

# *NUMERICAL MODELING OF THE IMPACT OF HYDRATE FORMATION DURING GEOLOGICAL CARBON STORAGE (GCS)*

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# OUTLINE

## ● Introduction

- General context
- CO<sub>2</sub> storage in depleted gas reservoir
- CO<sub>2</sub> storage in deep ocean sediments

## ● Mathematical model

- Non-isothermal reactive compositional multiphase flow in porous media
- Hydrate kinetic reaction
- Joule-Thomson effect

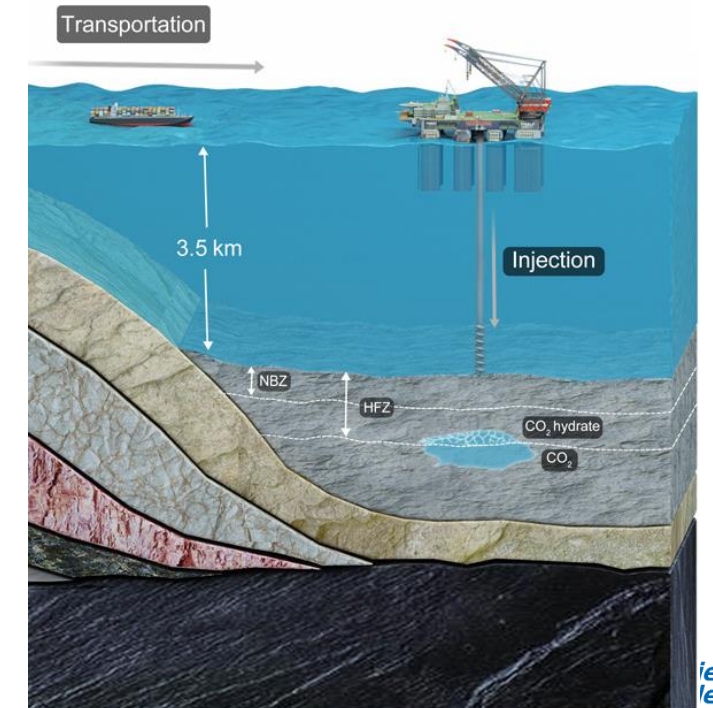
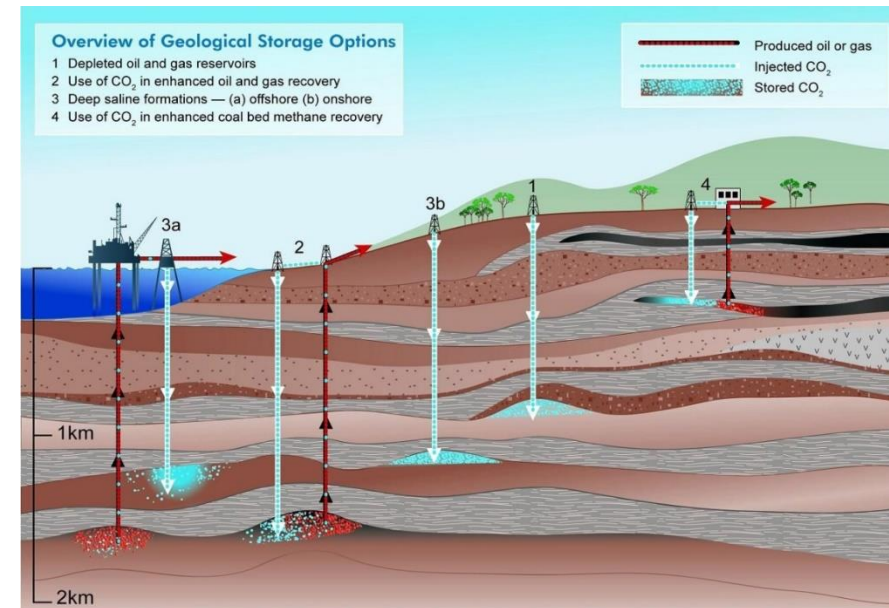
## ● Numerical simulation

# INTRODUCTION



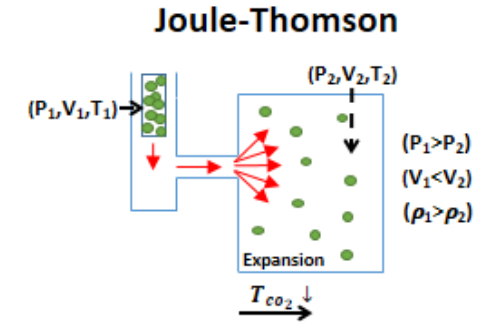
# CONTEXT

- In the last decades, the CO<sub>2</sub> concentration in the atmosphere has dramatically increased due to excessive burning of fossil fuels.
- This greenhouse gas has an important impact on climate change.
- A solution to reduce the concentration of CO<sub>2</sub> in the atmosphere is the **storage in geological formations**:
  - In deep saline aquifers
  - In unmineable coal seams
  - In depleted oil or gas reservoirs
  - In deep ocean sediments

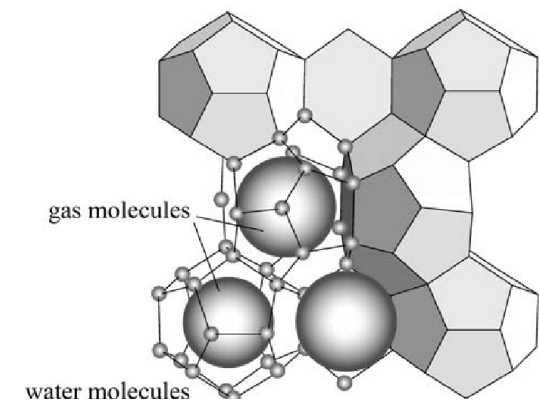
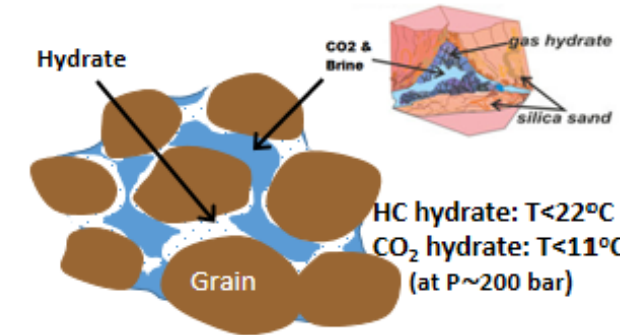


# CO<sub>2</sub> STORAGE IN DEPLETED GAS RESERVOIR

- High pressure injection in low pressure reservoir
- ↓
- Expansion of the gas near the wellbore area:  
Pressure decreases
- ↓
- Temperature decreases due to the **Joule-Thomson (JT) effect**
- ↓
- Possibility of **hydrate formation**
- ↓
- **Loss of injectivity**



## Hydrate formation



Gas hydrate

# CO<sub>2</sub> STORAGE IN DEEP OCEAN SEDIMENTS

- **High pressure and low temperature** in deep ocean environment

- *Hydrate Cap*: Hydrate formation may block the CO<sub>2</sub> plume
- *Gravitational Trapping* : Negative buoyancy may seal the CO<sub>2</sub> plume

$$\rho_{CO_2} > \rho_{H_2O} \Leftrightarrow \rho_{H_2O} - \rho_{CO_2} < 0$$

- A more detailed study can be found in [1]

**[1] A numerical model for offshore Geological Carbon Storage (GCS) undergoing hydrate formation**

Yufei Wang Eric Flauraud, Anthony Michel, Véronique Lachet and Clémentine Meiller,  
Computational Geosciences, July 2024

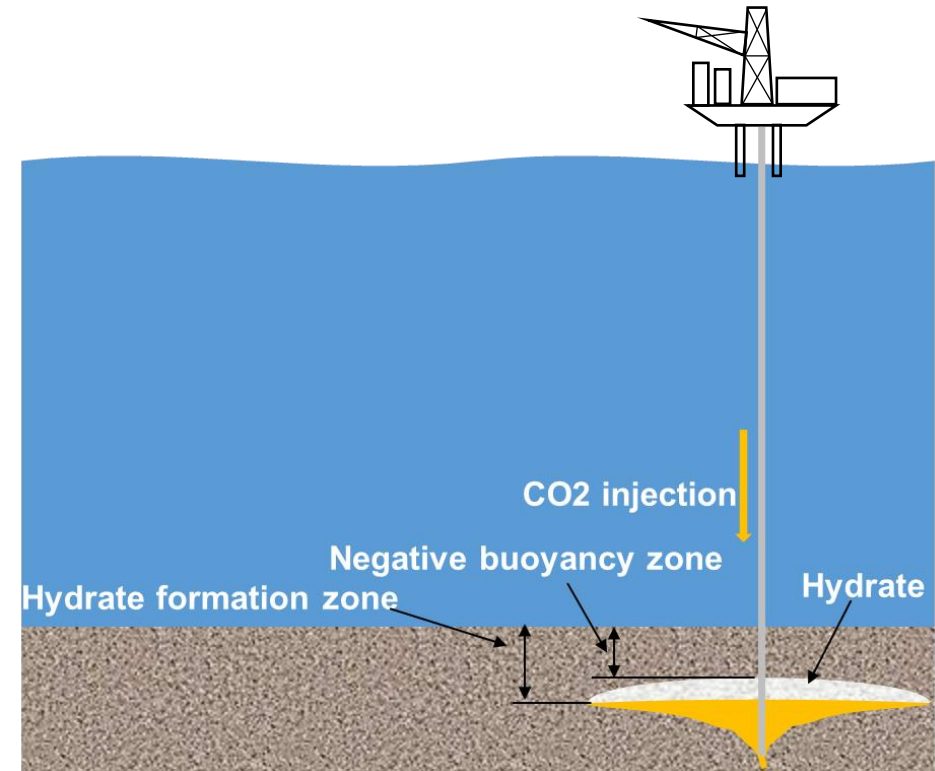


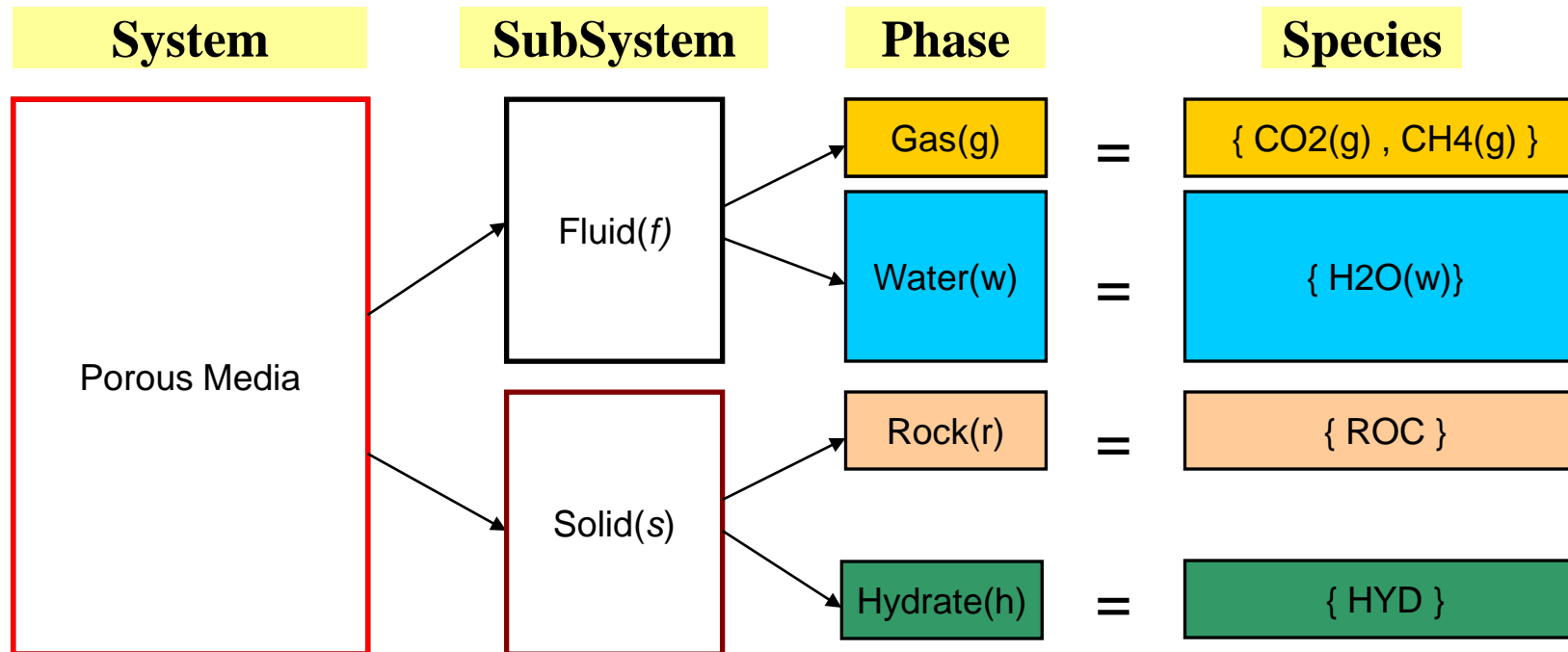
Figure: Injecting and storing CO<sub>2</sub> in the deep ocean sediment

# MATHEMATICAL MODEL



# NON-ISOTHERMAL REACTIVE COMPOSITIONAL MULTIPHASE FLOW IN POROUS MEDIA

- Example of multiphase compositional system formulation





# NON-ISOTHERMAL REACTIVE COMPOSITIONAL MULTIPHASE FLOW IN POROUS MEDIA

## ● Conservation equations

$$\frac{\partial}{\partial t} (\phi_f S_g \rho_g X_{CO_2}^g) + \text{div}(\rho_g X_{CO_2}^g \vec{v}_g) + Q_{CO_2} + R_{CO_2} = 0 \quad (CO_2)$$

$$\frac{\partial}{\partial t} (\phi_f S_g \rho_g X_{CH_4}^g) + \text{div}(\rho_g X_{CH_4}^g \vec{v}_g) + Q_{CH_4} = 0 \quad (CH_4)$$

$$\frac{\partial}{\partial t} (\phi_f S_w \rho_w X_{H_2O}^w) + \text{div}(\rho_w X_{H_2O}^w \vec{v}_w) + Q_{H_2O} + R_{H_2O} = 0 \quad (H_2O)$$

$$\frac{\partial}{\partial t} (\phi_s S_r \rho_r X_{ROC}^r) = 0 \quad (ROC)$$

$$\frac{\partial}{\partial t} (\phi_s S_h \rho_h X_{HYD}^h) + R_{HYD} = 0 \quad (HYD)$$

## ● Closure equations

$$\phi_f + \phi_s = 1$$

$$S_w + S_g = 1$$

$$X_{H_2O}^w = 1$$

$$X_{ROC}^r = 1$$

$$S_r + S_h = 1$$

$$X_{CO_2}^g + X_{CH_4}^g = 1$$

$$X_{HYD}^h = 1$$

## ● Darcy law

$$\vec{v}_\alpha = -K \frac{kr_\alpha}{\mu_\alpha} (\vec{\nabla} P_\alpha - \rho_\alpha^m \vec{g}) \quad \alpha = w, g$$

## ● Permeability law

$$K(\phi_f) = K_0 e^{c \left( \frac{\phi_f}{\phi_0} - 1 \right)}$$

# CO<sub>2</sub> HYDRATE KINETIC FORMATION/DISSOCIATION

- Chemical reaction:



where  $n_h$  is the hydrate number  $n_h \approx 6$

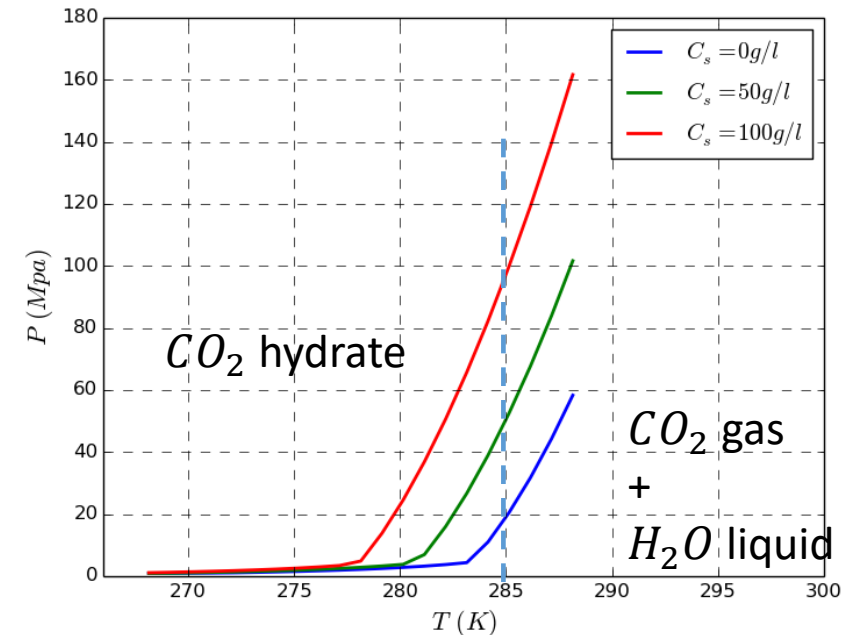
- Reaction rate  $\tau$ :

$$\tau = -k_r A_r (P_h(T, C_s) - P)$$

- $k_r$  is the kinetic rate constant:  $k_r = k_{r0} e^{-\frac{E_a}{RT}}$
- $A_r$  is the reaction surface:  $A_r = A_0 \Gamma_r$ 
  - $A_0$  is the pore surface area
  - $\Gamma_r$  is the active fraction of the pore surface area
    - $\Gamma_r = S_w S_g X_{H_2O}^w X_{CO_2}^g$  (hydrate formation)
    - $\Gamma_r = S_h$  (hydrate dissociation)
- $P_h(T, C_s)$  is the equilibrium pressure of hydrate
- $P_h(T, C_s) - P$  measures the deviation from equilibrium
  - if  $P_h(T, C_s) < P \Rightarrow \tau > 0$ : **Formation**
  - if  $P_h(T, C_s) > P \Rightarrow \tau < 0$ : **Dissociation**
  - if  $P_h(T, C_s) = P \Rightarrow \tau = 0$ : **Equilibrium**

$$R_{HYD} = -\tau, R_{CO_2} = \tau \text{ and } R_{H_2O} = n_h \tau$$

$P_h(T, C_s)$



# NON-ISOTHERMAL REACTIVE COMPOSITIONAL MULTIPHASE FLOW IN POROUS MEDIA

## ● Energy balance equation:

$$\frac{\partial}{\partial t} \left( \phi_f \sum_{\alpha \in \{w,g\}} S_\alpha \rho_\alpha u_\alpha + \phi_s \sum_{\beta \in \{r,h\}} S_\beta \rho_\beta u_\beta \right) + \text{div} \left( \sum_{\alpha \in \{w,g\}} \rho_\alpha h_\alpha \vec{v}_\alpha - \Lambda_E \vec{\nabla} T \right) + Q_E = 0$$

## ● Specific internal energy:

$$u_\alpha = h_\alpha - \frac{P}{\rho_\alpha} \quad \alpha \in \{w, g\} \quad u_\beta = h_\beta \quad \beta \in \{r, h\}$$

## ● Specific enthalpy:

● Simple linear law : 
$$h_\alpha(T, P) = h_{ref,\alpha} + C_{p,\alpha} \left( (T - T_{ref}) - \mu_{JT,\alpha} (P - P_{ref}) \right)$$

- $h_{\alpha,ref}$ ,  $T_{ref}$  and  $P_{ref}$  are the reference enthalpy, the reference temperature and the reference pressure.  $C_{\alpha,p}$  is the heat capacity factor and  $\mu_{JT,\alpha}$  is the Joule-Thomson coefficient.

● Equation of state (EOS) : 
$$h_\alpha(T, P, X) = h_{id,\alpha}(T, X) + h_{res,\alpha}(T, P, X)$$

- Ideal enthalpy: 
$$h_{id,\alpha}(T, X) = \sum_i X_i^\alpha h_{id}^i(T)$$

- Residual enthalpy (EOS): 
$$h_{res,\alpha}(T, P, X) = \sum_i X_i^\alpha h_{res}^i(T, P, X)$$

# JOULE-THOMSON EFFECT

## ● Joule-Thomson coefficient

$$\mu_{JT} = \frac{dT}{dP} = \frac{1}{C_p} \left( T \left( \frac{\partial V_g}{\partial T} \right)_P - V_g \right) = - \frac{1}{C_p \cdot \rho_g} \left( \frac{T}{\rho_g} \left( \frac{\partial \rho_g}{\partial T} \right)_P + 1 \right)$$

## ● Joule-Thomson effect

### ● For a gas expansion: $dP < 0$

● If  $\mu_{JT} > 0 \Rightarrow dT < 0$ : The gas expansion leads to a cooling.

● If  $\mu_{JT} < 0 \Rightarrow dT > 0$ : The gas expansion leads to a warming up.

### ● For a gas compression: $dP > 0$

● If  $\mu_{JT} > 0 \Rightarrow dT > 0$ : The gas compression leads to a warming up.

● If  $\mu_{JT} < 0 \Rightarrow dT < 0$ : The gas compression leads to a cooling.

## MATHEMATICAL FORMULATION: COATS FORMULATION

- The unknowns are:

$$P, T, S_w, S_g, S_h, S_r, \phi_f, \phi_s, X_{H_2O}^w, X_{CO_2}^g, X_{CH_4}^g, X_{ROc}^r, X_{HYD}^h.$$

- The equations are discretized with a fully implicit two-point flux finite volume scheme.
- The resulting nonlinear system is solved using the Newton method.
- The size of the system is reduced by pre-eliminating all local equations.
- The set of unknowns is subdivided into a set of primary and secondary unknowns whose definition depends on the local context (variable switching).
- The context is defined at each Newton iteration by using a flash calculation to predict the appearance of a phase and by using the sign of the saturations to predict the disappearance of a phase.

# NUMERICAL SIMULATION



# INJECTION OF $CO_2$ IN A GAS ( $CH_4$ ) DEPLETED RESERVOIR

- 1D radial geometry

- Radial mesh ( $\Delta r, \Delta\theta$ ):

$0,002m < \Delta r < 48m, \Delta\theta = 5^\circ, N_{cells} = 100$

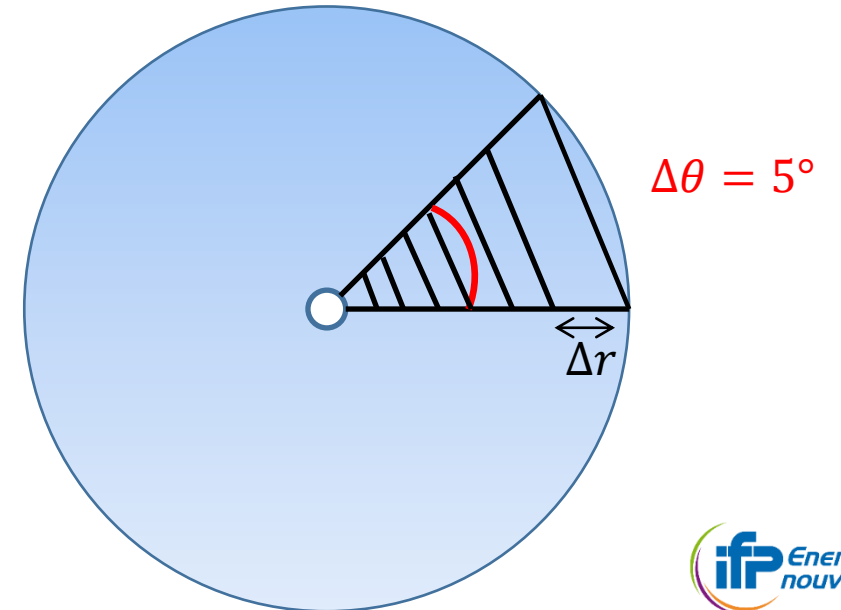
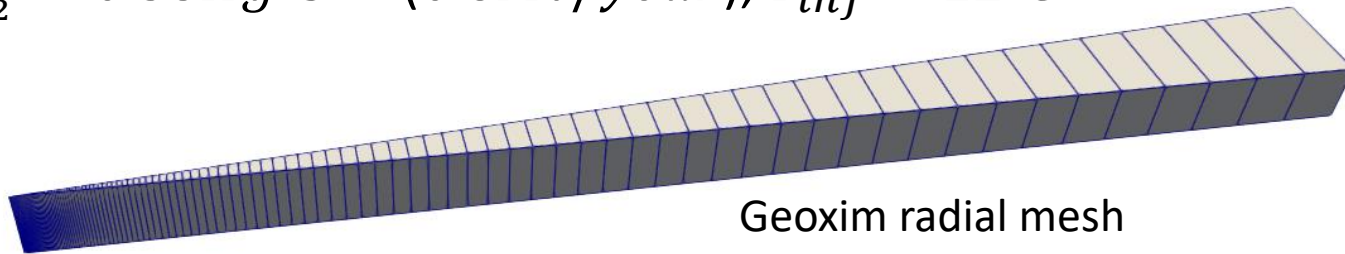
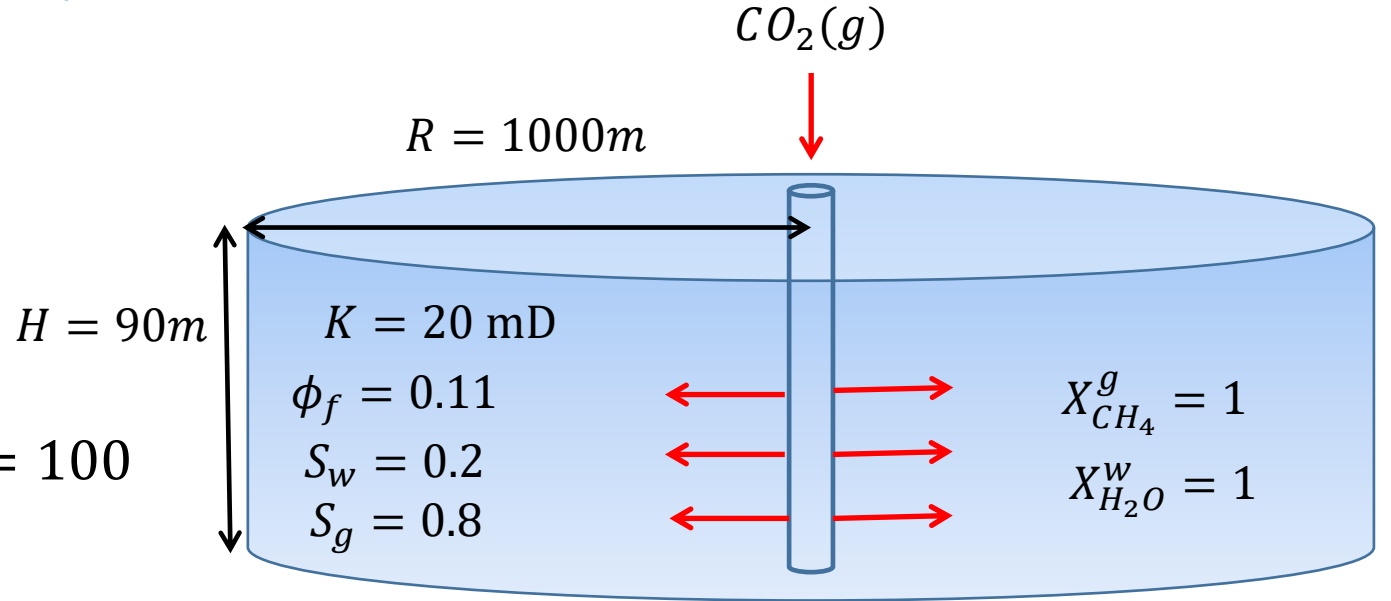
- Using EOS for fluid properties

- Initial conditions:

$P_{res} = 20bar, T_{res} = 105^\circ C, C_s = (0 g/l, 30 g/l)$

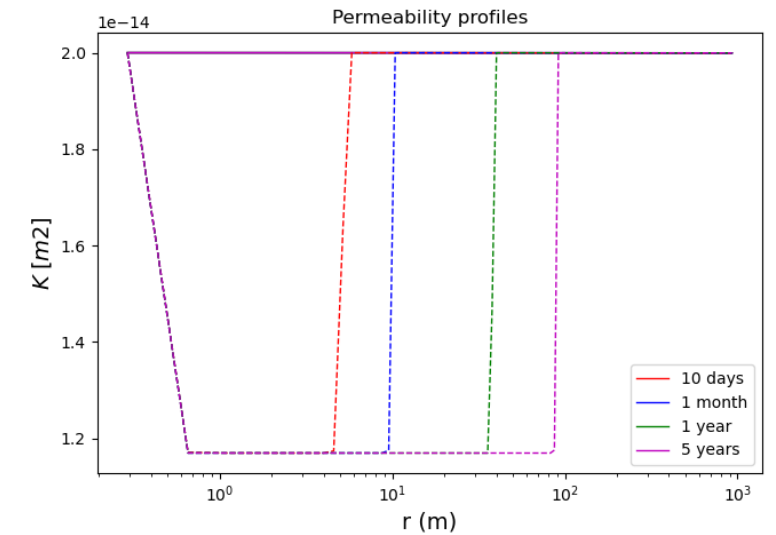
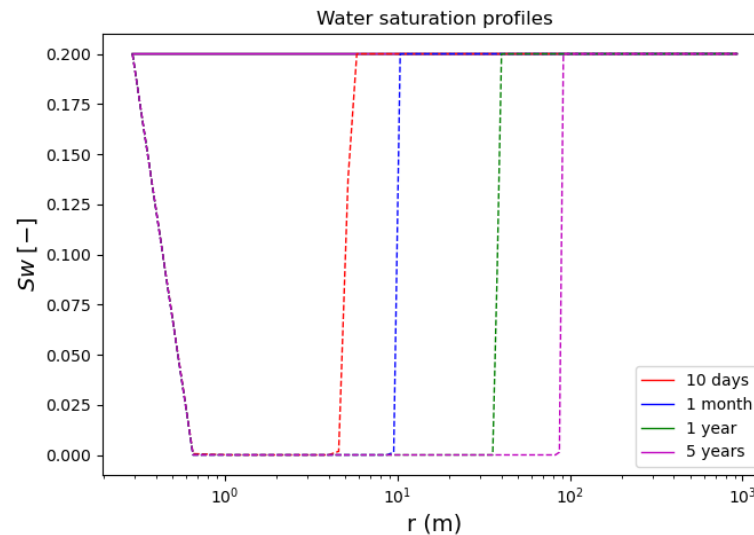
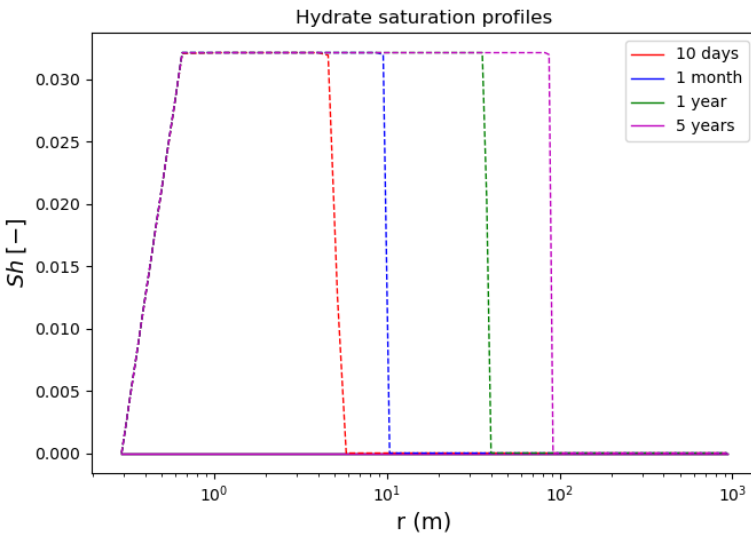
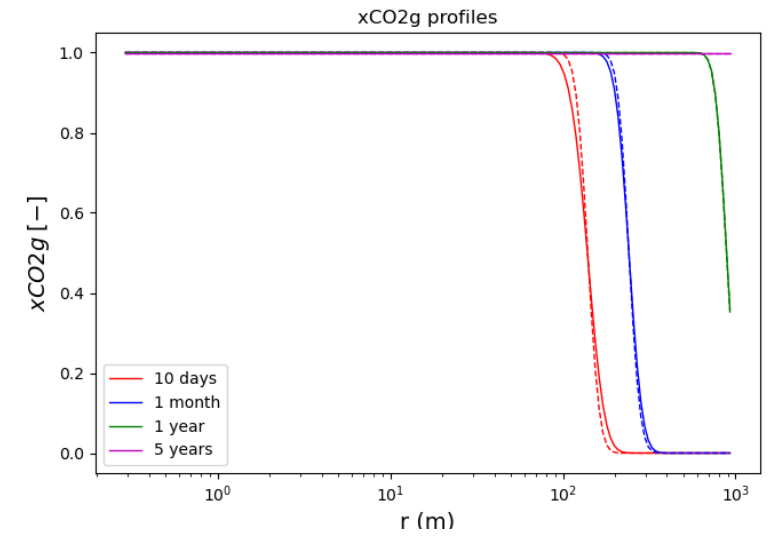
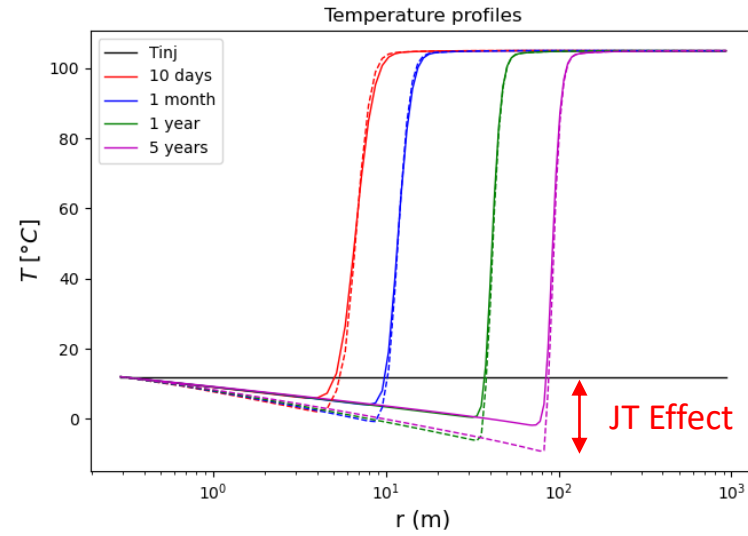
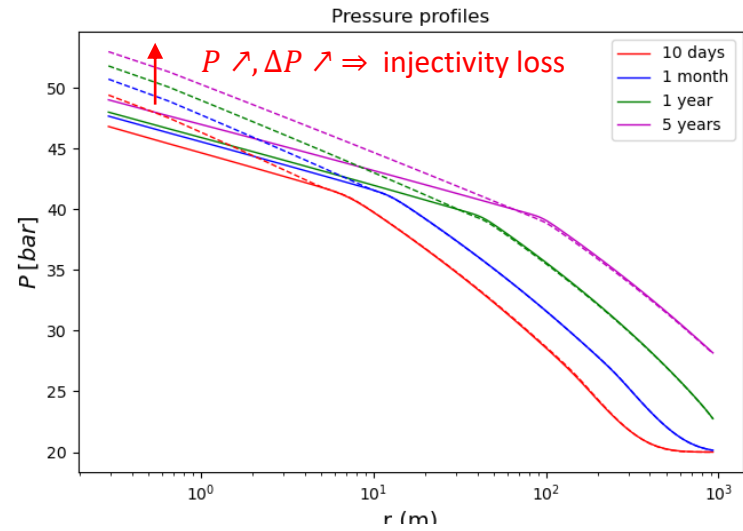
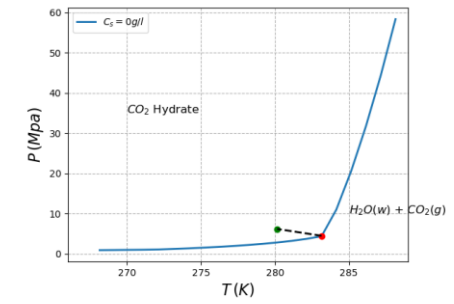
- Injection conditions for 5 years:

$Q_{CO_2} = 0.35Kg.s^{-1} (0.8Mt/year), T_{inj} = 12^\circ C$



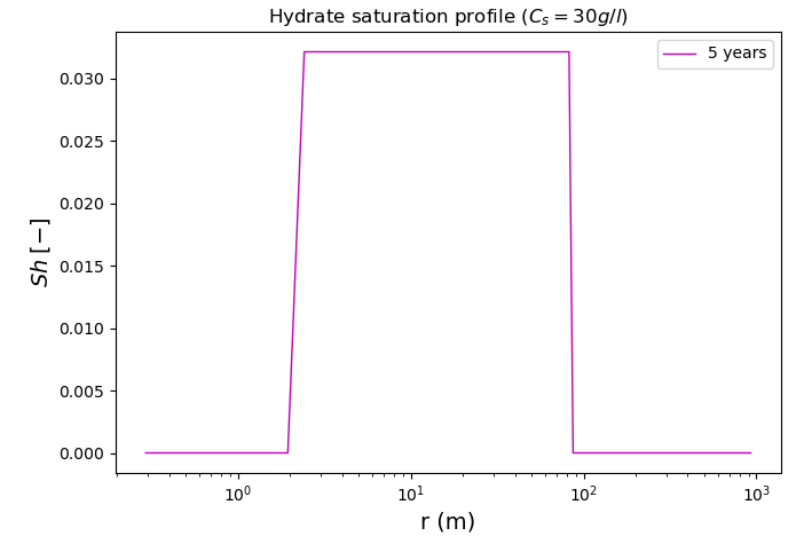
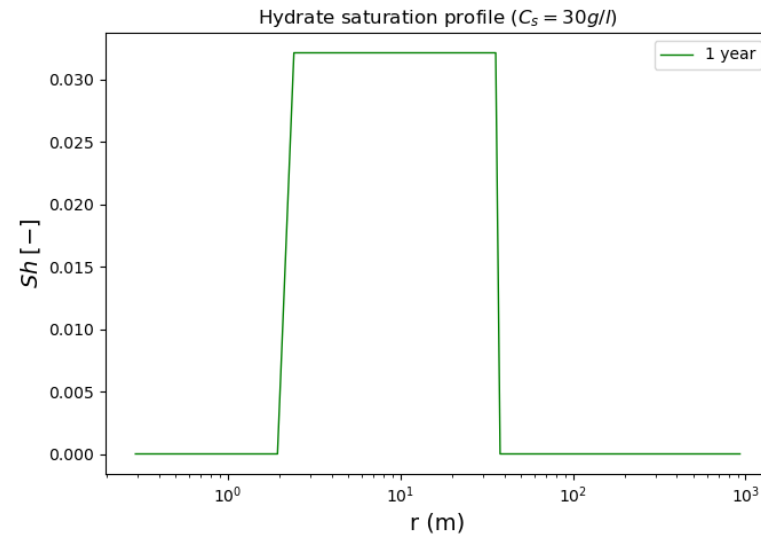
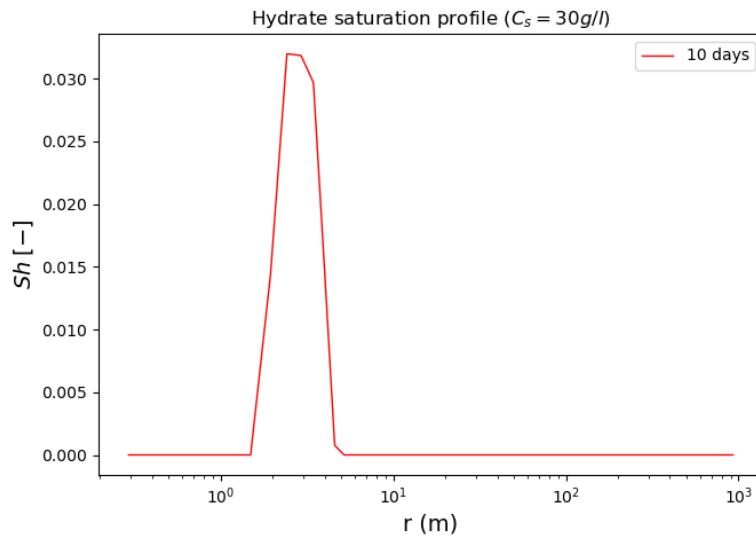
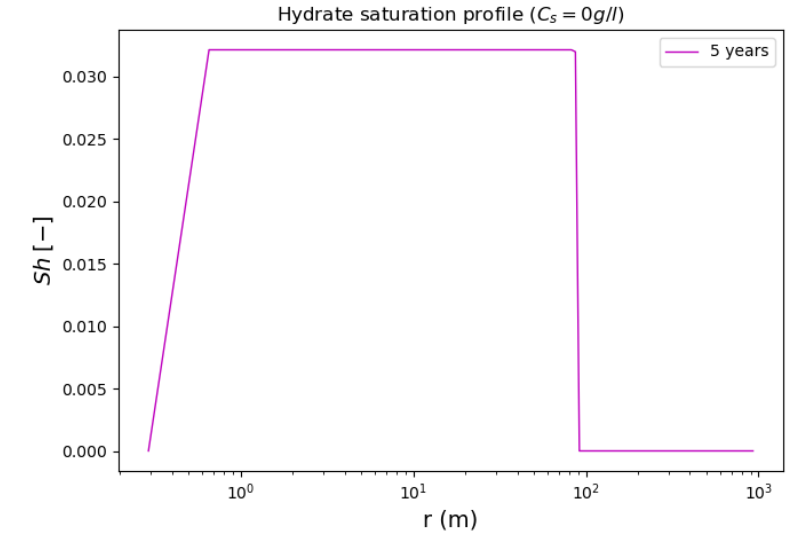
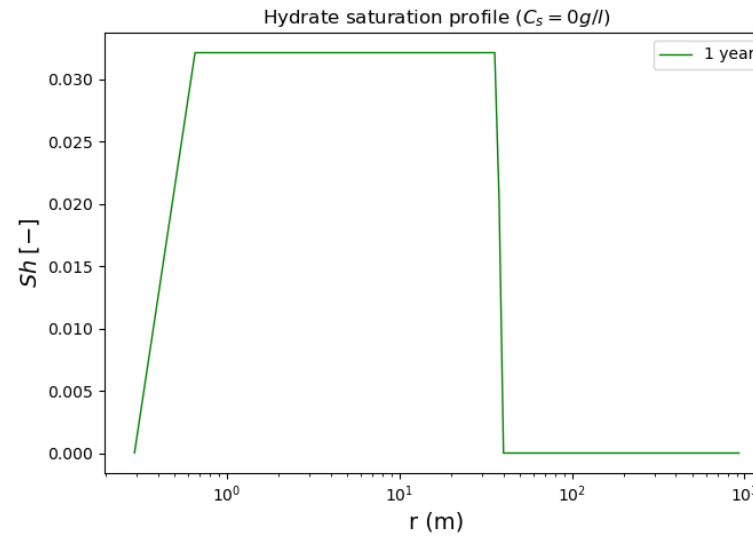
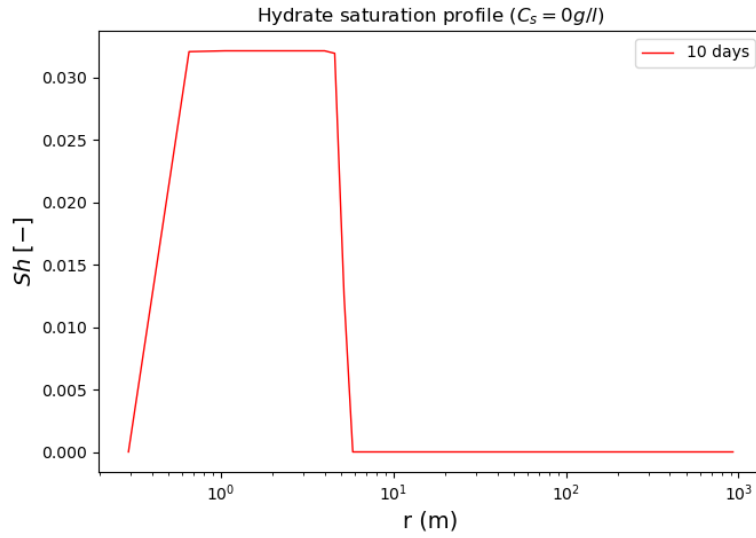
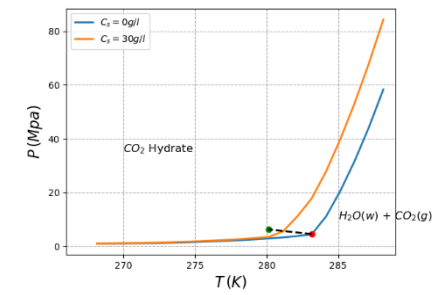
# NUMERICAL RESULTS WITHOUT SALINITY ( $C_s = 0 \text{ g/l}$ )

— (without hydrate formation)      - - - - (with hydrate formation)



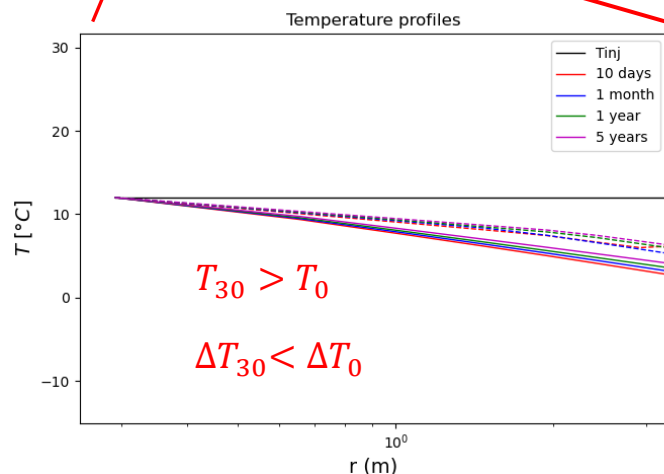
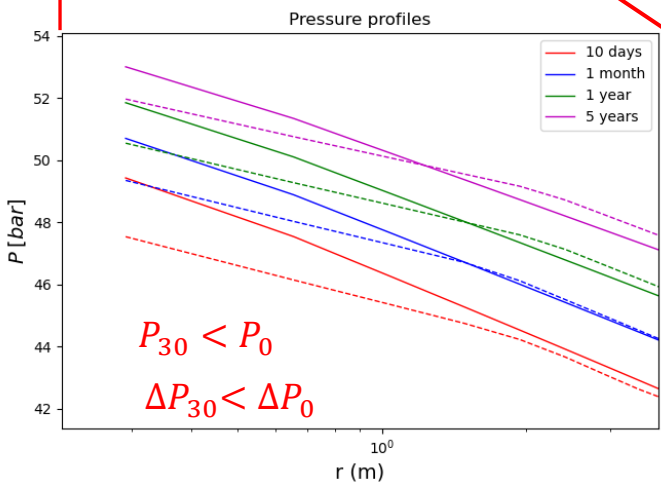
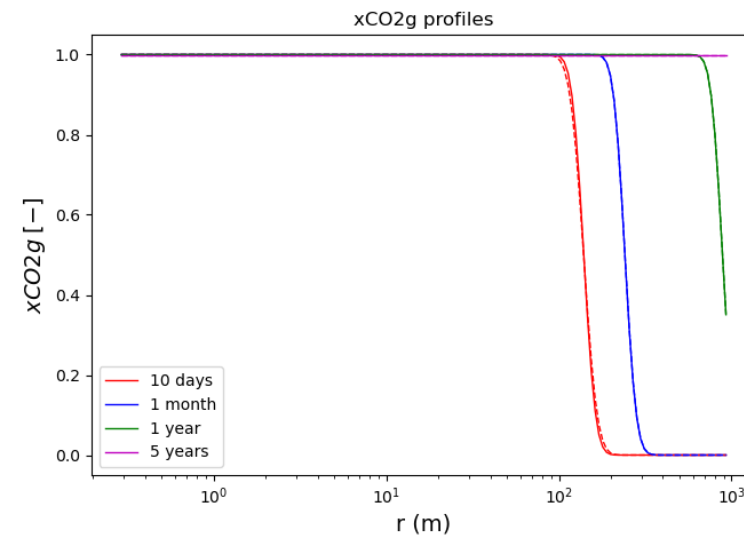
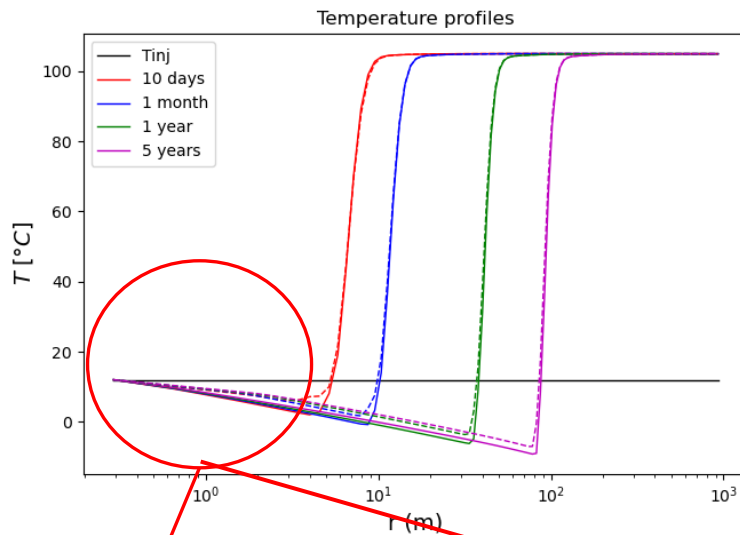
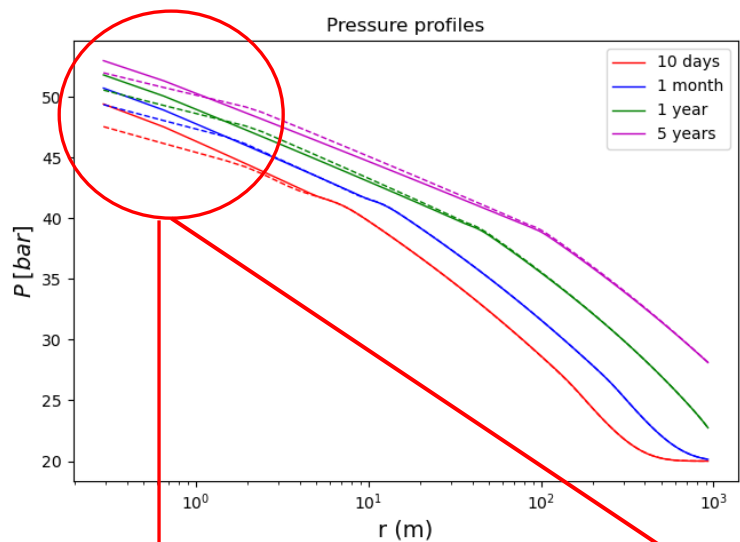
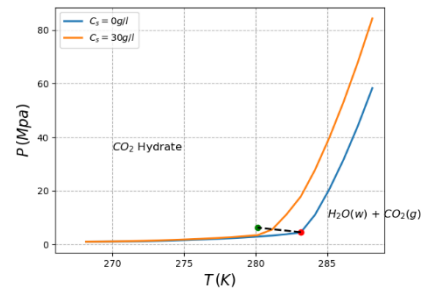


# NUMERICAL RESULTS WITH SALINITY ( $C_s = 30 \text{ g/l}$ )



# NUMERICAL RESULTS WITH SALINITY ( $C_s = 30 \text{ g/l}$ )

— ( $C_s = 0 \text{ g/l}$ )    - - - - ( $C_s = 30 \text{ g/l}$ )



## NUMERICAL RESULTS - CONCLUSION

- These numerical simulations of  $CO_2$  injection into a depleted reservoir have verified that:
  - EOS can well reproduce the Joule-Thomson cooling effect close to the well
  - JT cooling effect  $\Rightarrow CO_2$  hydrate formation
  - $CO_2$  hydrate formation  $\Rightarrow$  decrease in porosity and permeability  $\Rightarrow$  loss of injectivity
  - But increasing salinity reduces the formation of hydrates
- Future works:
  - Porosity and permeability sensitivity analysis
  - Tacking into account the dissolution of  $CO_2$  and  $CH_4$  in water and water vaporization
  - ...

# INJECTION OF $CO_2$ IN DEEP OCEAN SEDIMENTS

- Injection of  $CO_2$  in deep ocean sediments

- 2D radial geometry (R,Z)

- Regular radial mesh ( $\Delta r, \Delta z$ ):

$$N_r = 50, N_z = 100$$

$$\Delta r = 20m, \Delta z = 4m$$

- Dissolution of  $CO_2$  in water

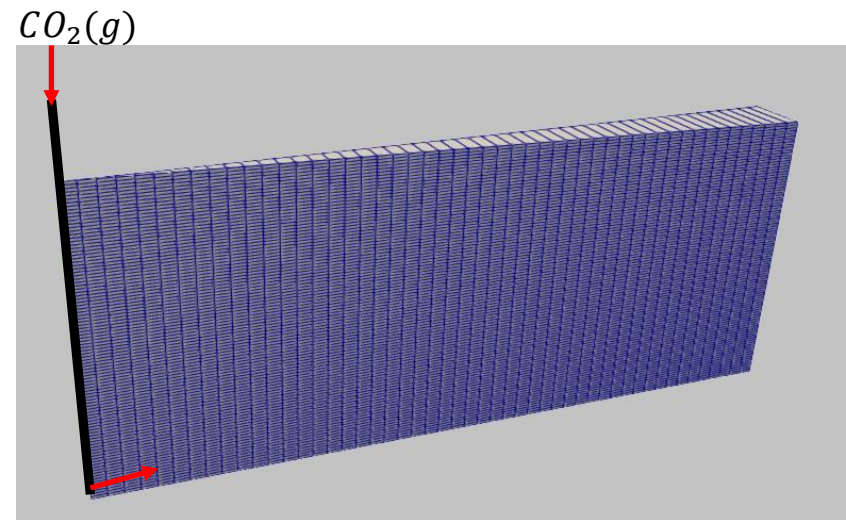
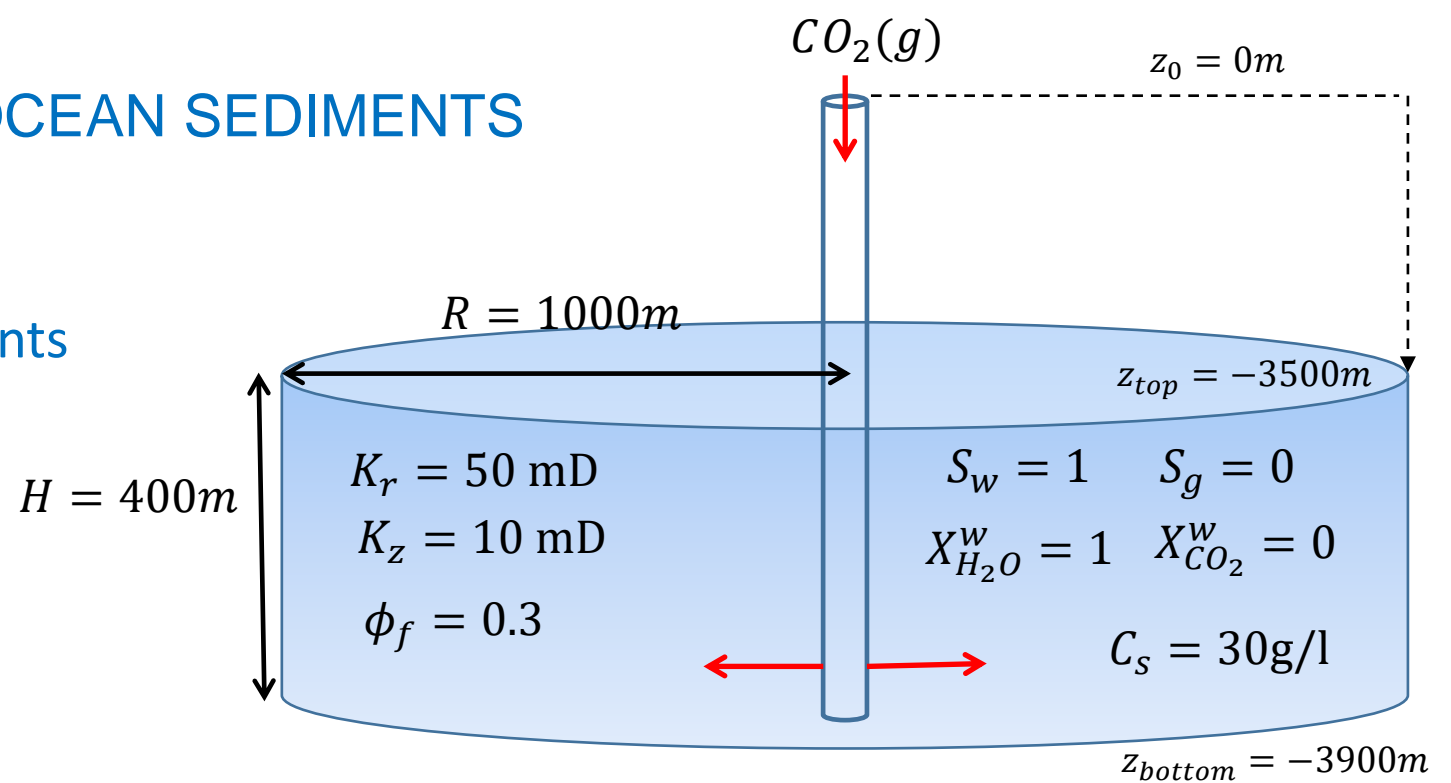
- Initial hydrostatic conditions:

$$P_{top} = 380bar, T_{top} = 3^\circ C$$

$$P_{bottom} = 420bar, T_{bottom} = 15^\circ C$$

- Injection conditions:

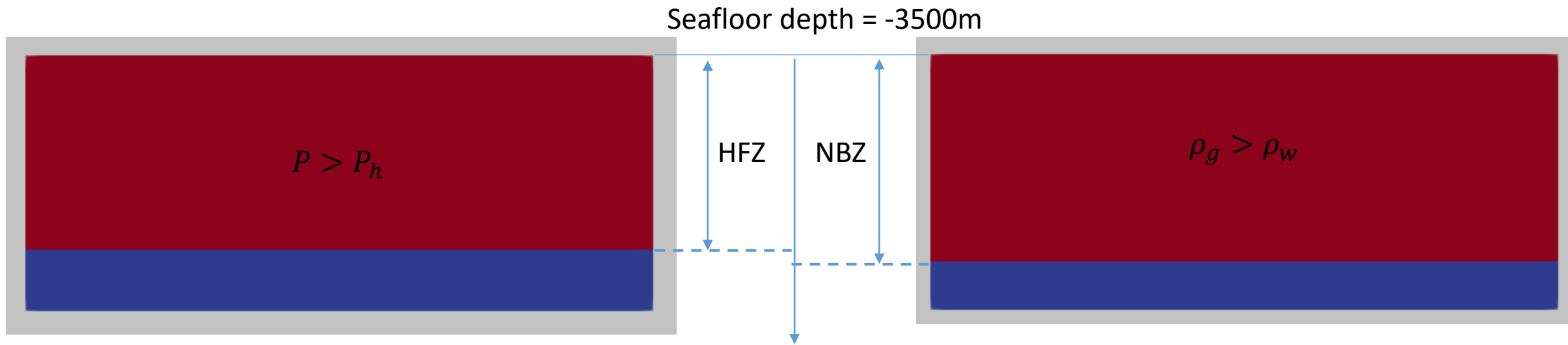
$$Q_{CO_2} = 0.44Kg.s^{-1} (1 Mt/year), T_{inj} = 14^\circ C$$



Geoxim 2D radial mesh

## NUMERICAL RESULTS WITH $Z_{top} = -3500m$

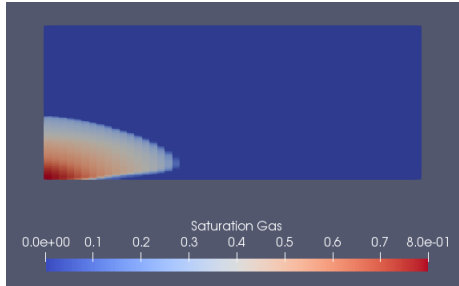
- Initial Hydrate Formation Zone (HFZ) and initial Negative Buoyancy Zone (NBZ)



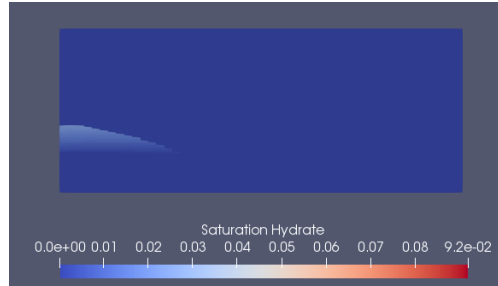
# NUMERICAL RESULTS WITH $Z_{top} = -3500m$

$T = 5 \text{ years}$

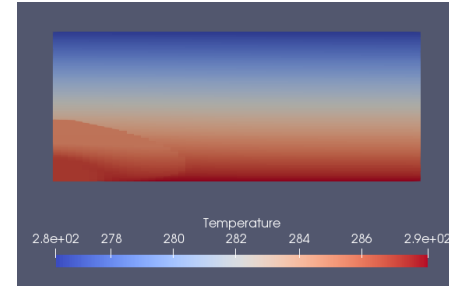
$S_g$



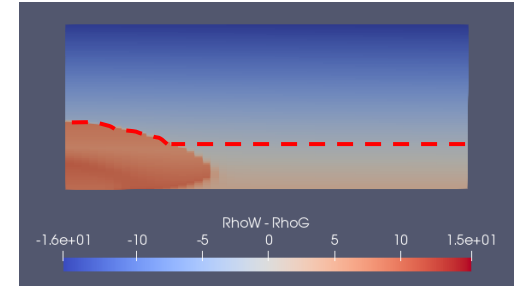
$S_h$



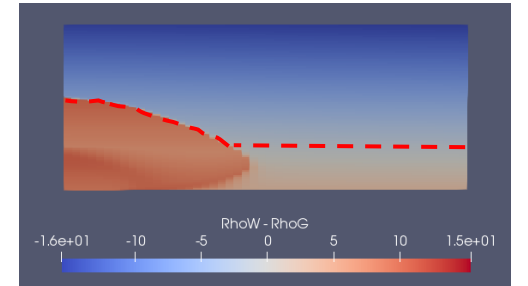
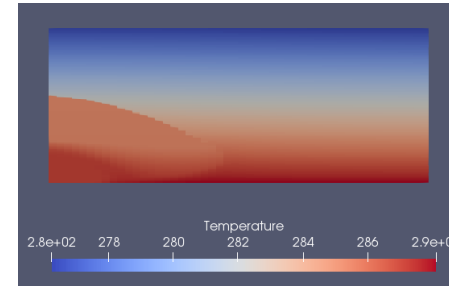
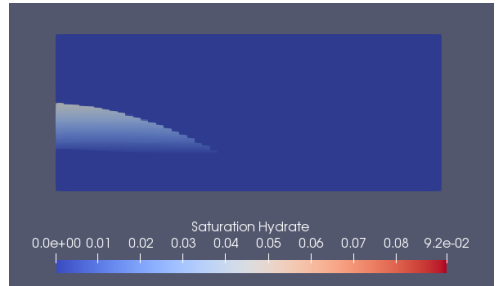
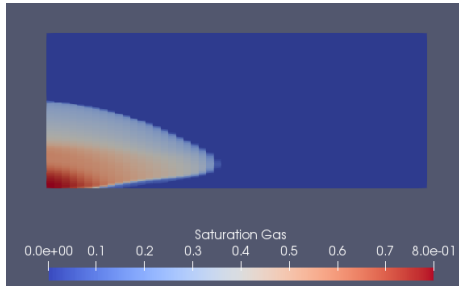
$T$



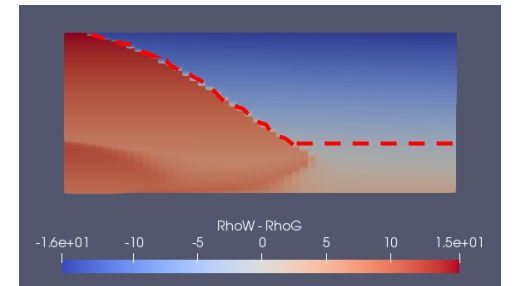
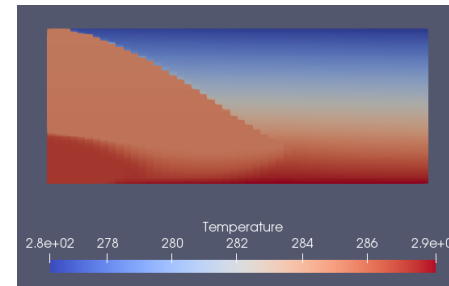
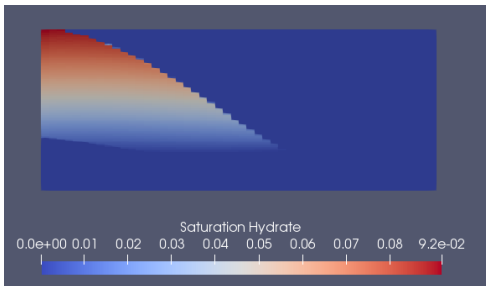
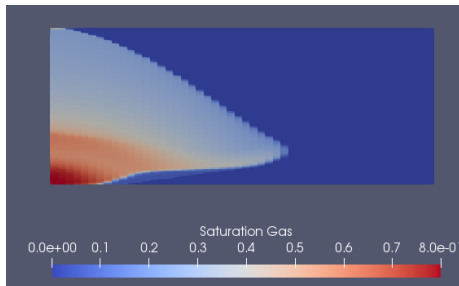
$\rho_w - \rho_g$



$T = 10 \text{ years}$

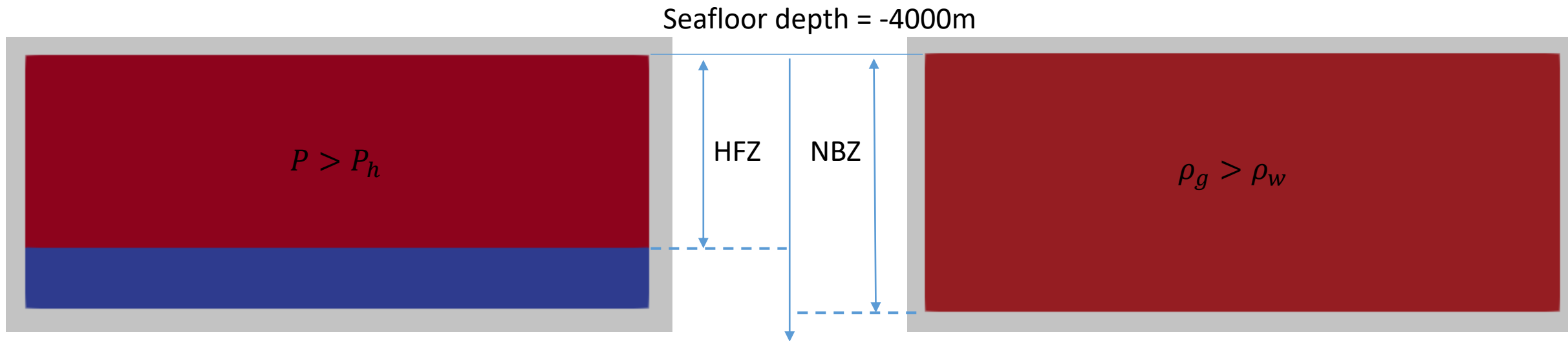


$T = 25 \text{ years}$

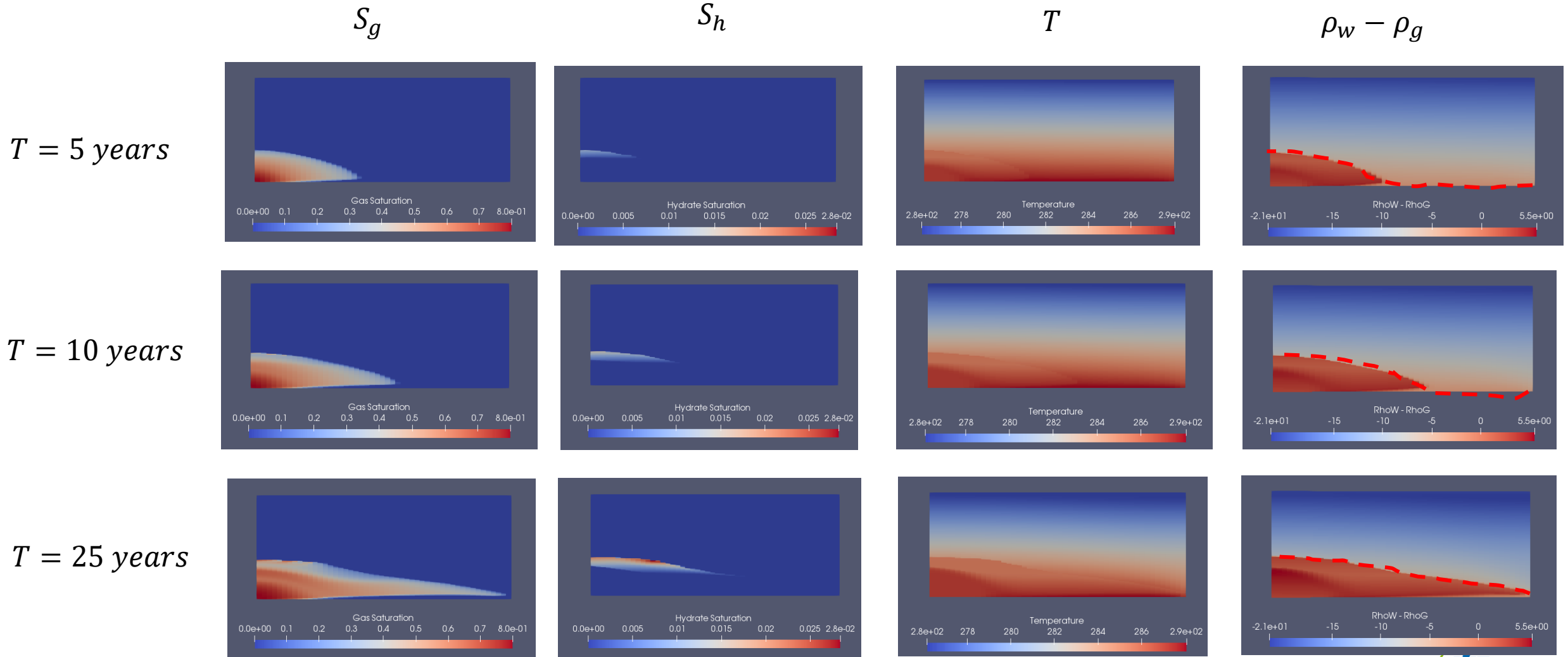


## NUMERICAL RESULTS WITH $Z_{top} = -4000m$

- Initial Hydrate Formation Zone (HFZ) and initial Negative Buoyancy Zone (NBZ)



# NUMERICAL RESULTS WITH $Z_{top} = -4000m$





## NUMERICAL RESULTS - CONCLUSION

- Storing  $CO_2$  in deep ocean sediments is not safe:
  - An amount of  $CO_2$  leaks out of the sediments.
  - The amount of hydrate formation is too small to block the  $CO_2$  plume.
  - The Negative Buoyancy zone decreases due to rising temperatures and dissolution of  $CO_2$  in water.
- Permanent  $CO_2$  storage can exist in super deep ocean high permeability sediments which may bring high costs.

THANK YOU FOR YOUR ATTENTION



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