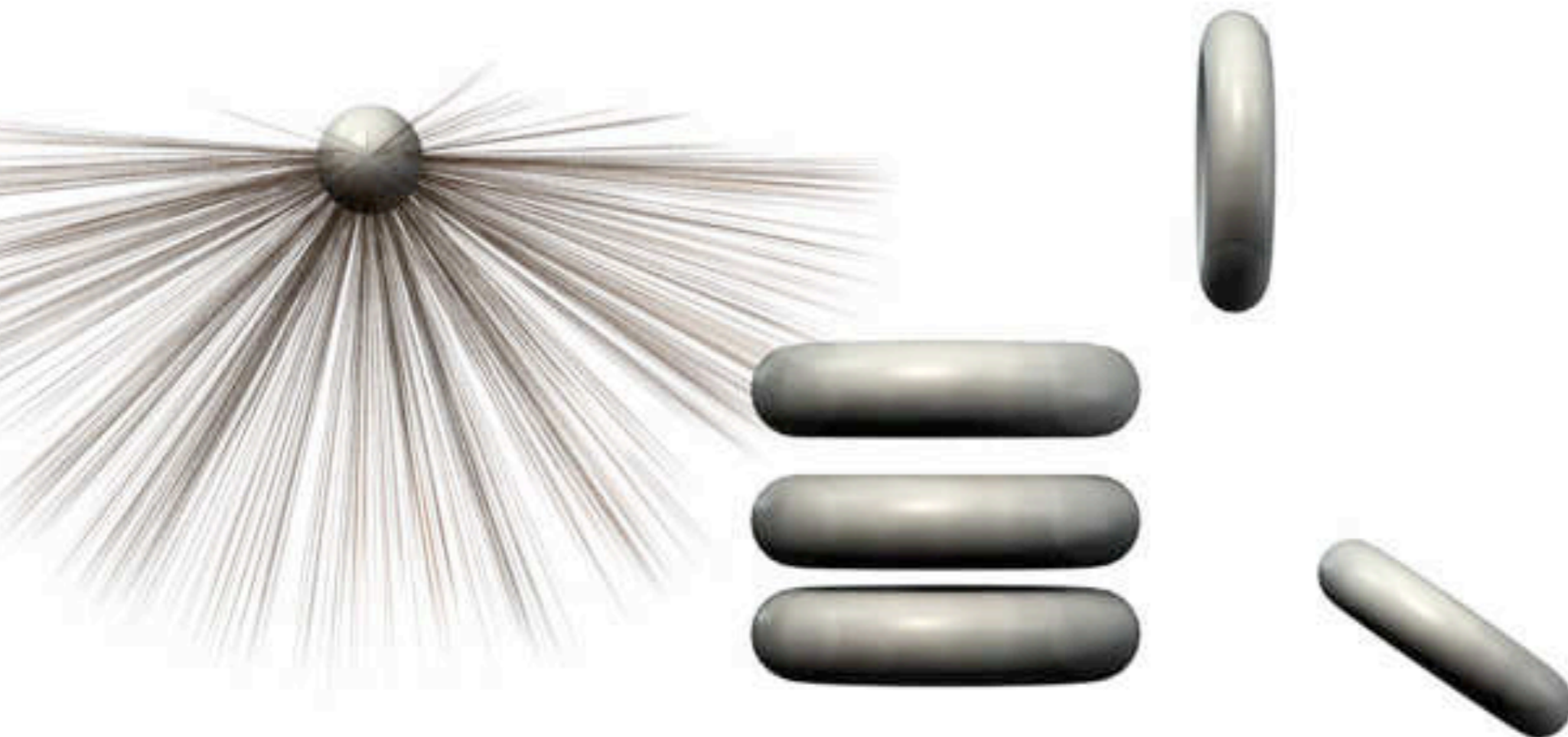


**Factor out physics**

**Computation**

**(“capillarity is negligible” - Fabrice)**

**Hair in film:**



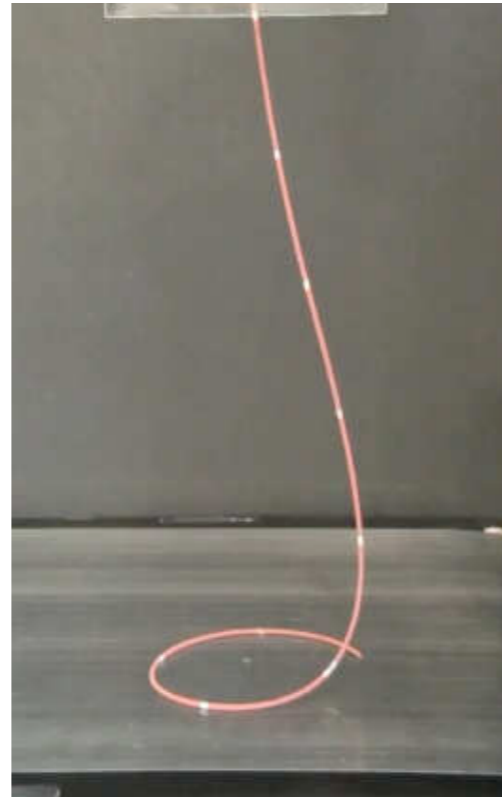
Confidential property of Weta Digital. For Columbia University internal use only.



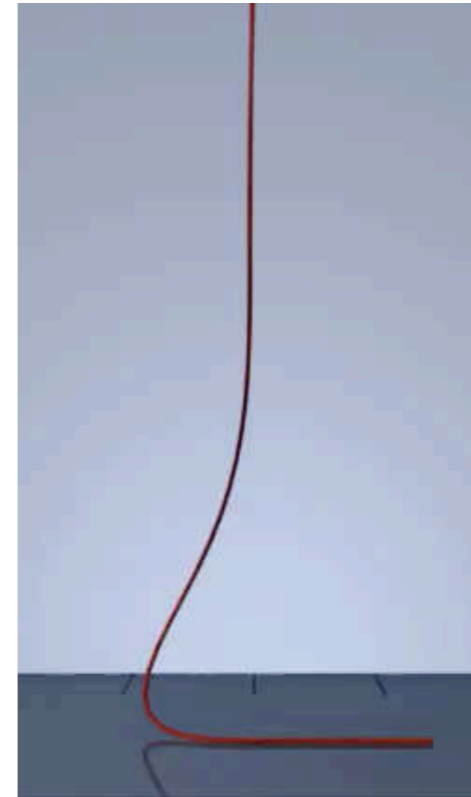
# Steady coiling:

$v_{belt} = 0$   
 $\epsilon = 1$   
 Silicone rod  
 $d = 1.6\text{mm}$

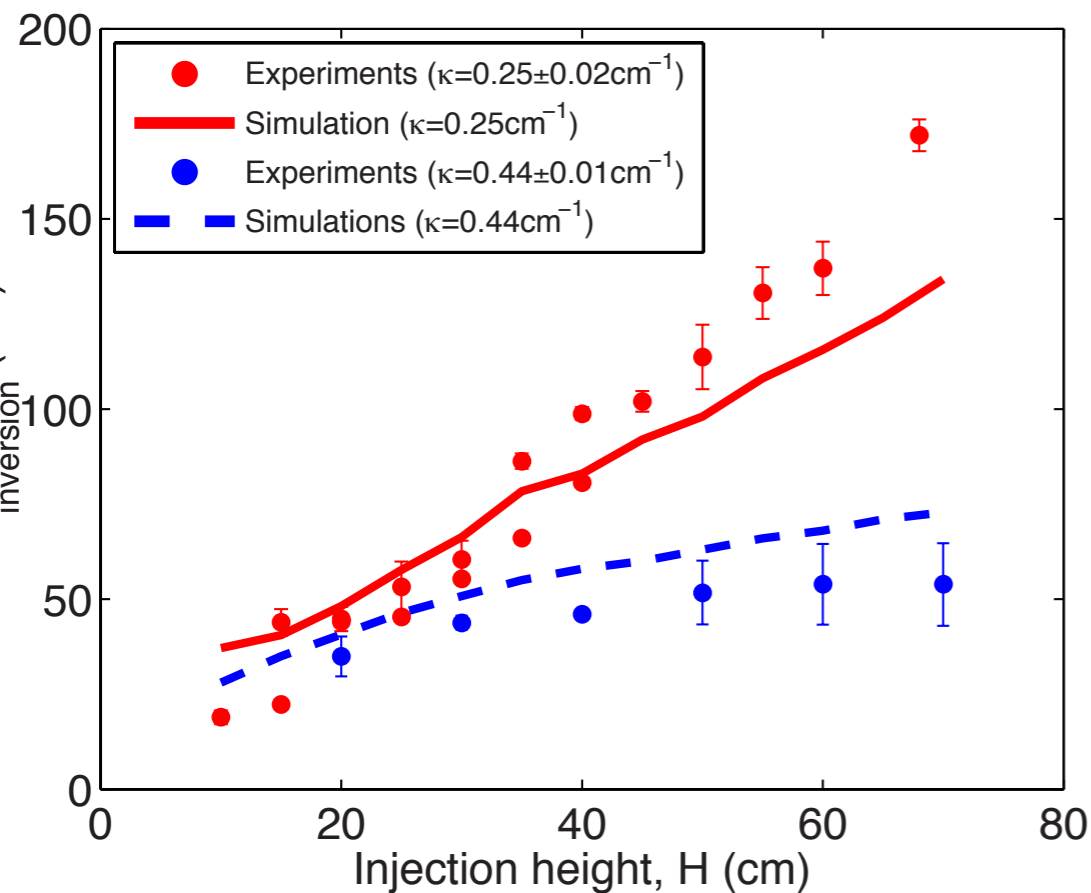
Experiments  
 $k = 0.25\text{cm}^{-1}$



Simulations  
 $k = 0.25\text{cm}^{-1}$



Experiments  
 $k \sim 0\text{cm}^{-1}$



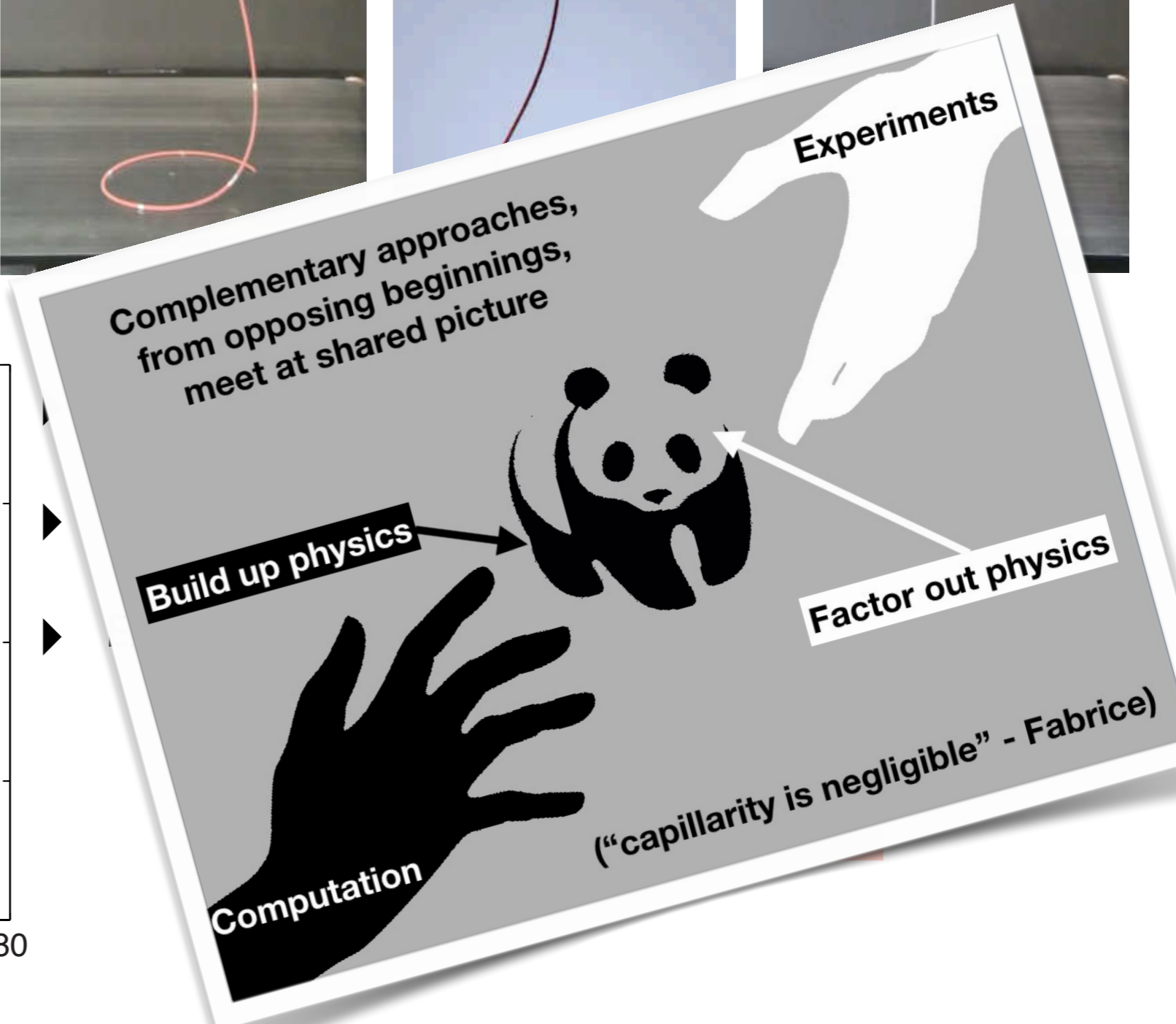
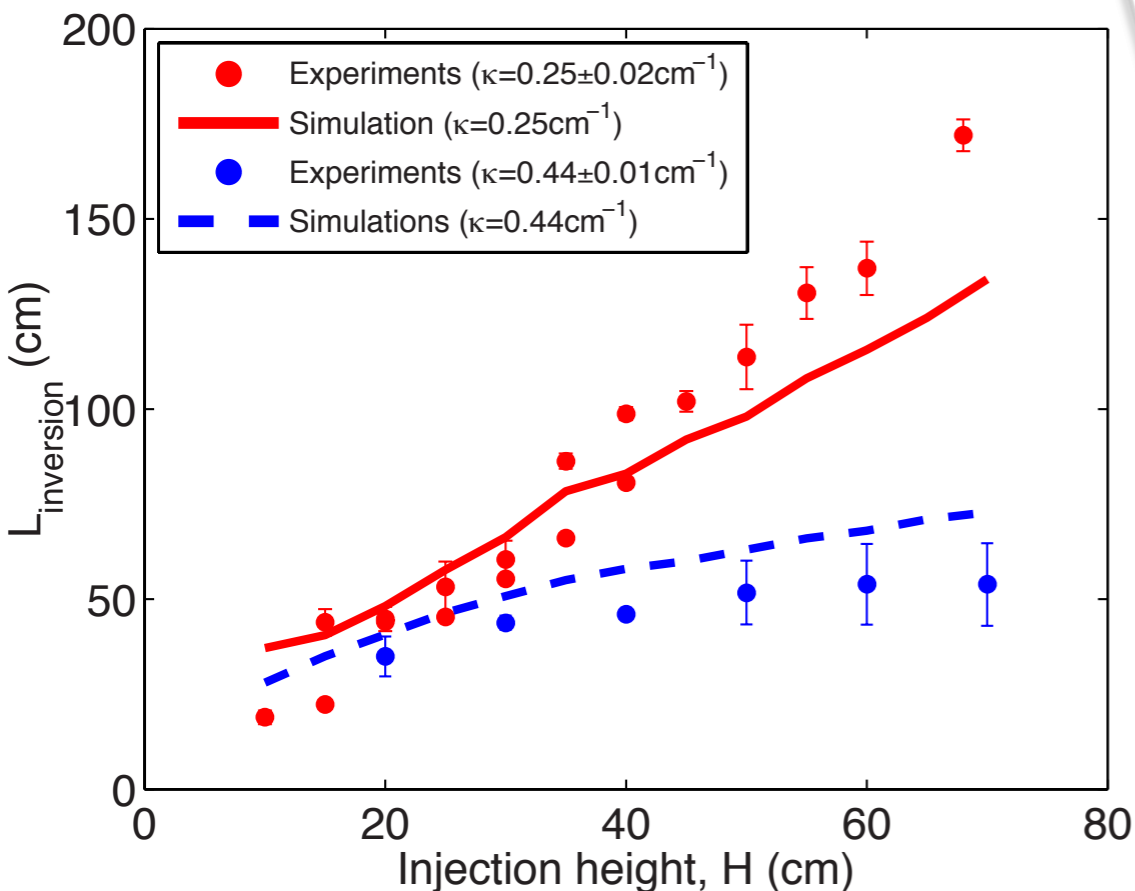
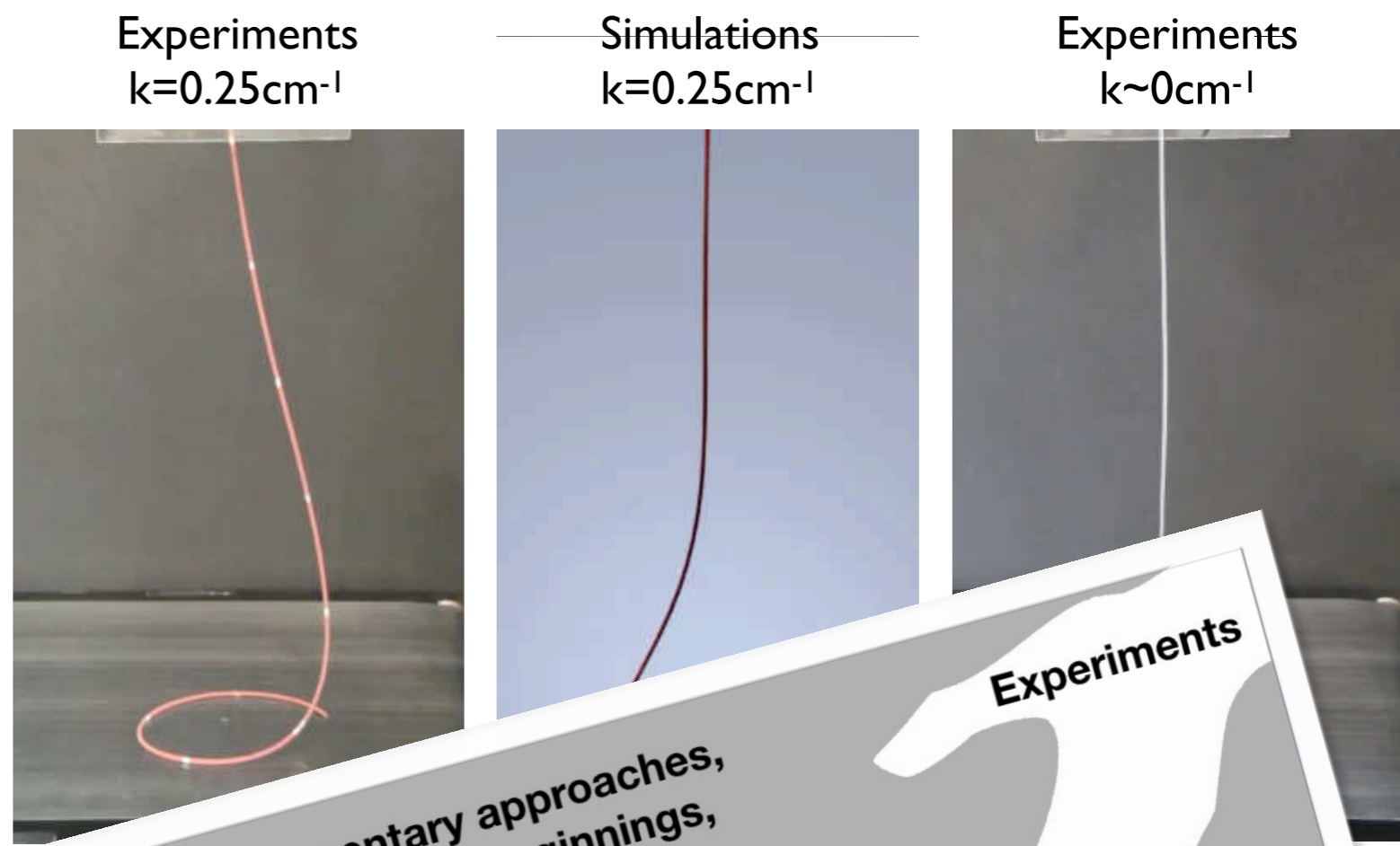
- ▶ Coiling inversion due to torsional buckling;
- ▶ Length of inversion scales with injection height;
- ▶ Excellent agreement with no fitting parameters.

**Curvature Matters!**



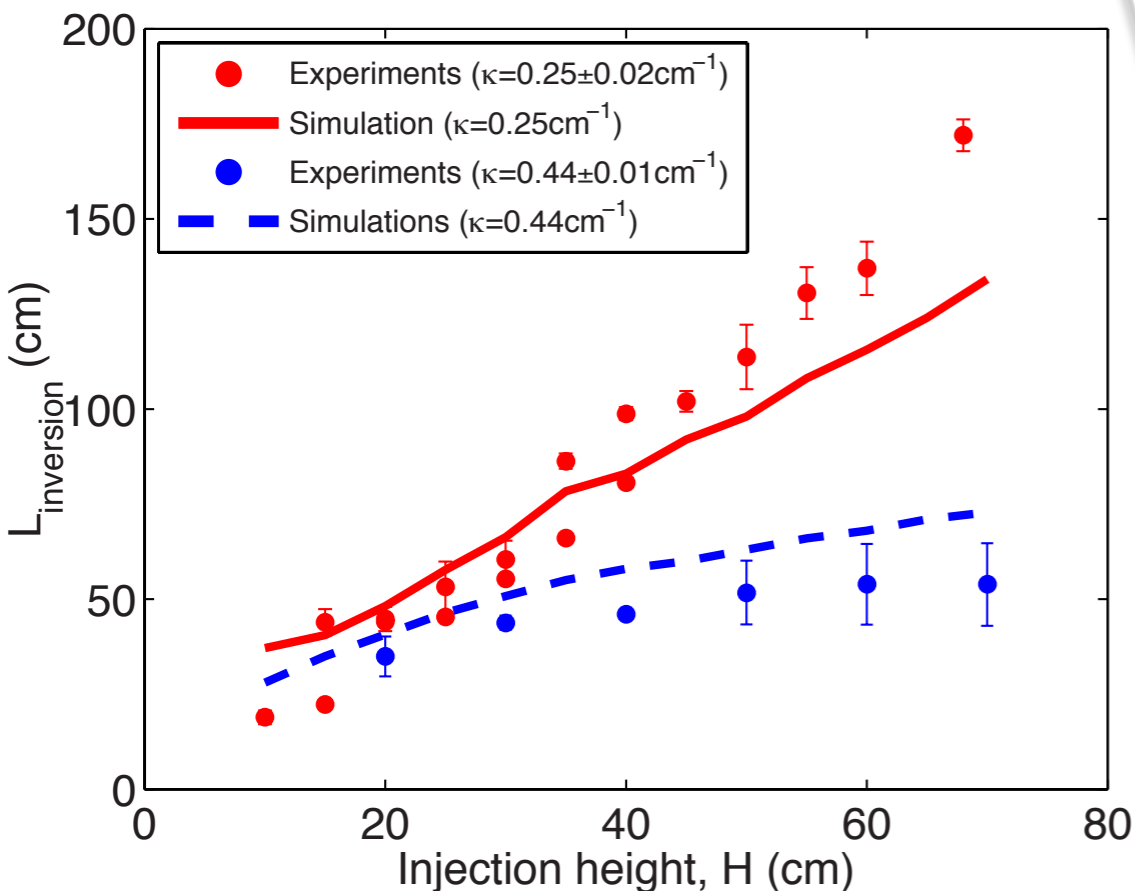
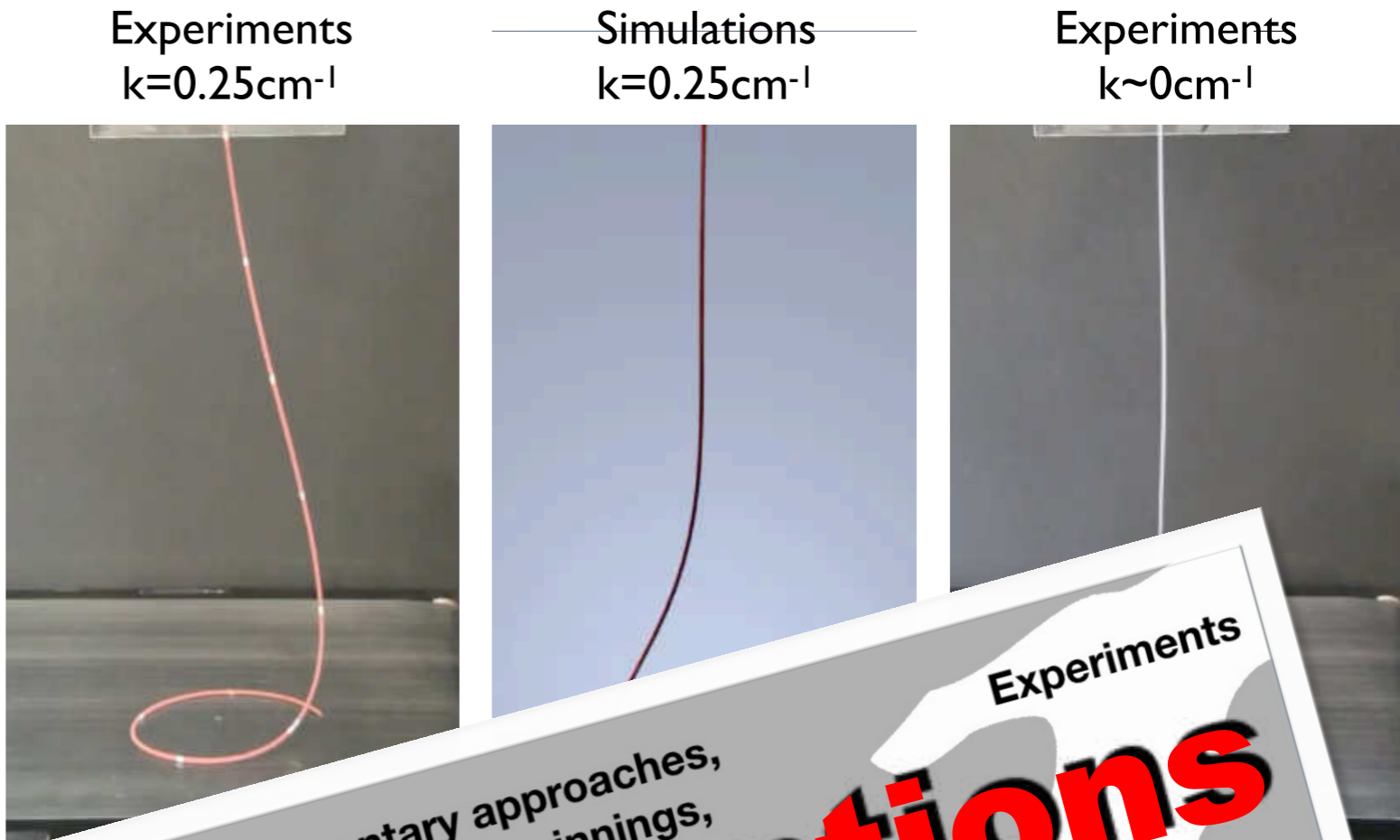
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Complementary approaches, from opposing beginnings, meet at shared picture

# Assumptions

Build up physics

Factor out physics

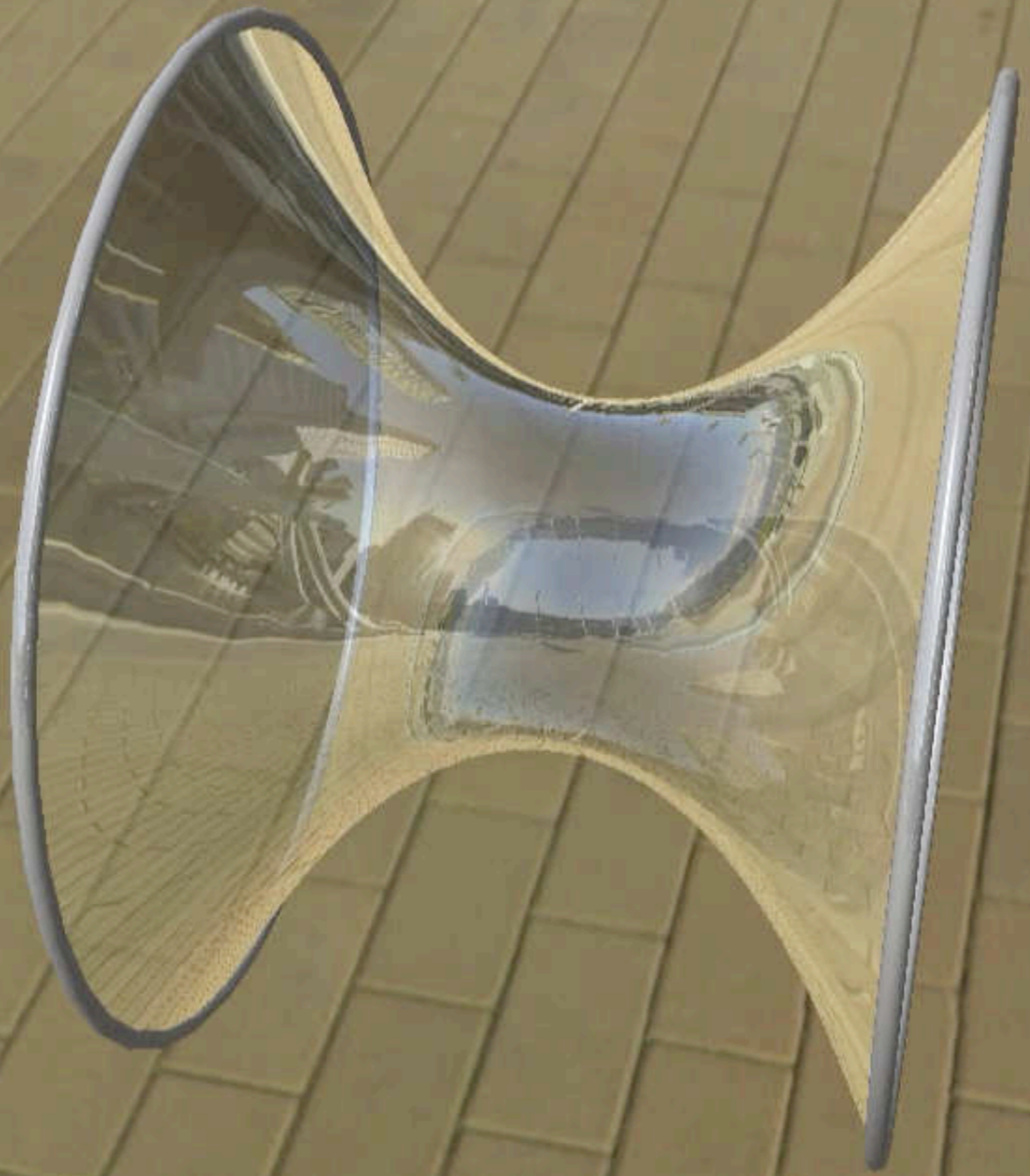
# Discovery

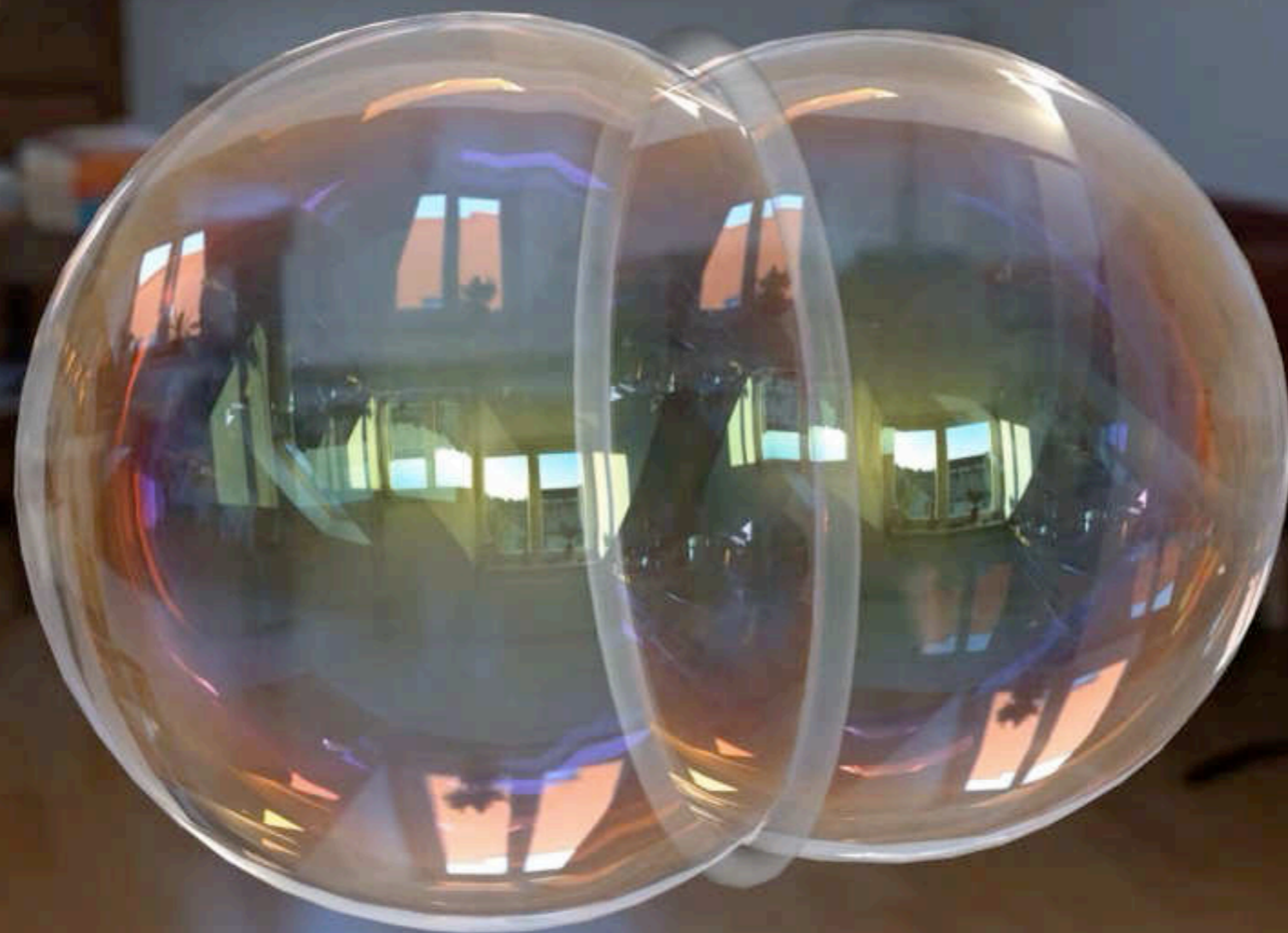
Computation

("capillarity is negligible" - Fabrice)

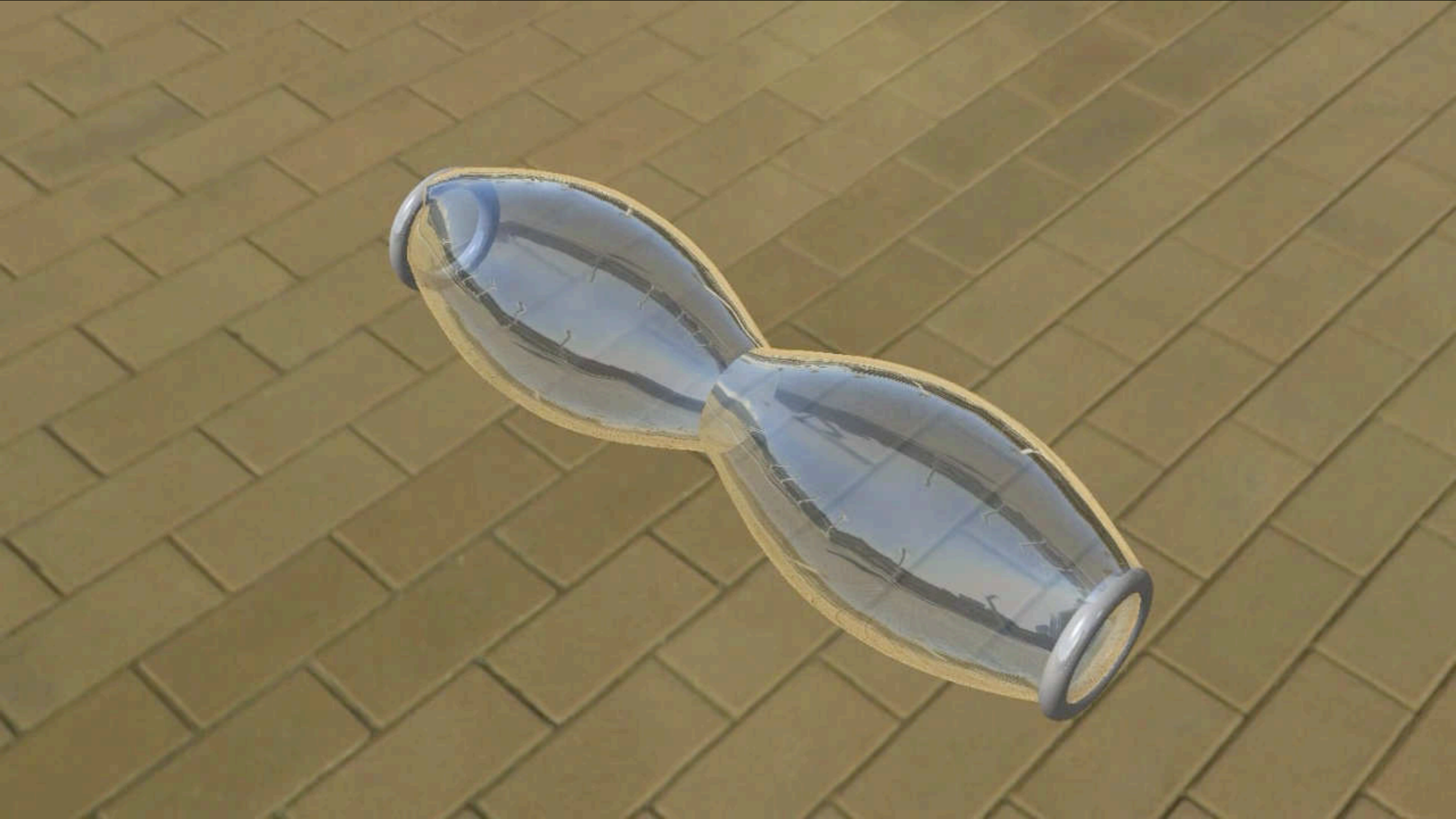
**More assumptions looking  
for collaborators...**







**A bubble trapped in a solid ring**





**Popping bubbles in the cluster**



# Assumptions

Dynamics governed by

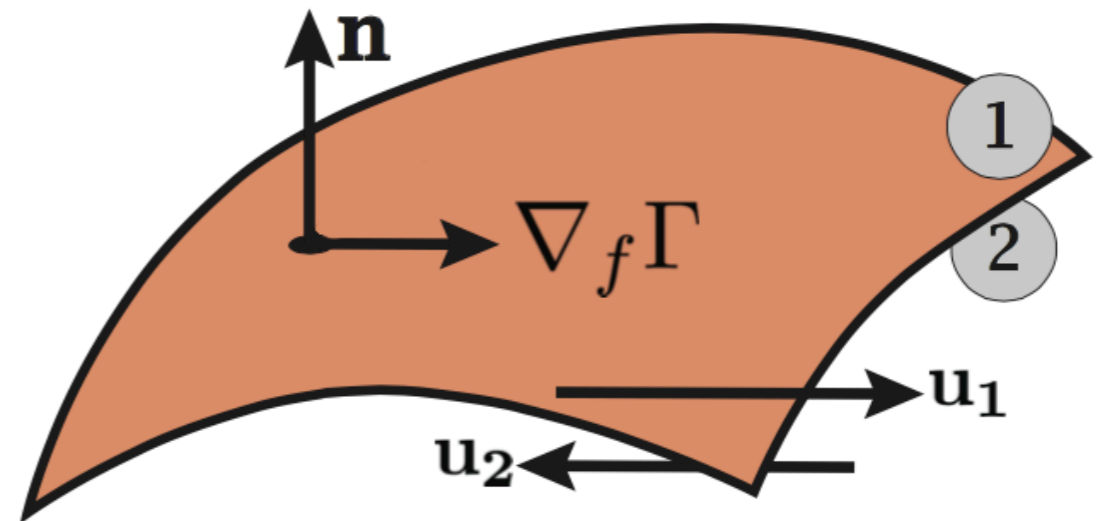
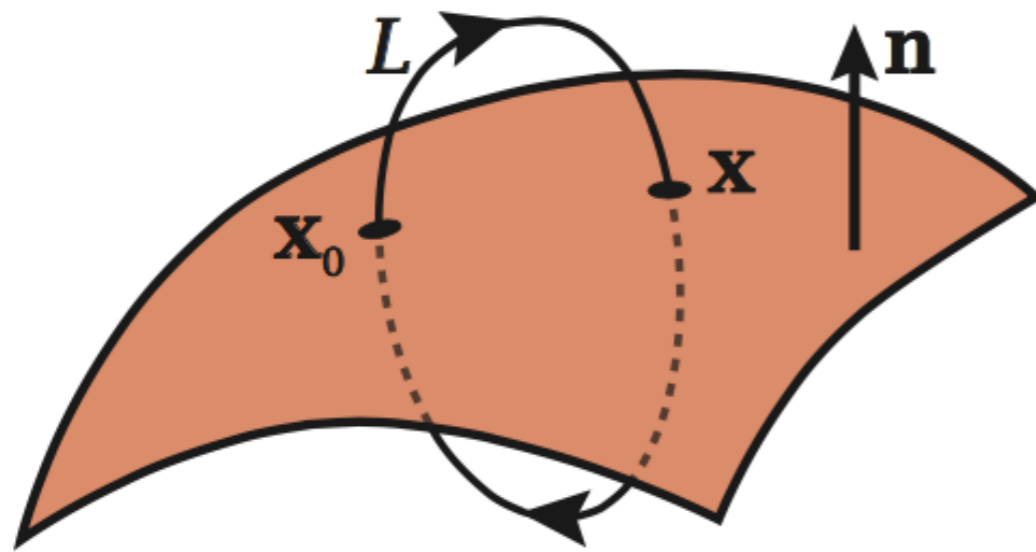
(a) surface tension

(b) inertia of air (neglect liquid inertia)

(c) incompressibility of air

(d) soap film advected in airflow

# Vortex Sheet Representation



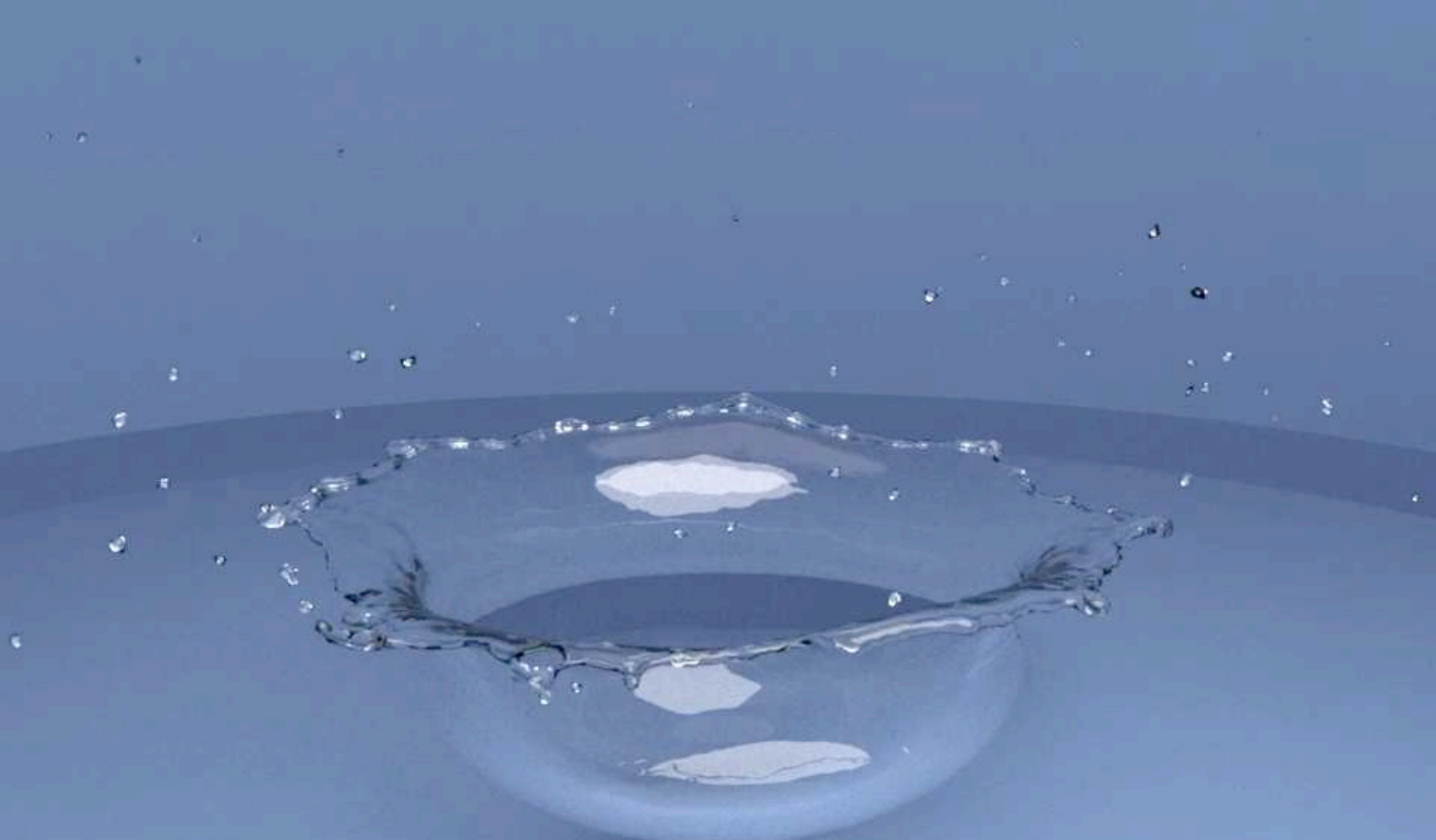
$$\Delta \mathbf{u} = \nabla_f \Gamma$$

**Circulation** =  $\Gamma(\mathbf{x}) = \oint_L \mathbf{u} \cdot d\mathbf{s}$

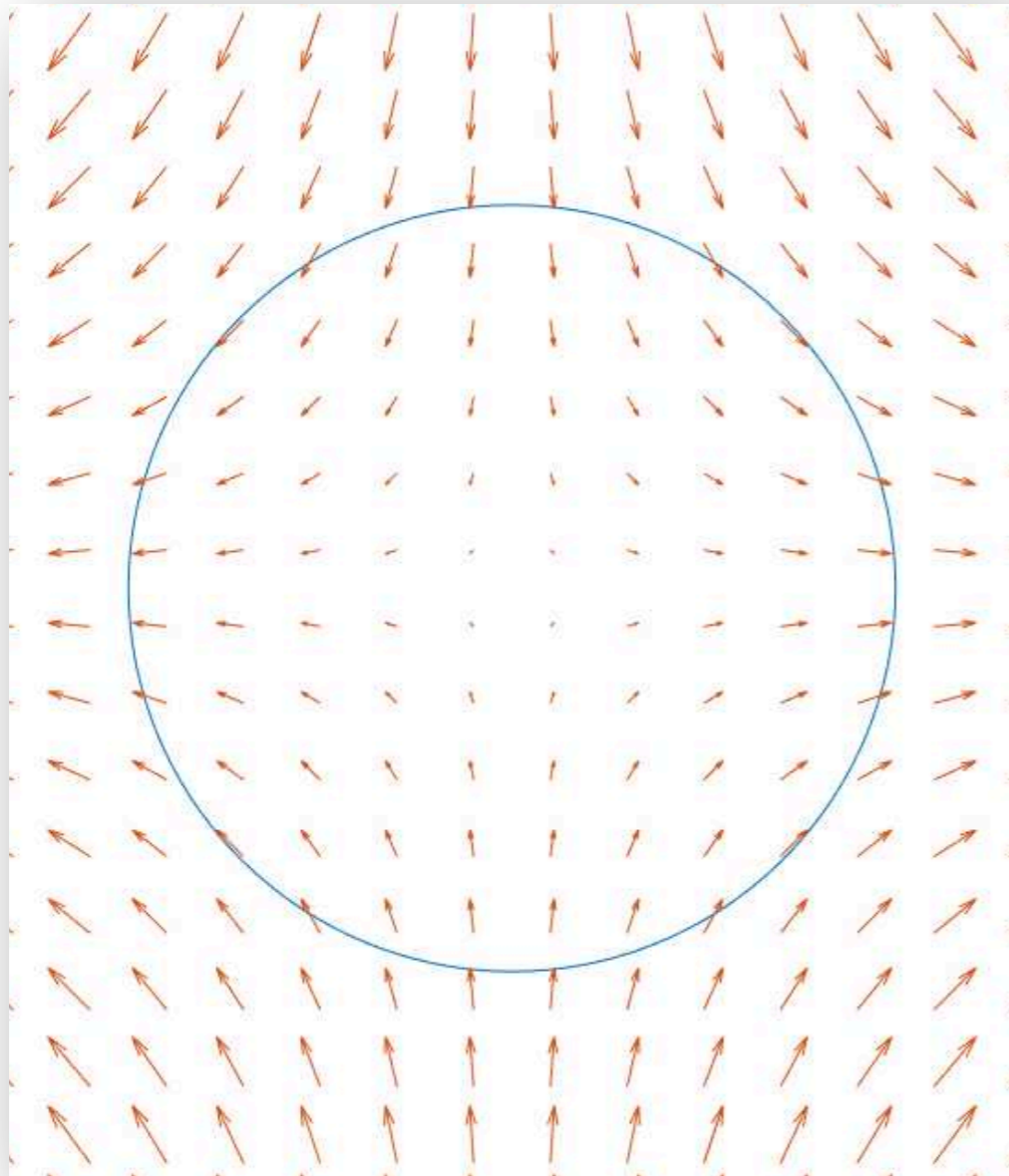
**Temporal evolution**  $\frac{D\Gamma}{Dt} = -\frac{\sigma}{\rho} (H_1 - H_2)$

velocity (air)  $\leftarrow$  (points to \$\mathbf{u}\$ in the circulation equation)

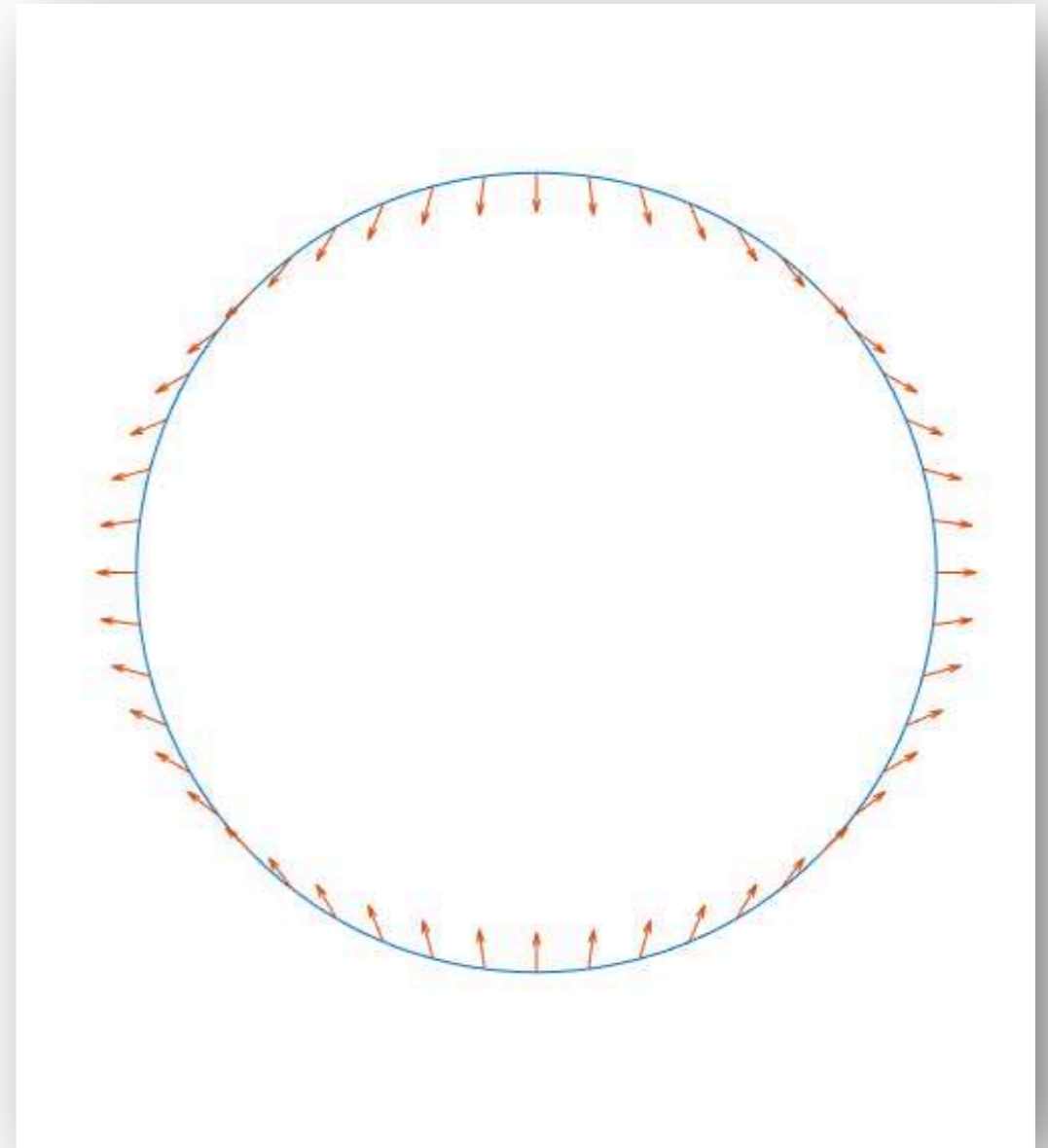
surface tension (mean curvature)  $\leftarrow$  (points to \$H\_1 - H\_2\$ in the temporal evolution equation)



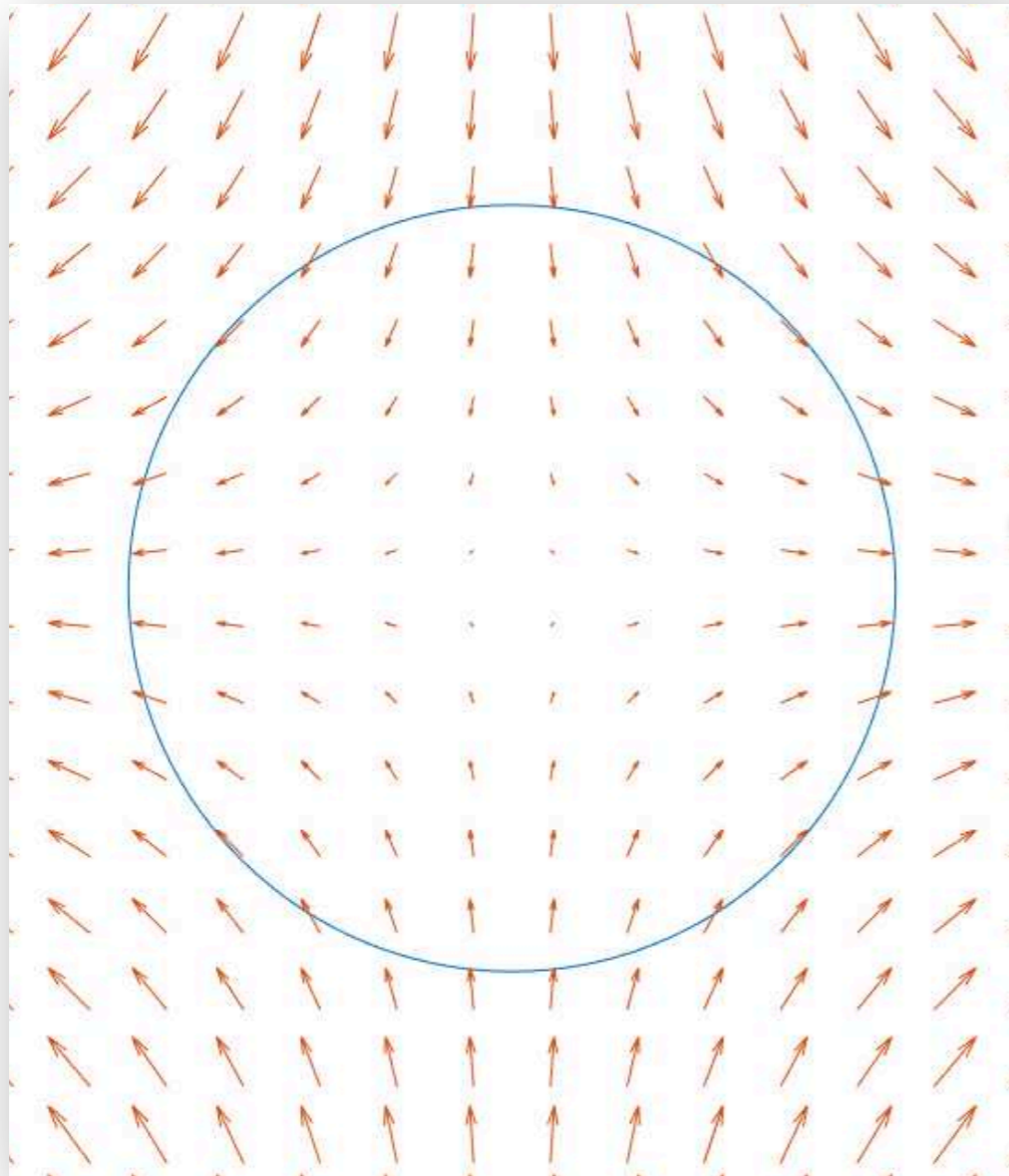
Can you see the flow **beneath** the surface?



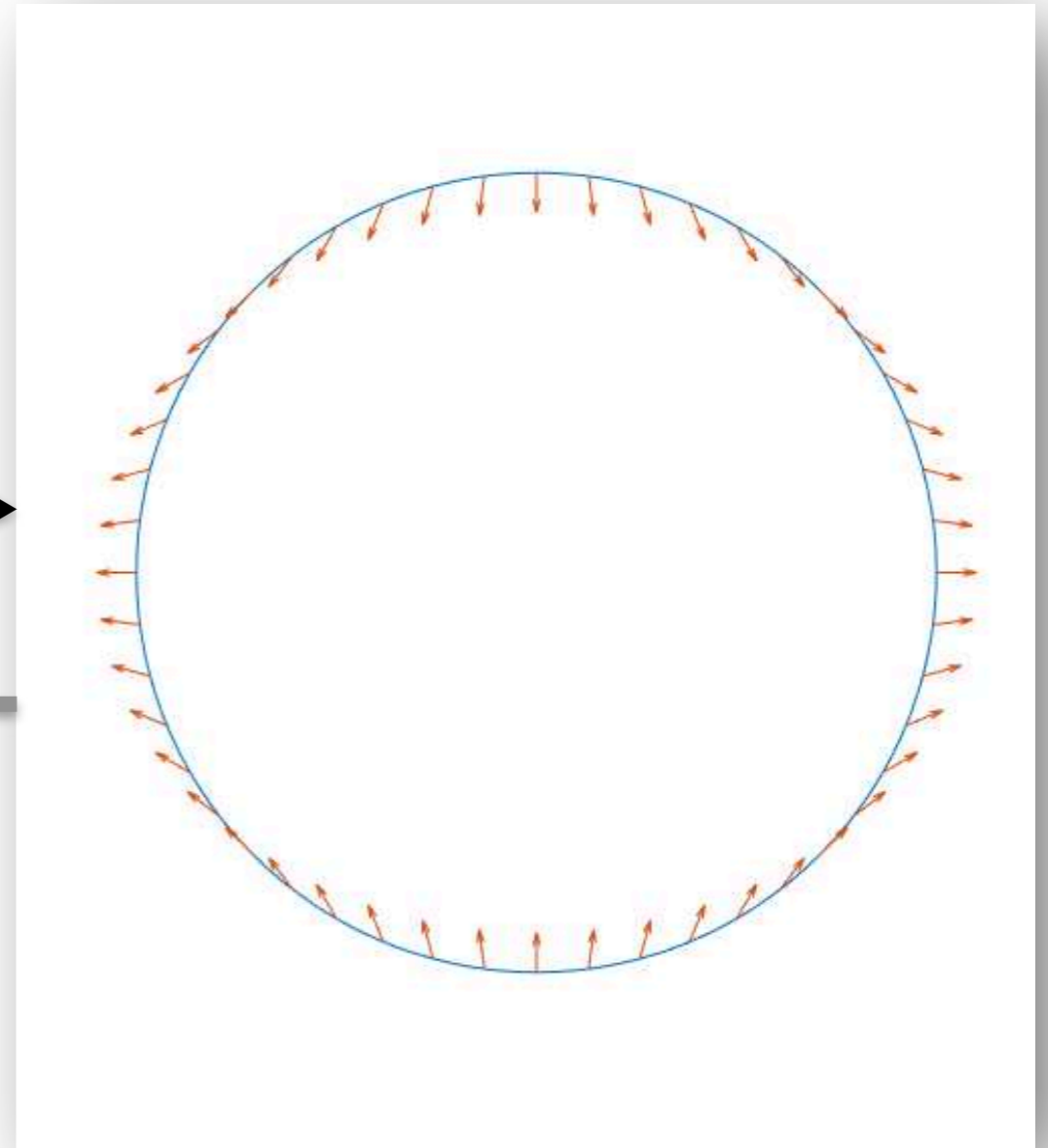
**3D velocity field**



**Surface velocity field**



3D velocity field

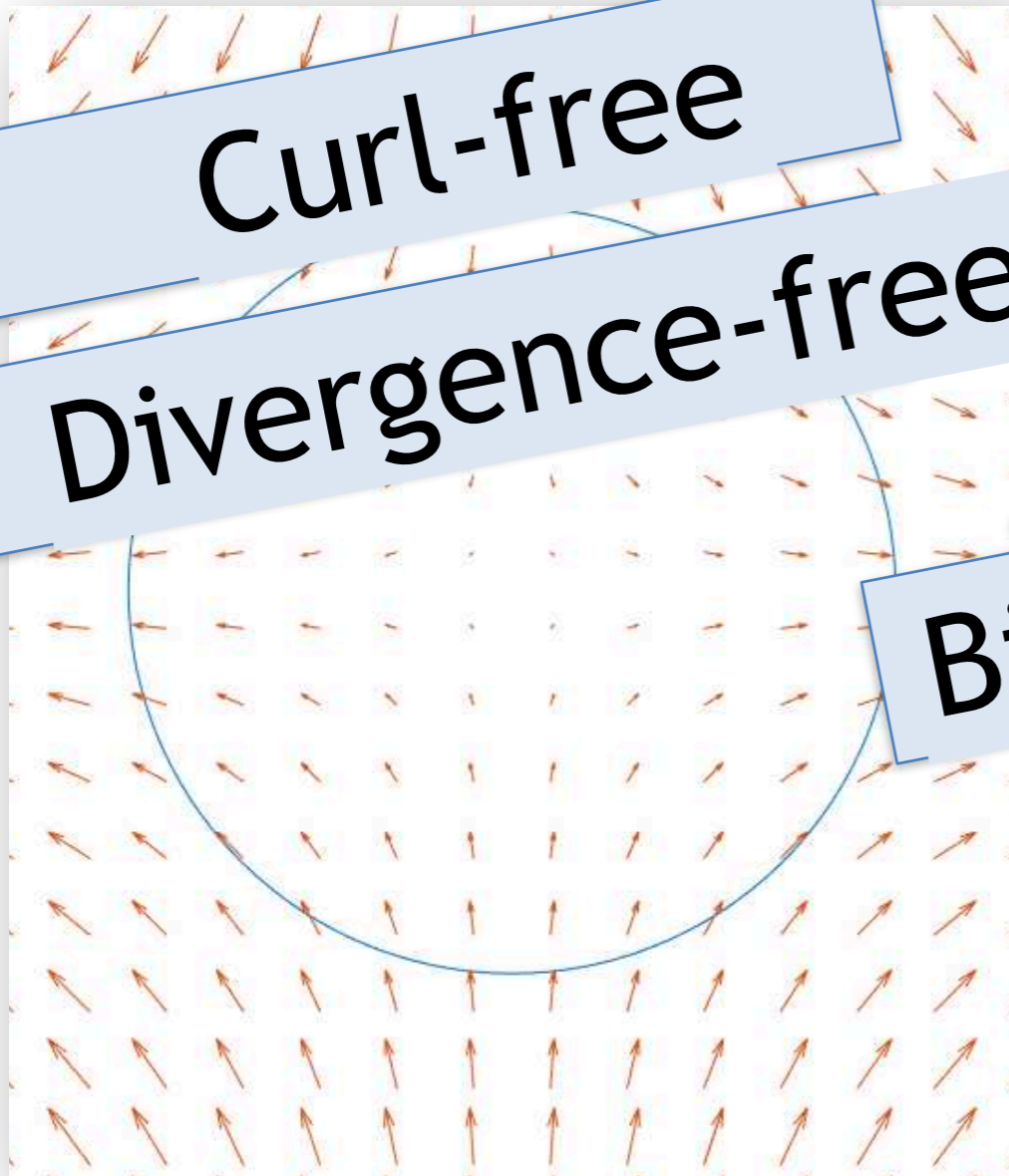


Surface velocity field

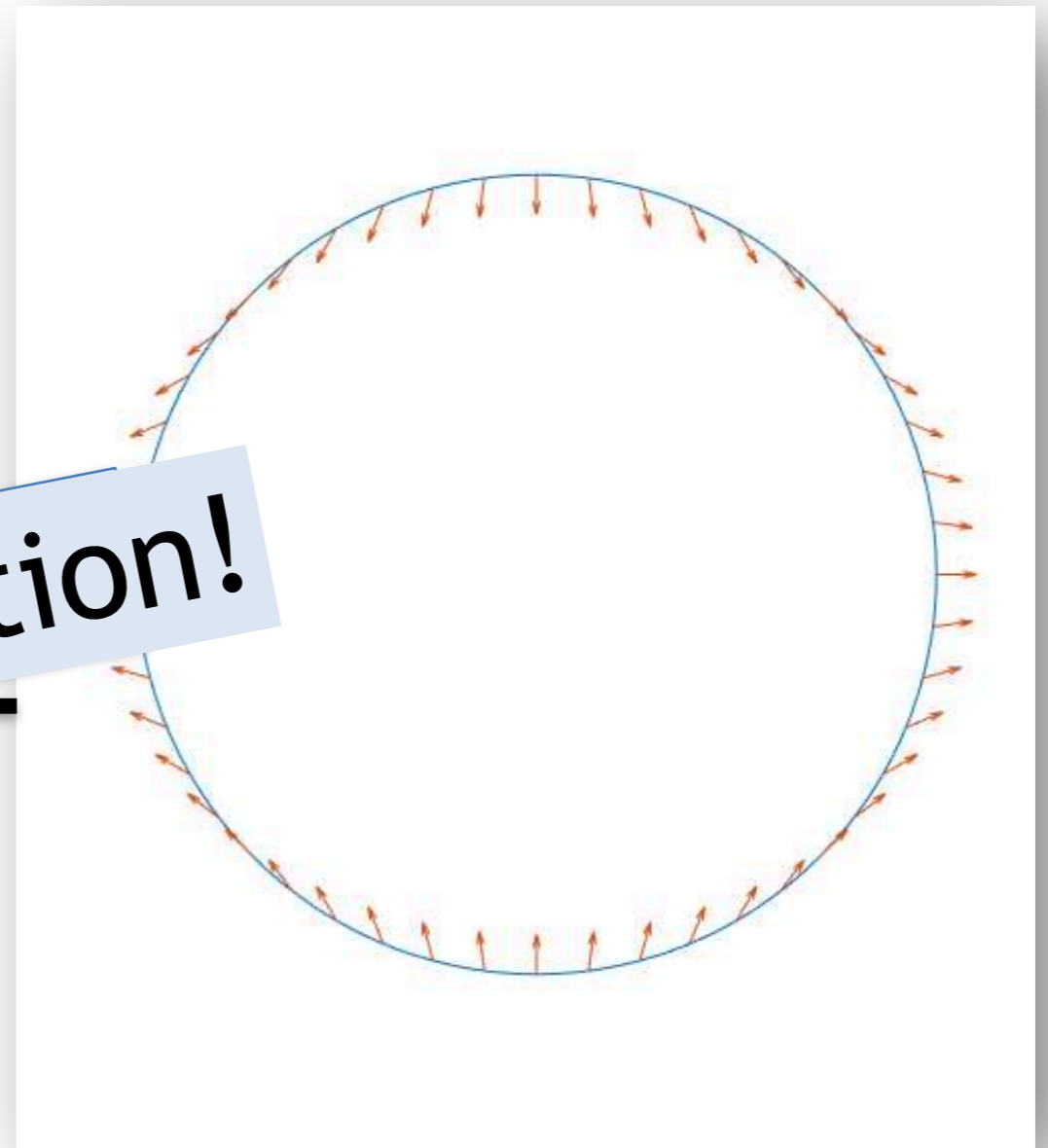
Curl-free

Divergence-free

Bijection!



3D velocity field



Surface velocity field



Curl-free

Divergence-free



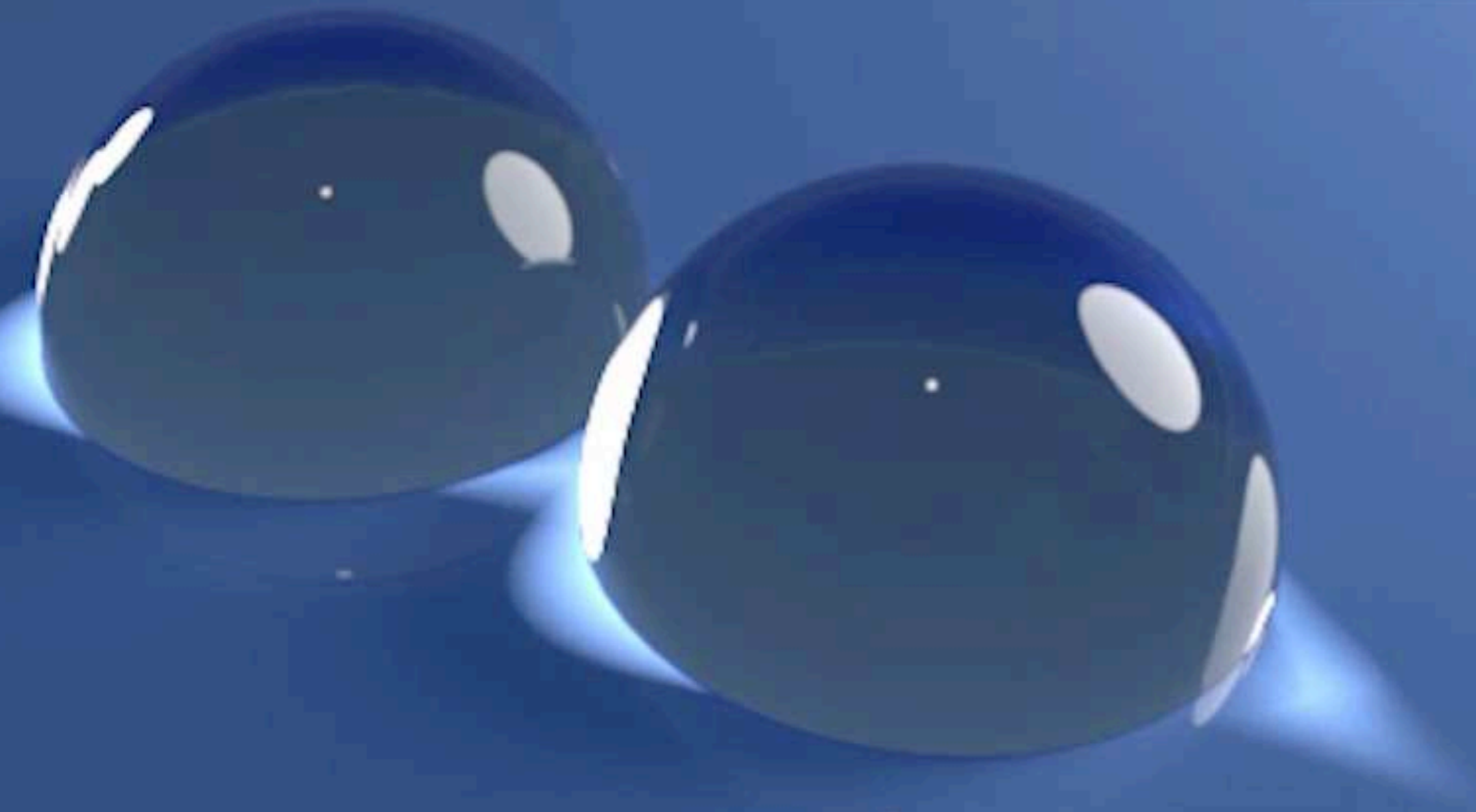
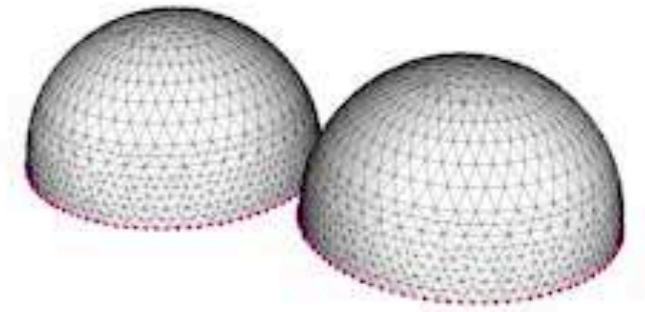
Projection!

# Assumptions

Divergence-Free ← Incompressible

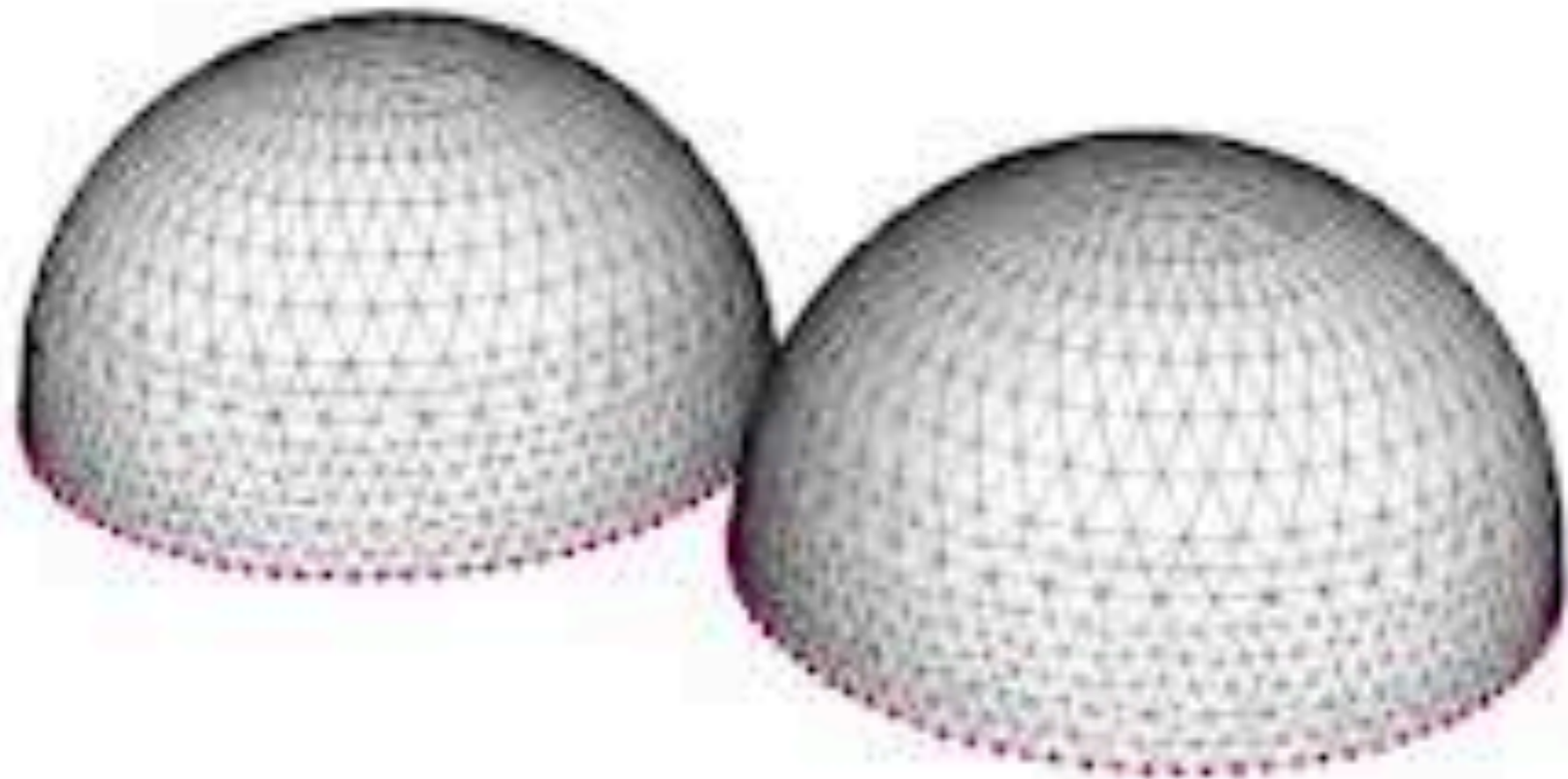
Curl-Free ← Inviscid

# Surface mesh





# Surface mesh



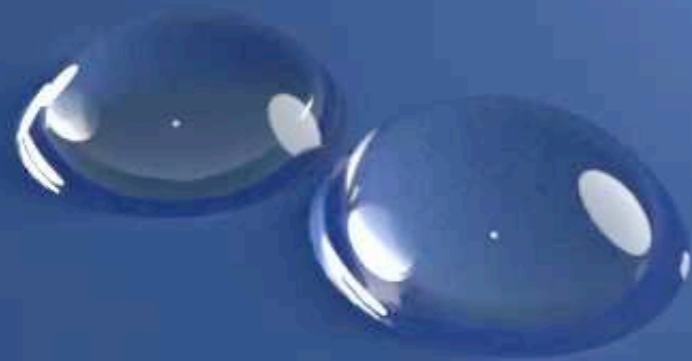
**contact angle =  $45^\circ$**



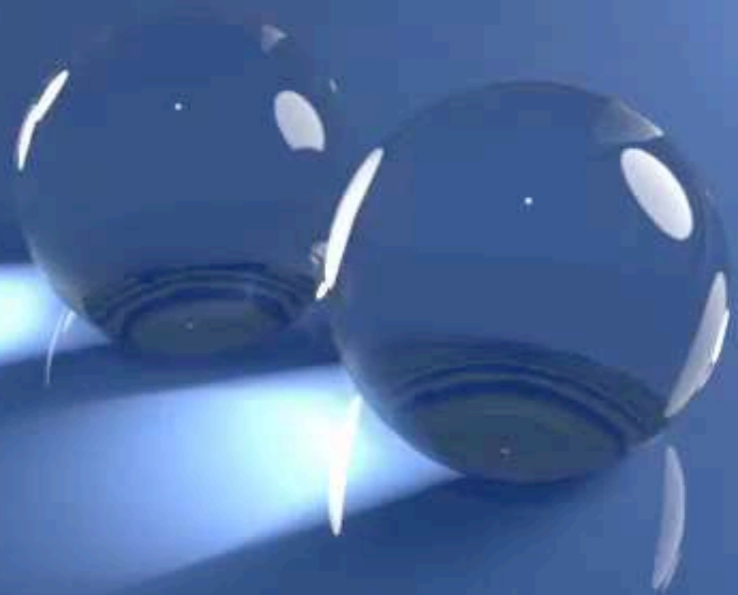
**contact angle =  $120^\circ$**

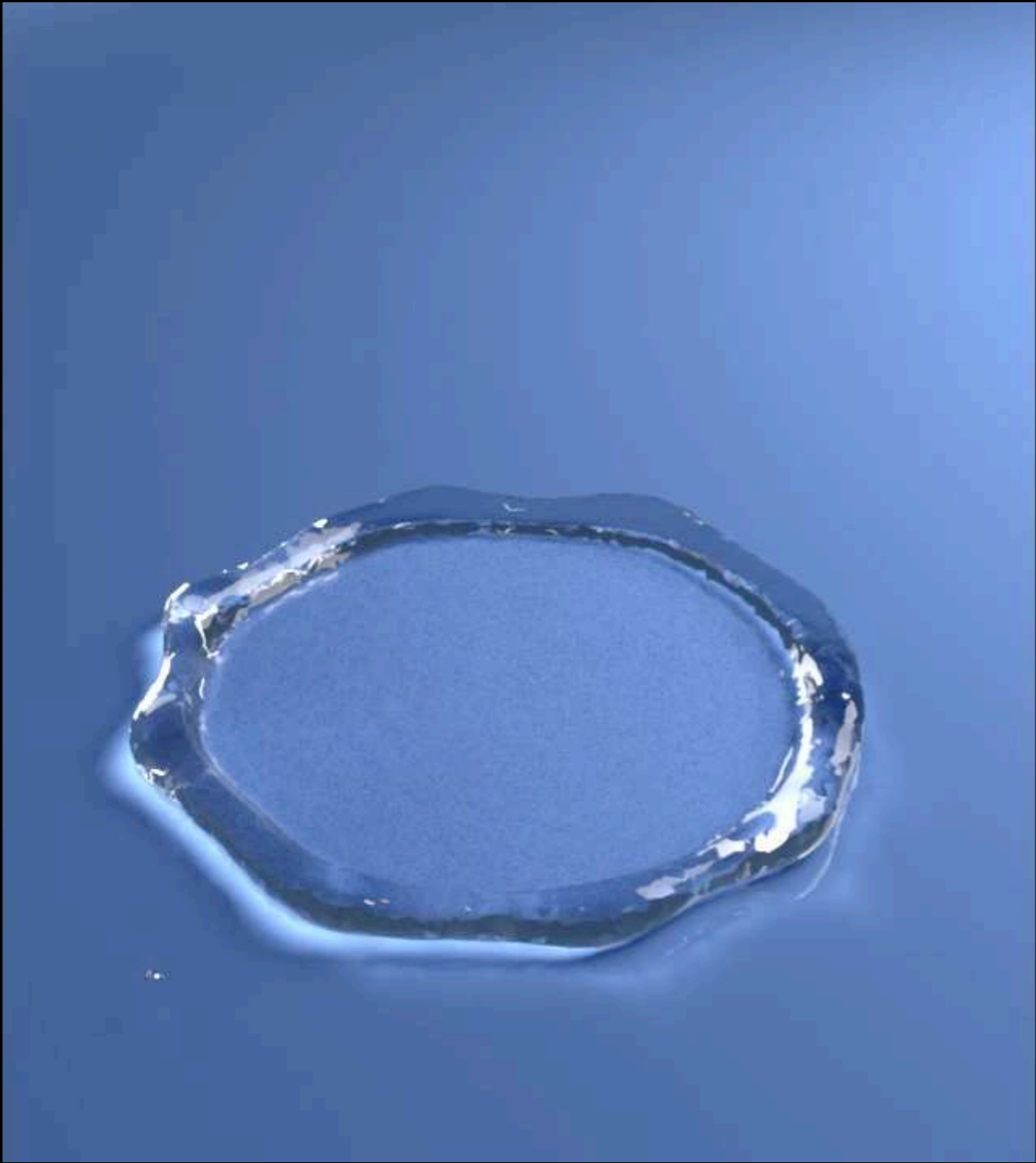


**contact angle =  $60^\circ$**



**contact angle =  $135^\circ$**

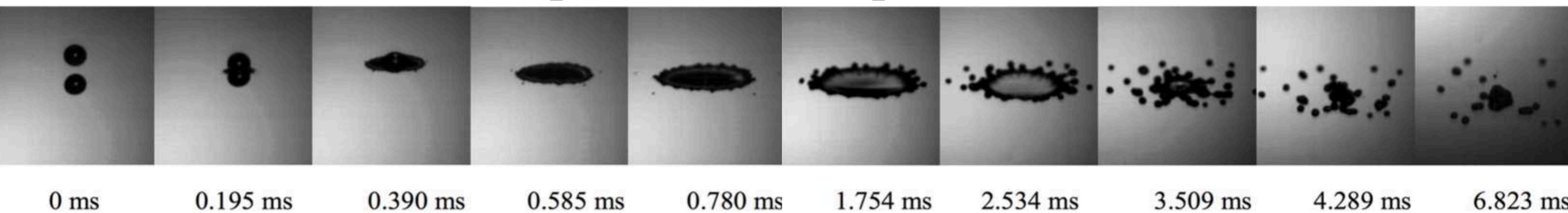




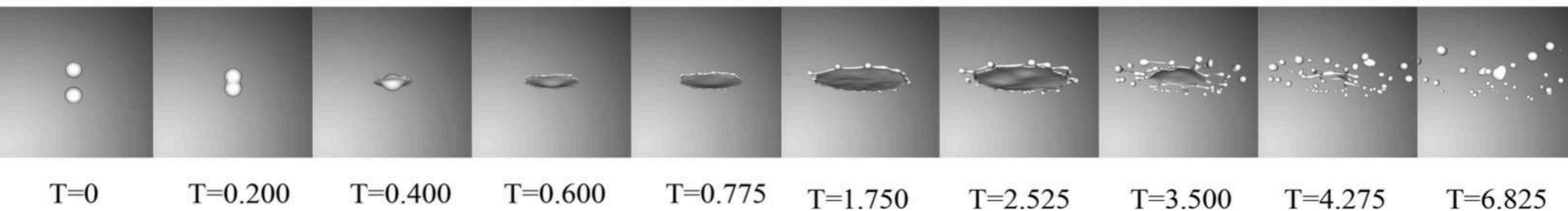




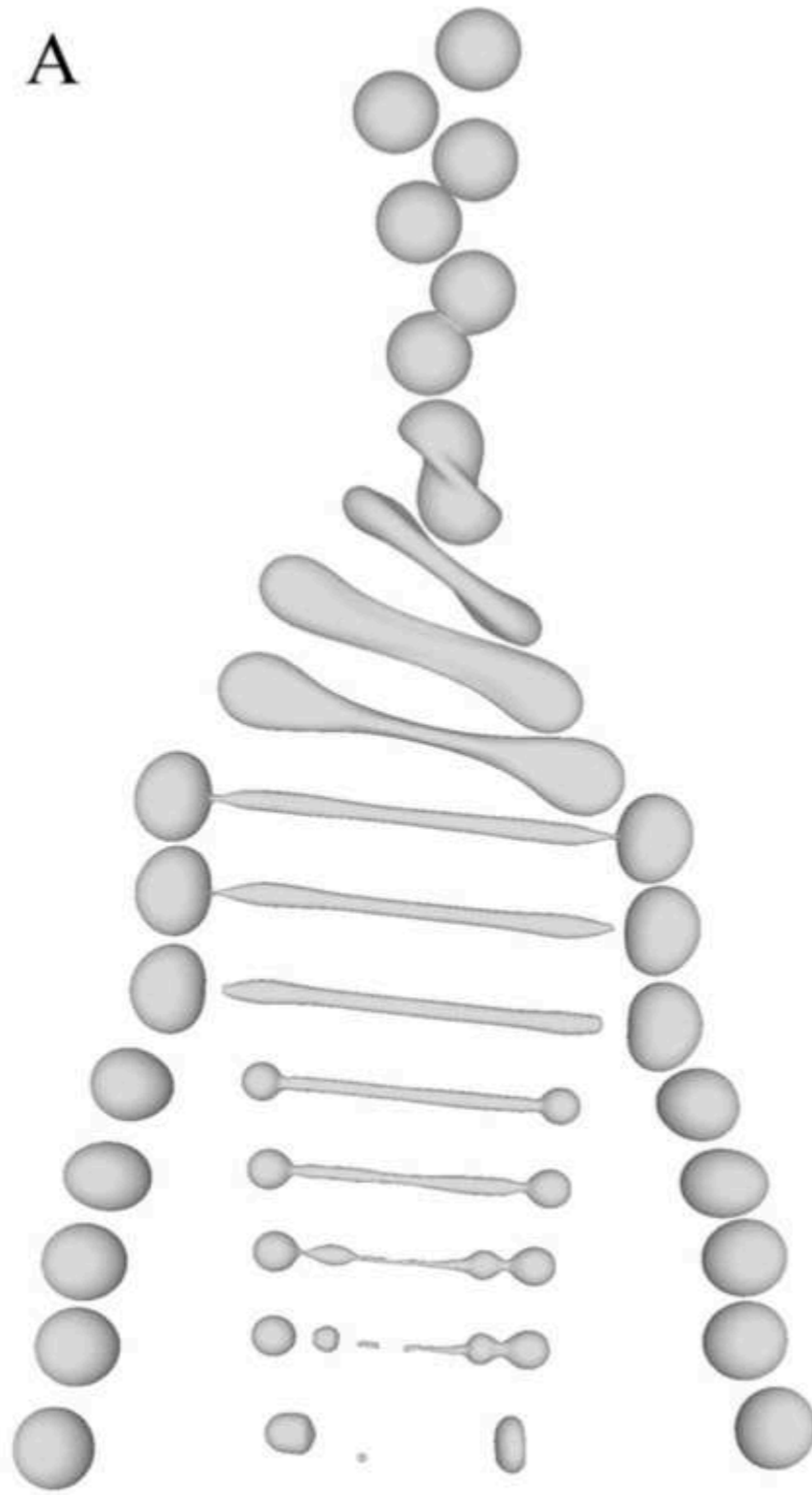
## Physical experiment [Pan et al 2009]



## Our approach

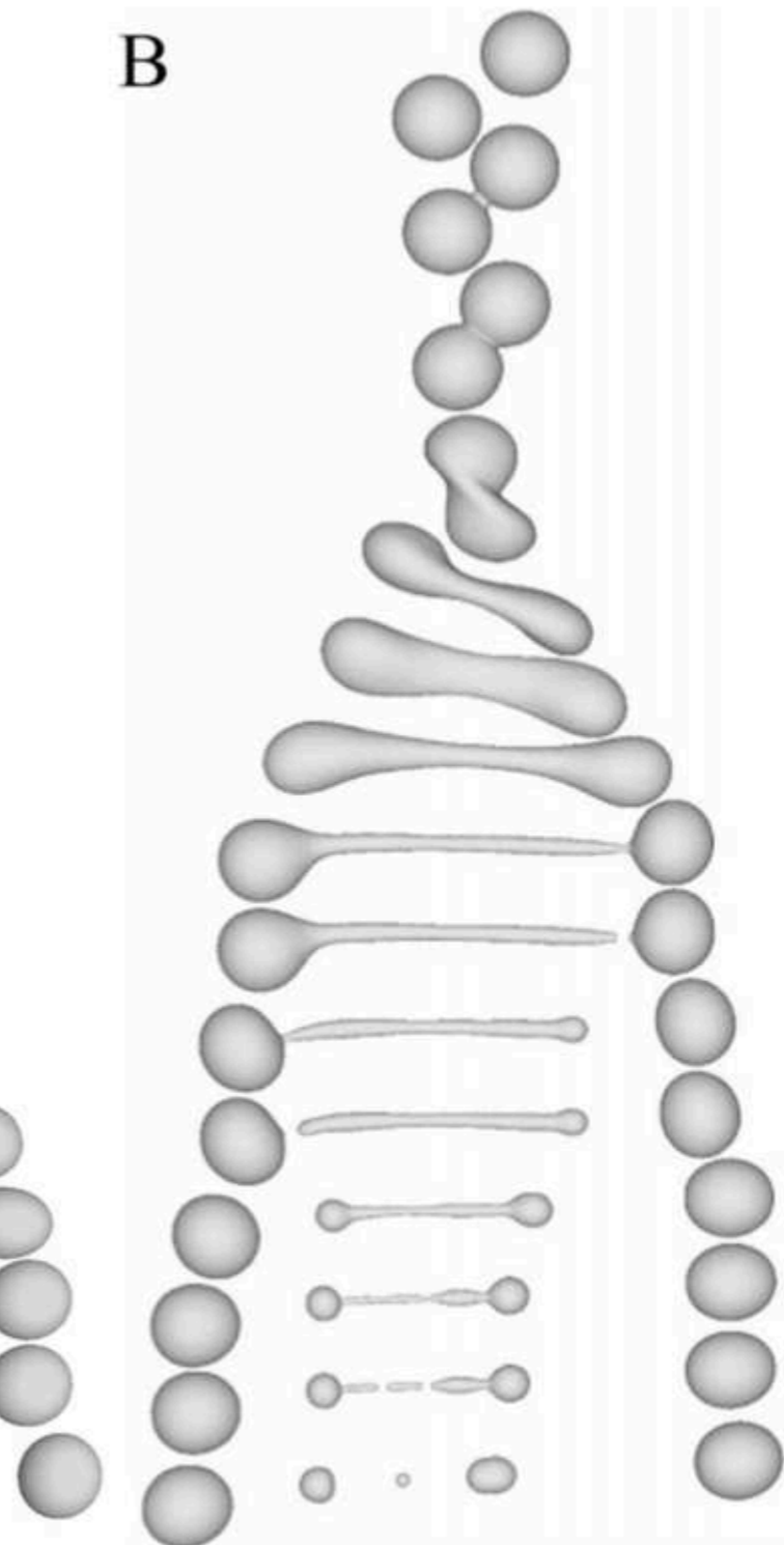


A



Our approach

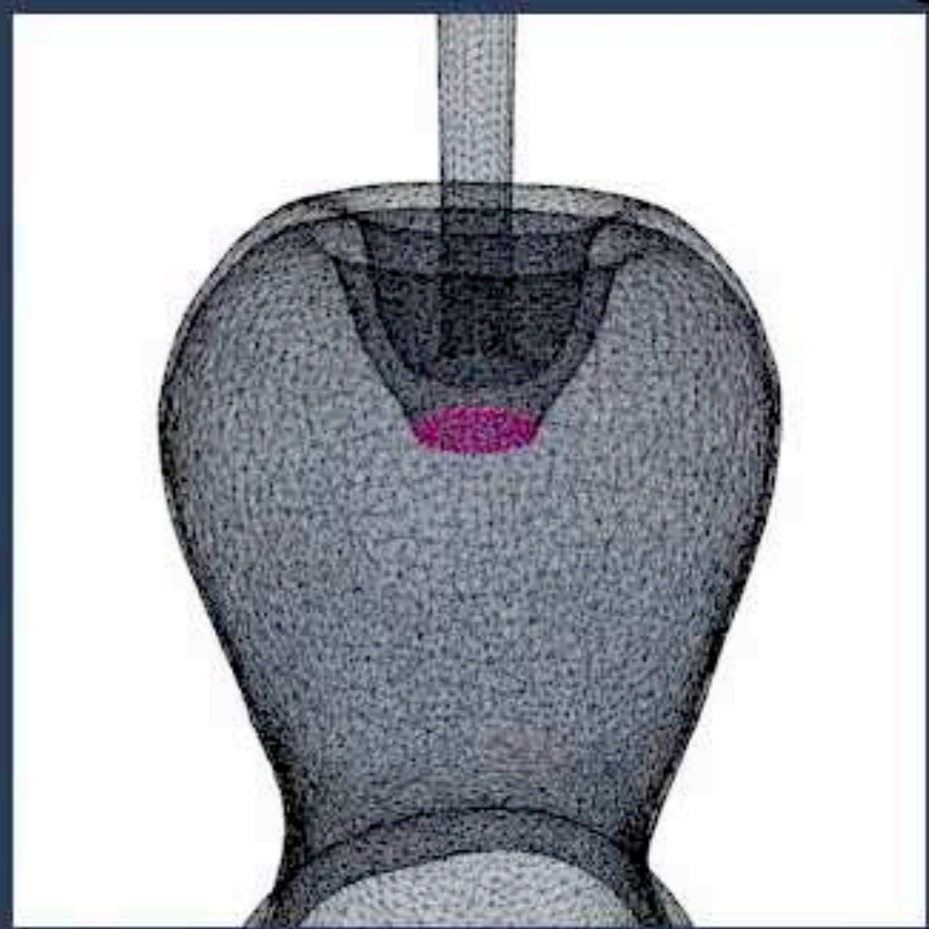
B

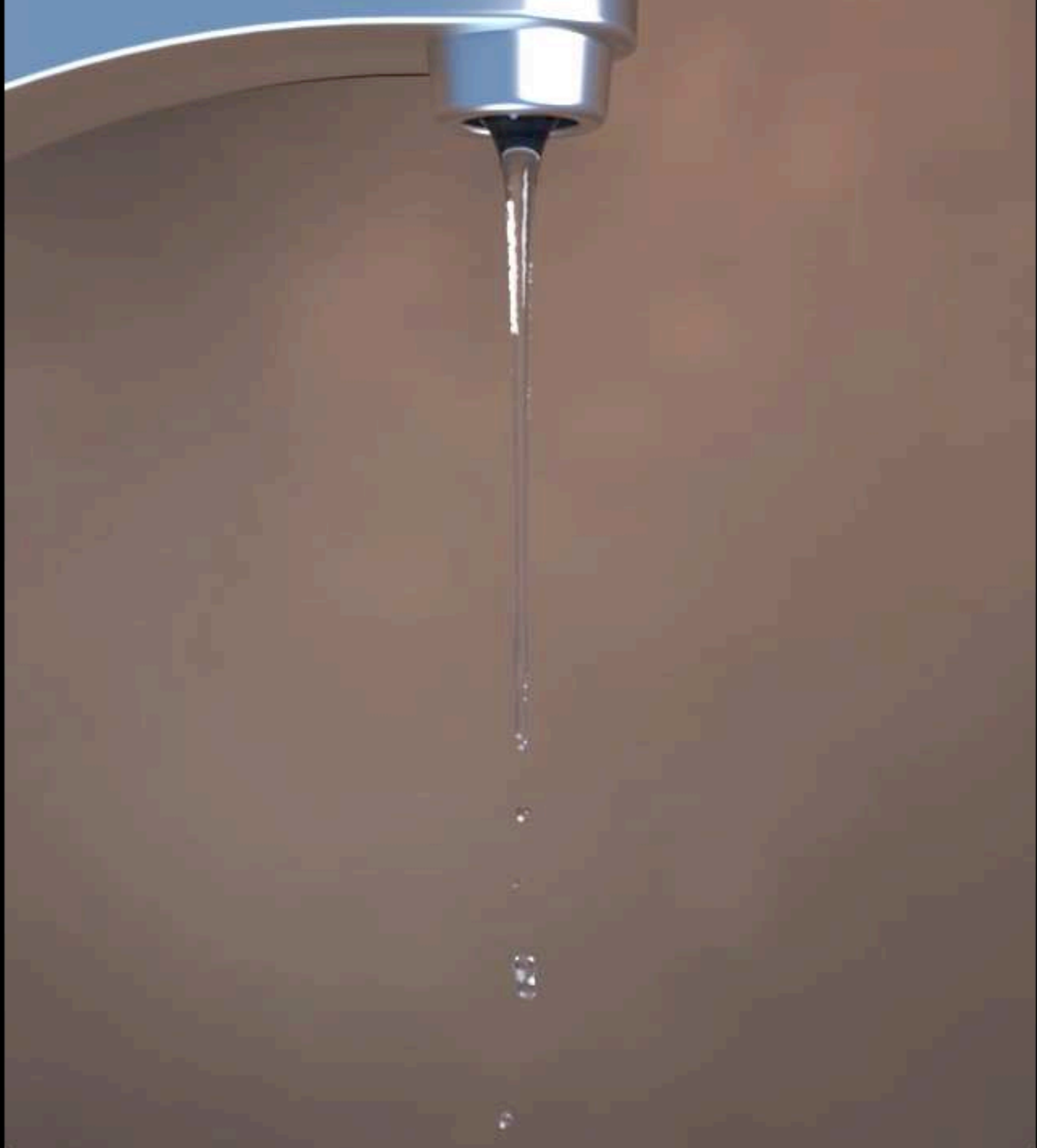


Unstructured tet mesh  
[Quan et al 2009]









**Flow r**



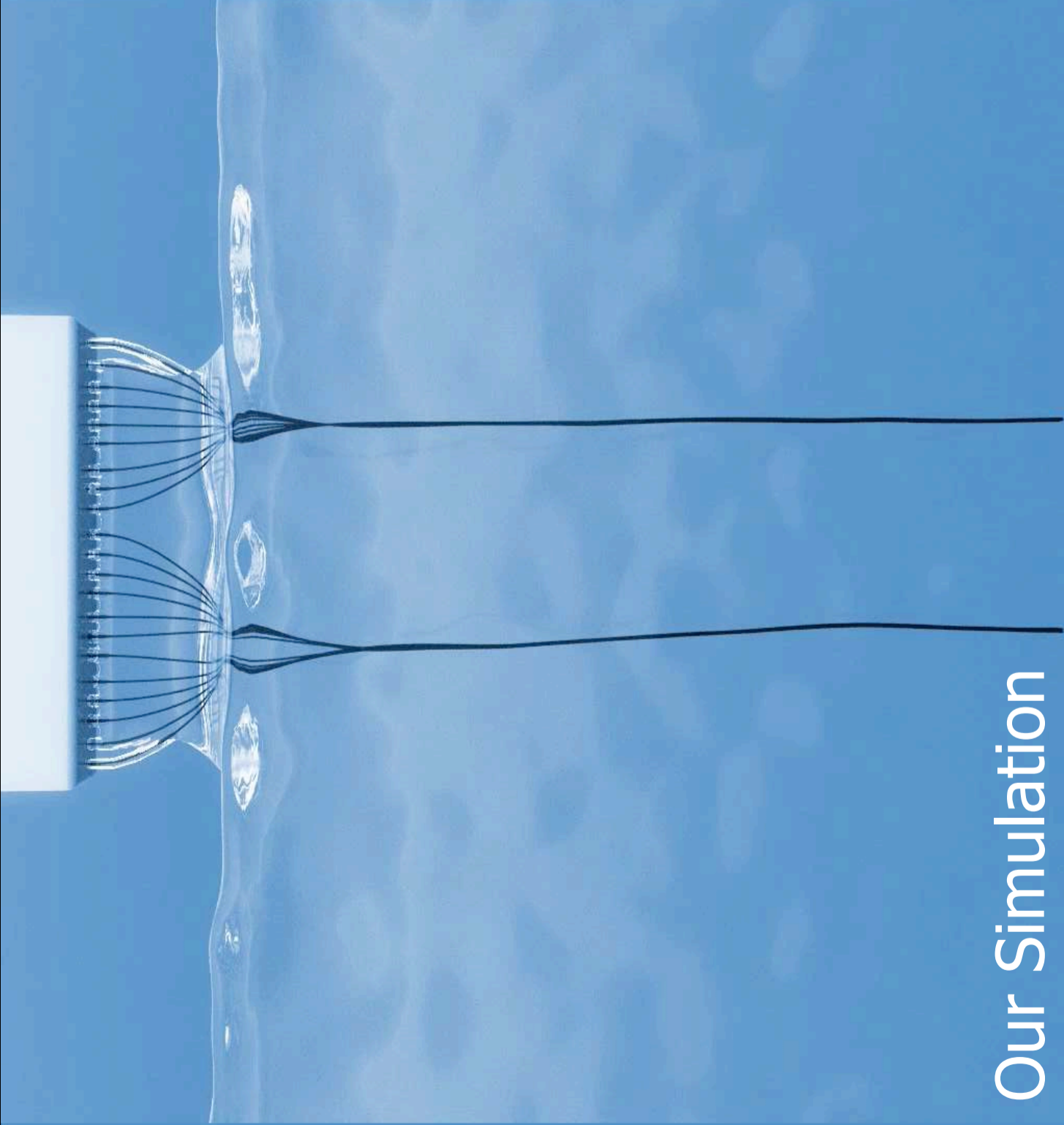
**2**

**10**

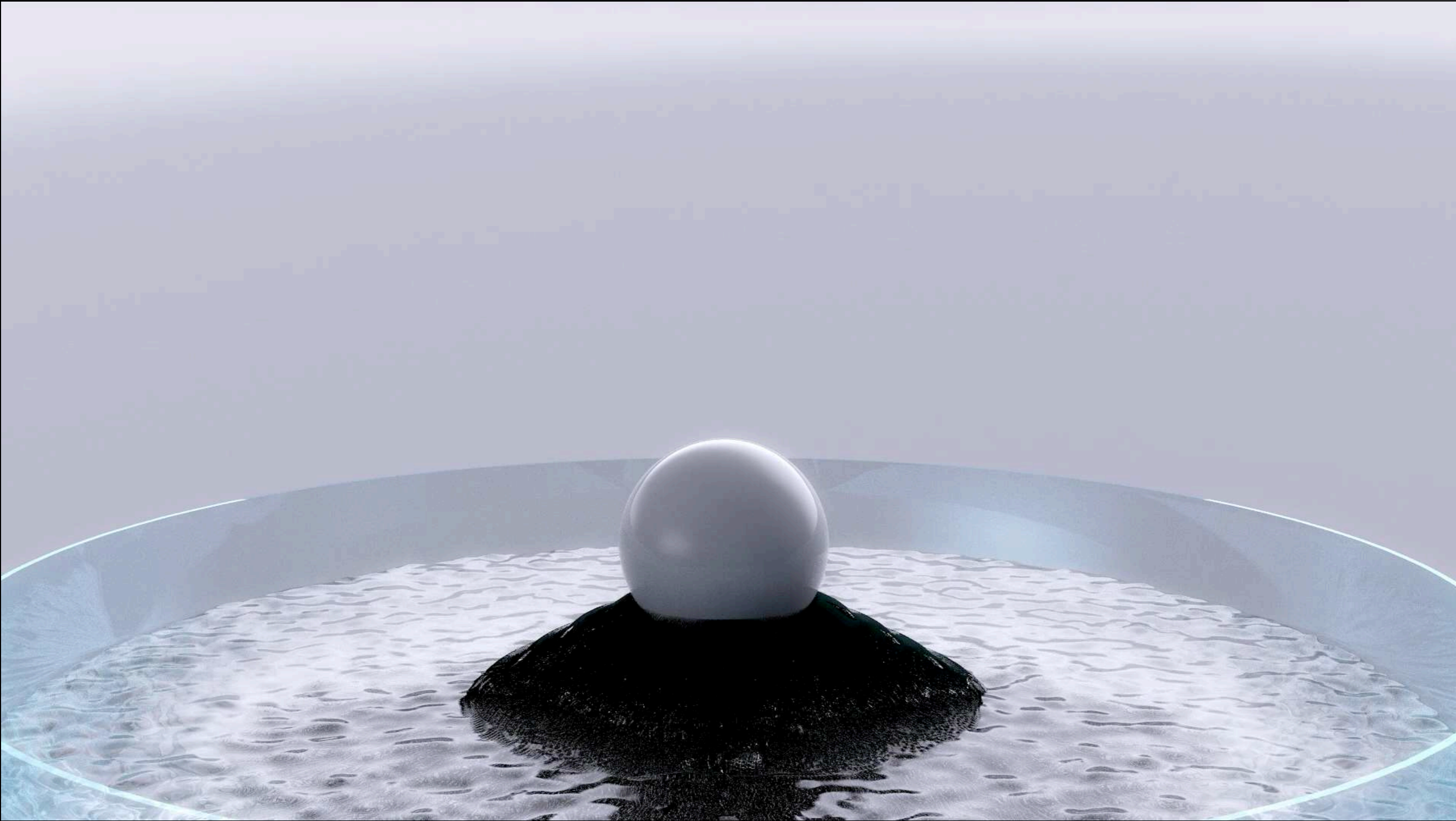




Experiment [Bico et al. 2004]



Our Simulation





cohesion

flow along  
hairs

dripping



# Thank you!



The first Graphics-Physics Workshop