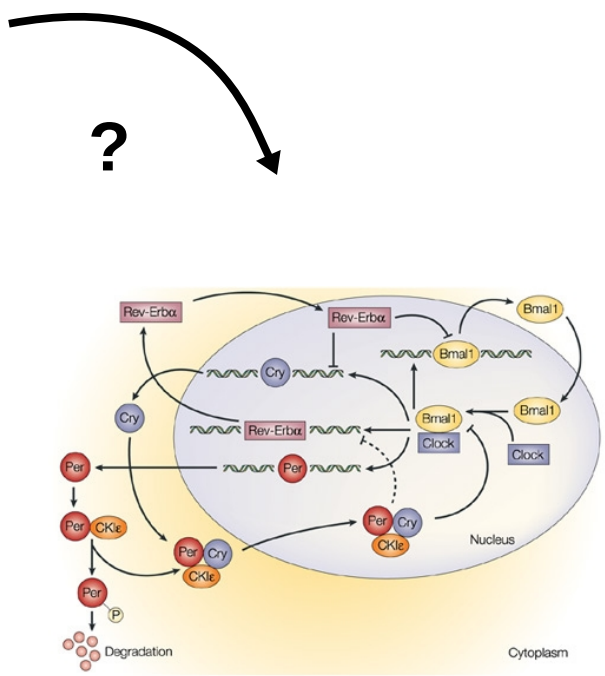
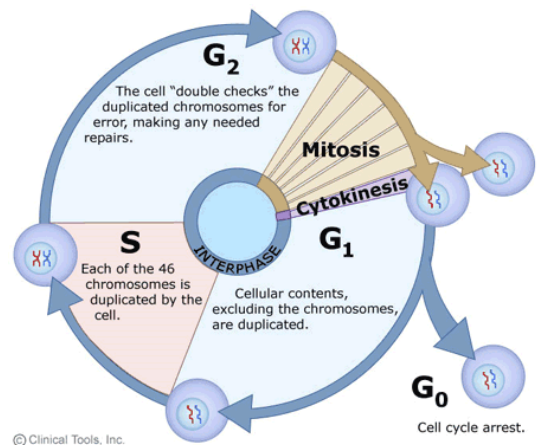
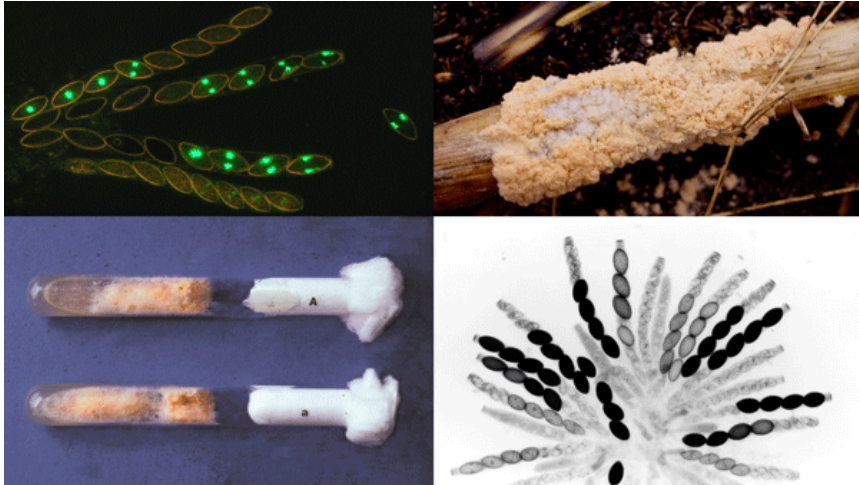


# L'horloge circadienne, le cycle cellulaire et leurs interactions



Madalena CHAVES

# What do all these living organisms have in common?



*Neurospora crassa*



*Mus musculus*



*Arabidopsis thaliana*



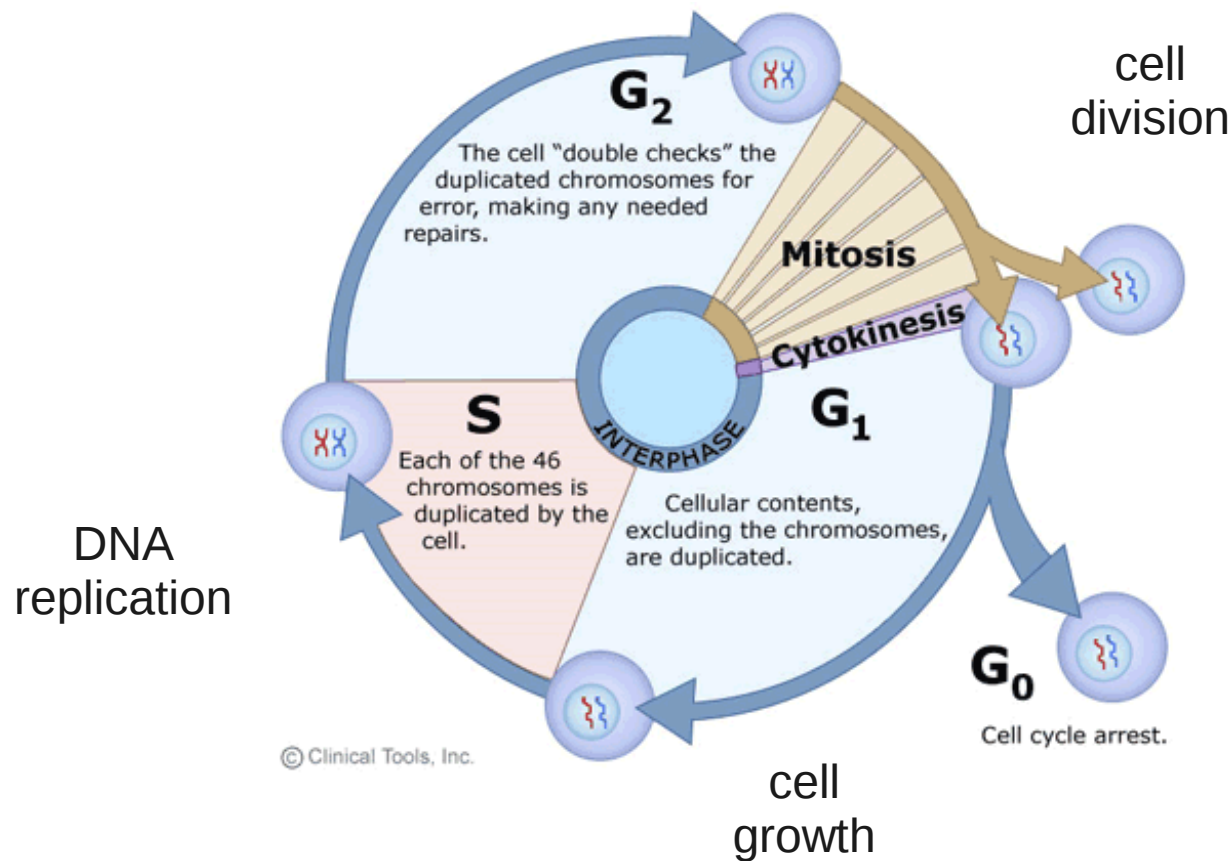
*Drosophila melanogaster*



*Synechococcus elongatus*  
Cyanobacteria in Baltic sea

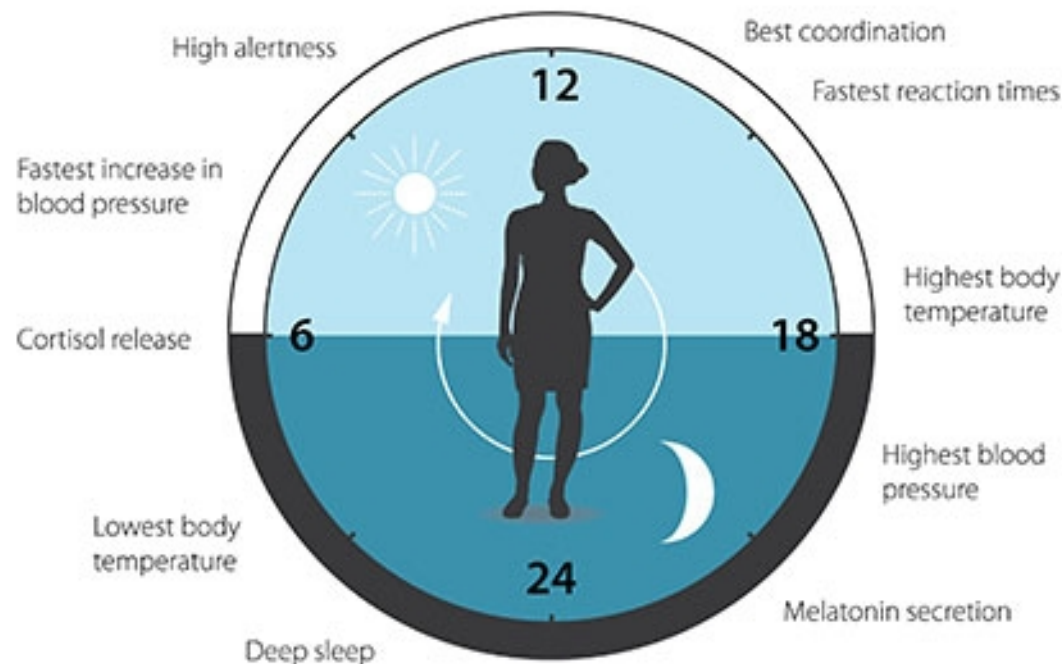
# Cell cycle

- Cell cycle is the process by which cells growth and divide



# Circadian rhythms

- Anticipate environment cycles (day/night) and prepare living organism for upcoming events (eg., expressing required genes)
- Generate an **AUTONOMOUS molecular clock**: cycle goes on independently of other cellular processes
- Temperature compensation: cycle always adjusts to 24h



## Cortisol

Lipid degradation,  
Glucose production  
(energy)

## Melatonin

To promote sleep

# 2017 Nobel Prize

- J. Hall and M. Rosbash (1984) first to identify gene “period”, responsible for circadian rhythm in drosophila
- Hypothesis: protein PER contributes to **eventually repress its own gene**, thus creating a negative feedback loop



Drosophila Melanogaster  
→ mouche du vinaigre

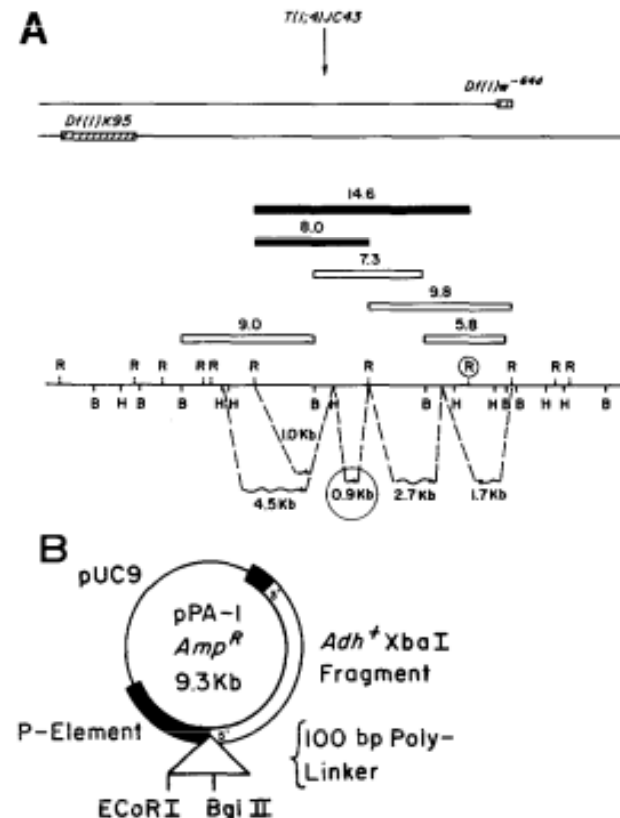
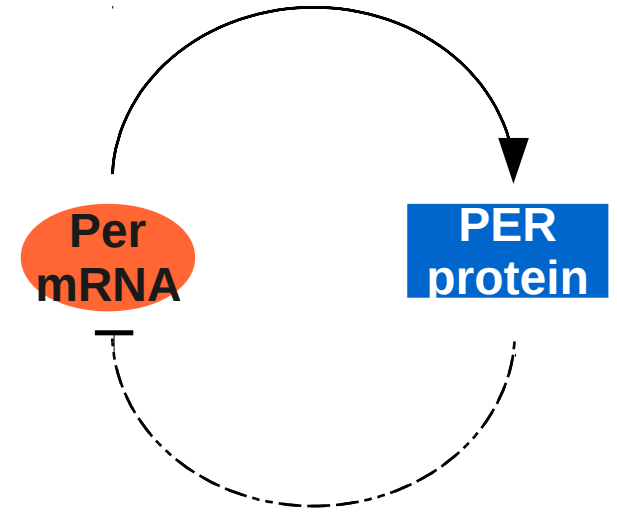
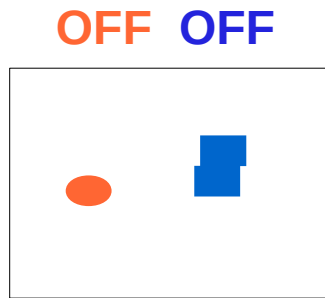
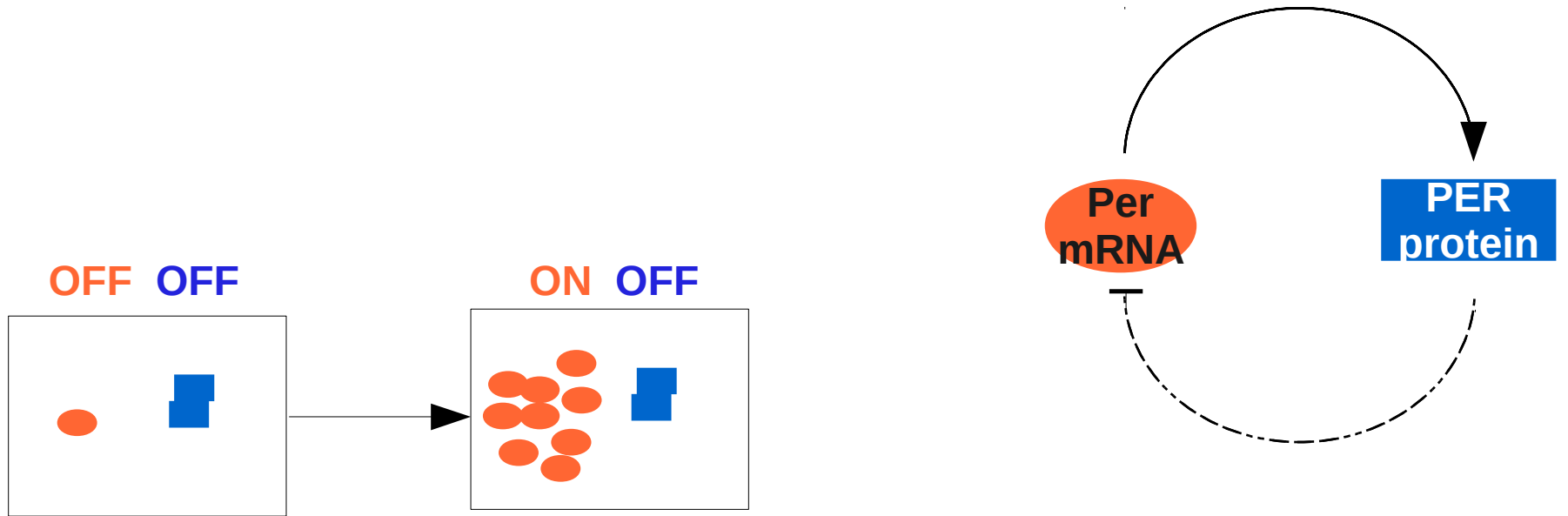


Figure 1. Molecular Map of Subclones in the *per* Region Used in Transformation, with Reference to Chromosomal Breakpoints and Transcripts from

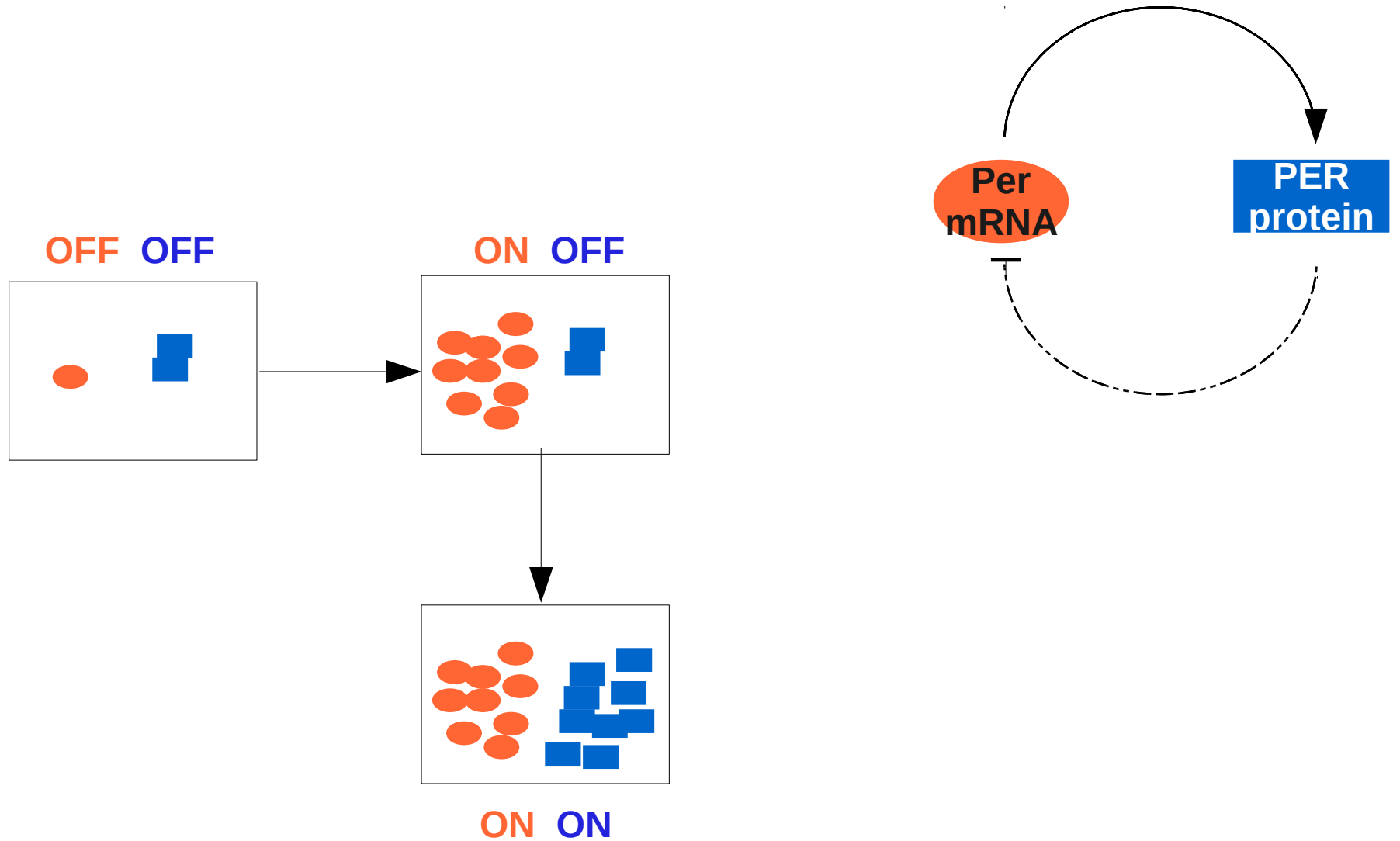
# Negative feedback loop



# Negative feedback loop

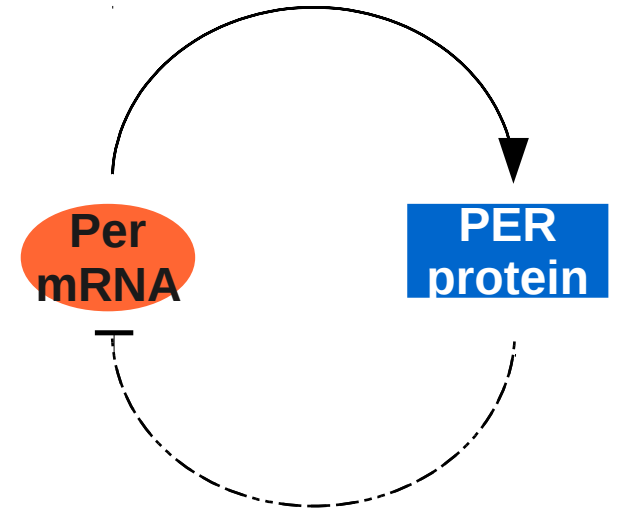
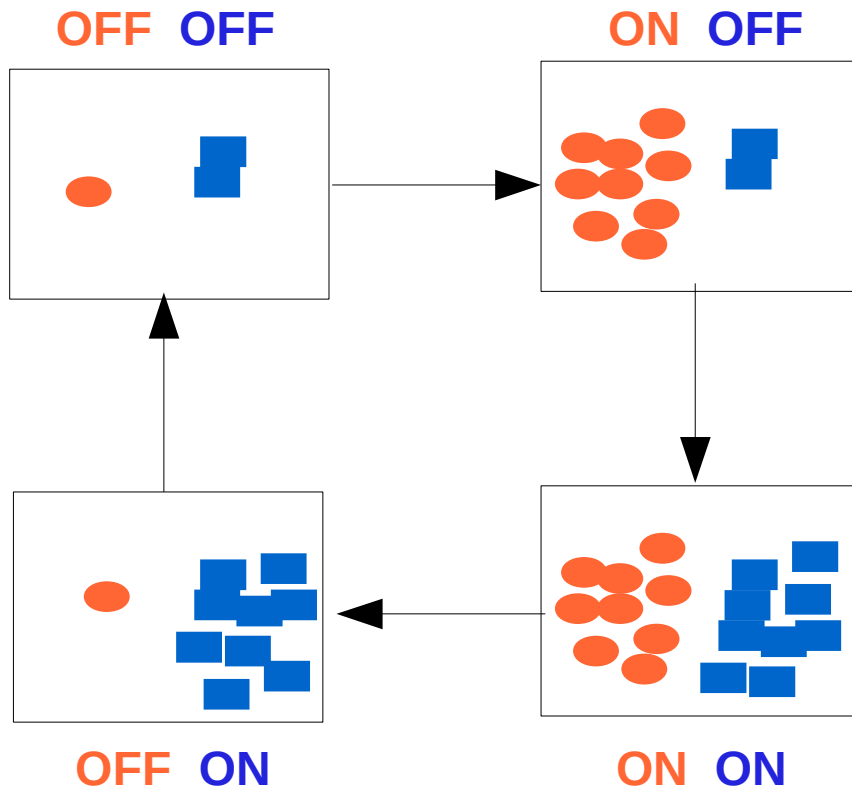


# Negative feedback loop



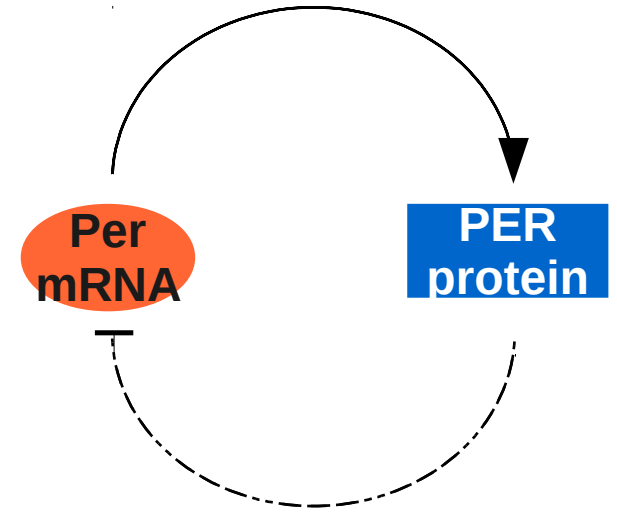
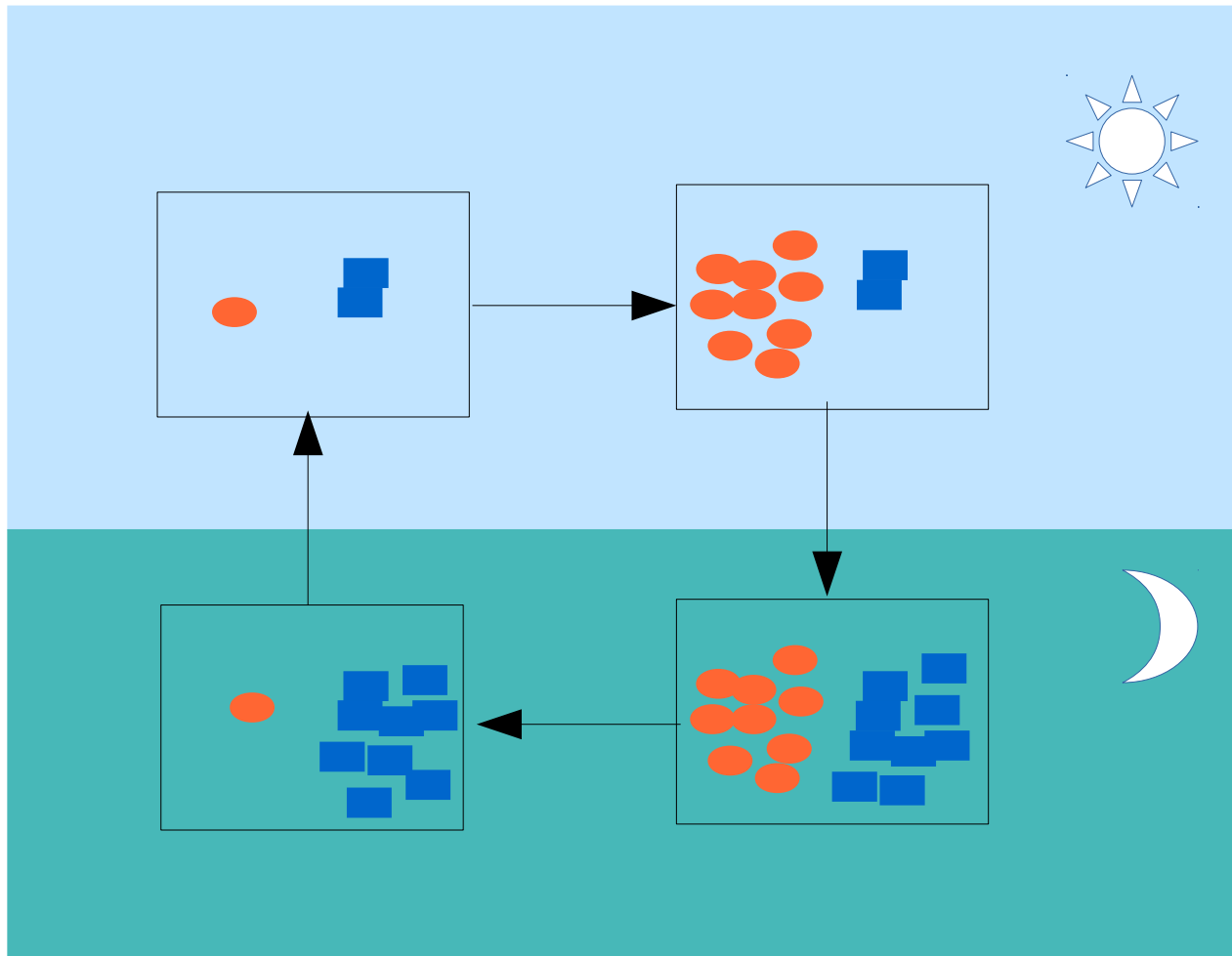


# Negative feedback loop



Generates an  
**oscillatory  
Cycle !**

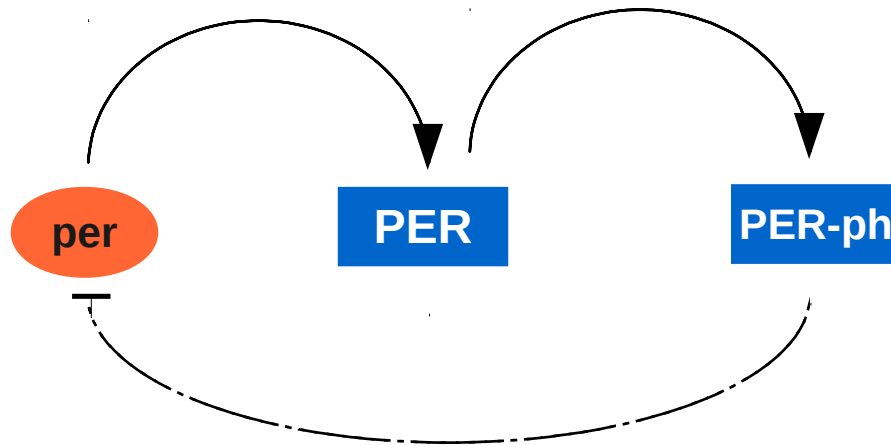
# Negative feedback loop



PER protein  
accumulates  
during  
the night

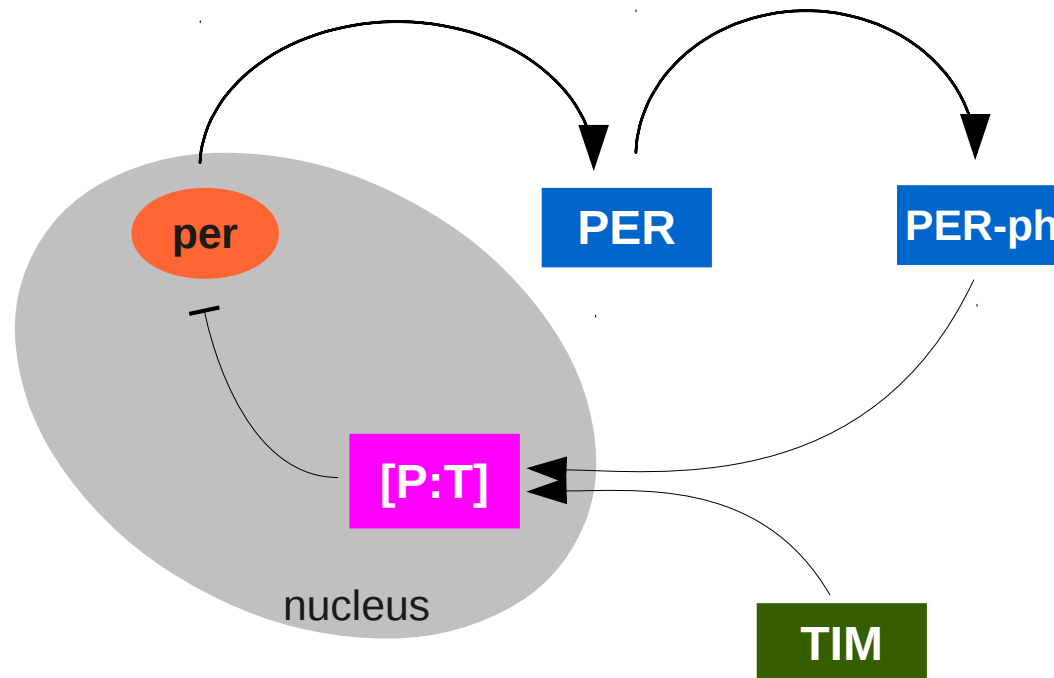
# A basic negative feedback loop is not enough

- How to guarantee that oscillations are sustained ?  
→ increase the number of steps:



# A basic negative feedback loop is not enough

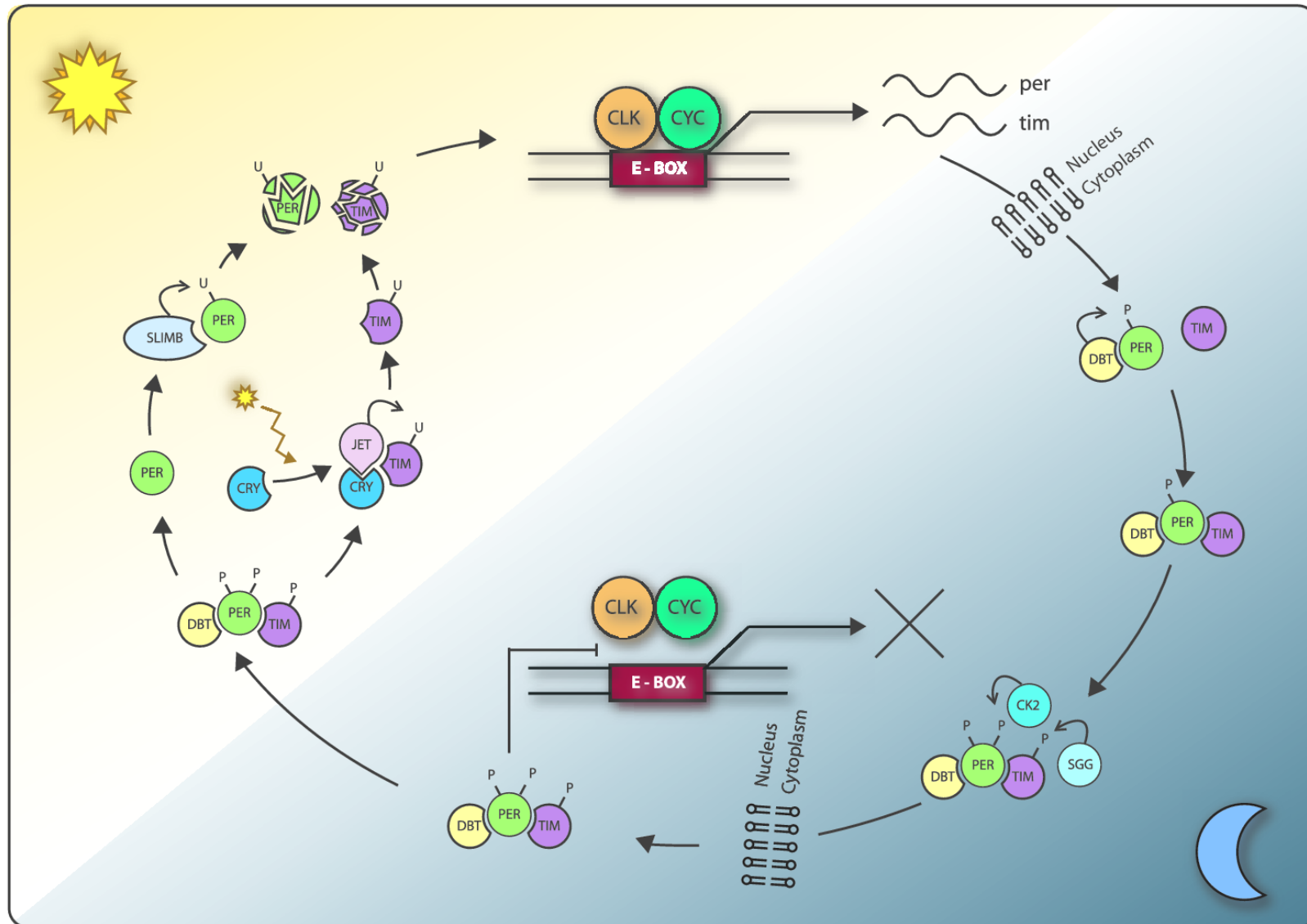
- How to guarantee that oscillations are sustained ?  
→ increase the number of steps:
- How to generate a **24 hour cycle** ?



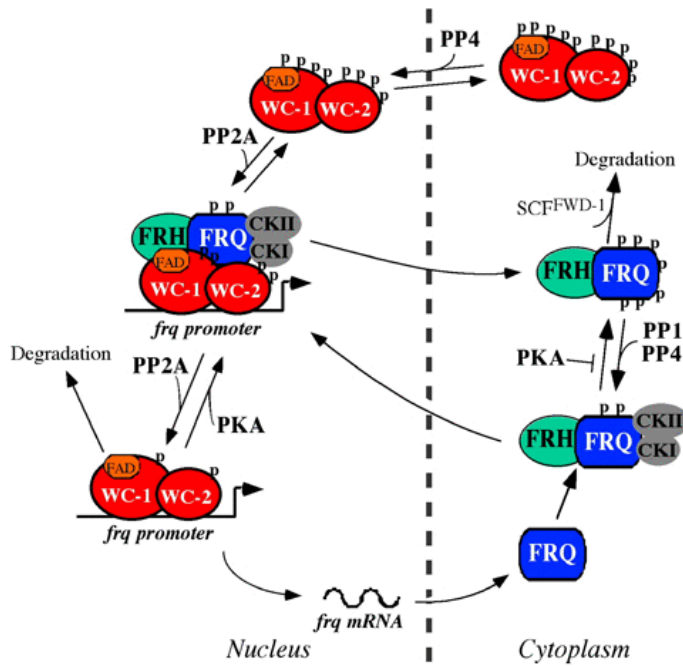
Other proteins are involved that impose “waiting” times

“timeless” (TIM) and “doubletime”, discovered by M. Young 1994, 98

# Circadian clock in Drosophila

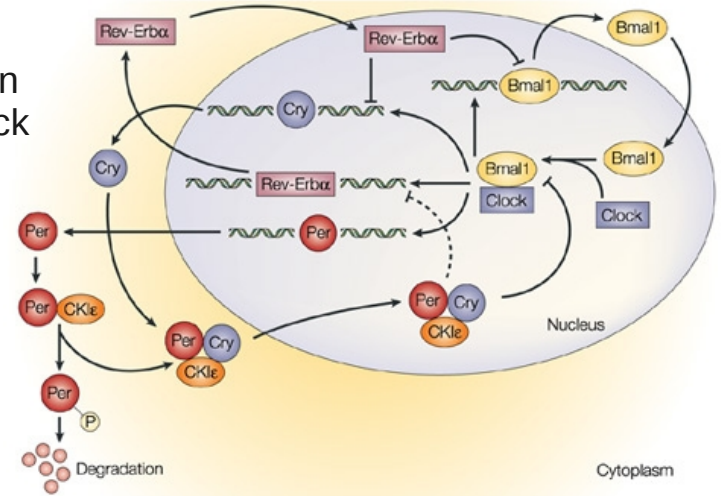


# Similar clock mechanisms across organisms



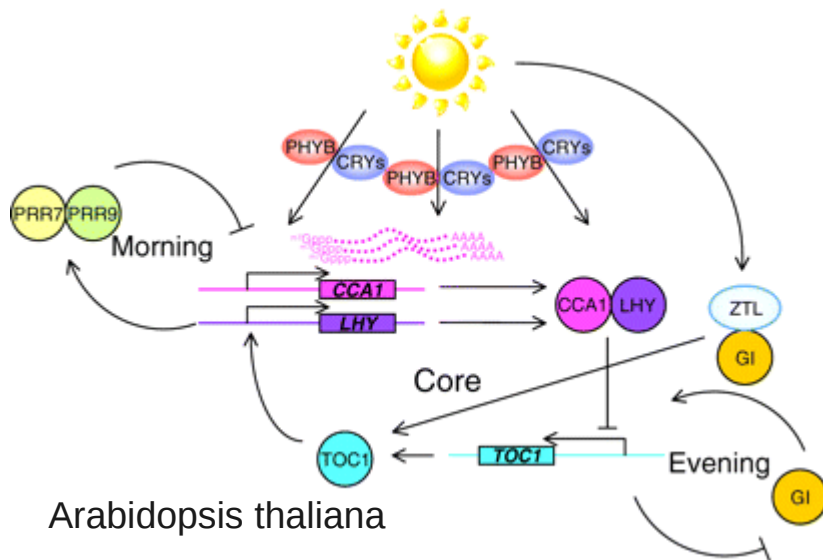
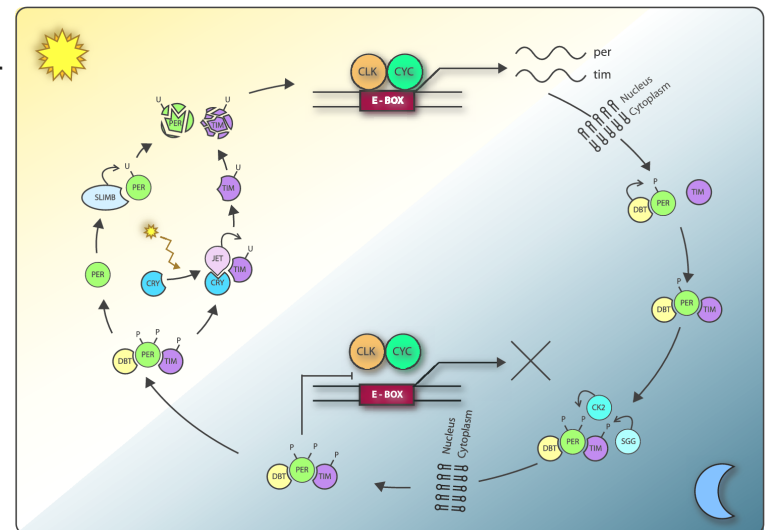
*Neurospora crassa*

Mammalian clock

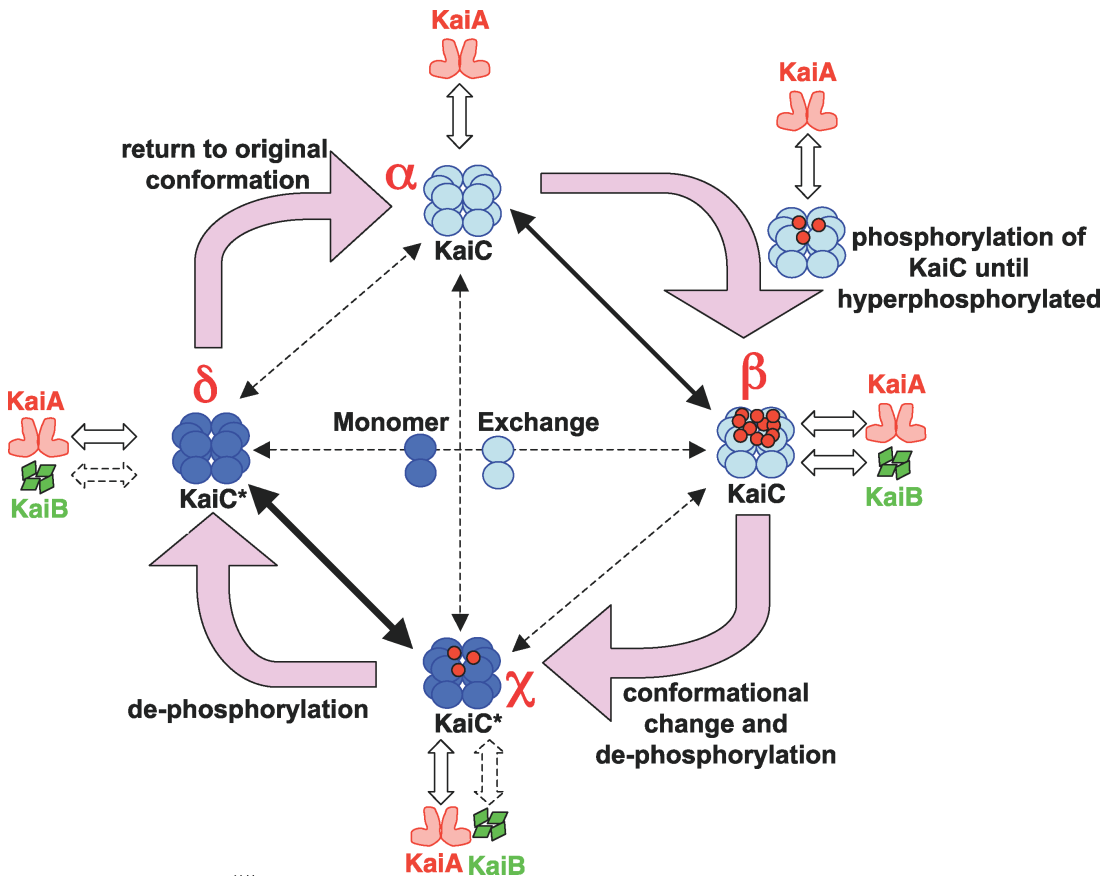


Nature Reviews | Cancer

*Drosophila melanogaster*

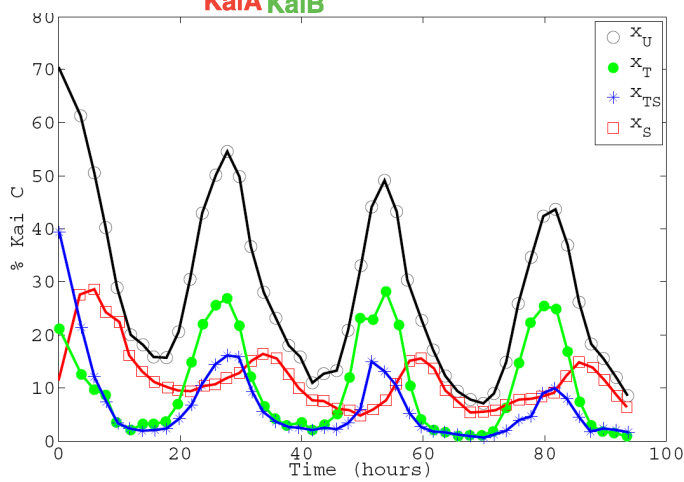


# Autonomous clock: cyanobacteria



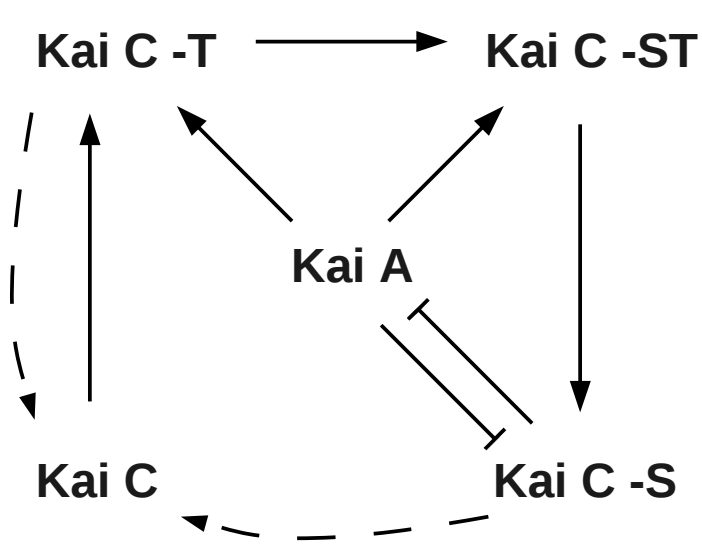
“In vitro” system:  
only proteins in a test tube;  
no genes, no transcription  
or translation involved !

Oscillations are due to an  
ordered cycle of phosphorylations  
and dephosphorylations  
of a protein, Kai C



Kondo lab, 2005-2007,  
Rust et al. 2007

# Modeling cyanobacteria clock



$$\dot{x}_A = k_A h^-(x_S, \theta_S) - \gamma_A x_A$$

$$\dot{x}_T = k_T h^+(x_U, \theta_U) h^+(x_A, \theta_A) - \gamma_T x_T$$

$$\dot{x}_{TS} = k_{TS} h^+(x_T, \theta_T) h^+(x_A, \theta_A) - \gamma_{TS} x_{TS}$$

$$\dot{x}_S = k_S h^+(x_{TS}, \theta_{TS}) h^-(x_A, \theta_{A2}) - \gamma_S x_S$$

$$x_U = x_{total} - x_T - x_{TS} - x_S$$

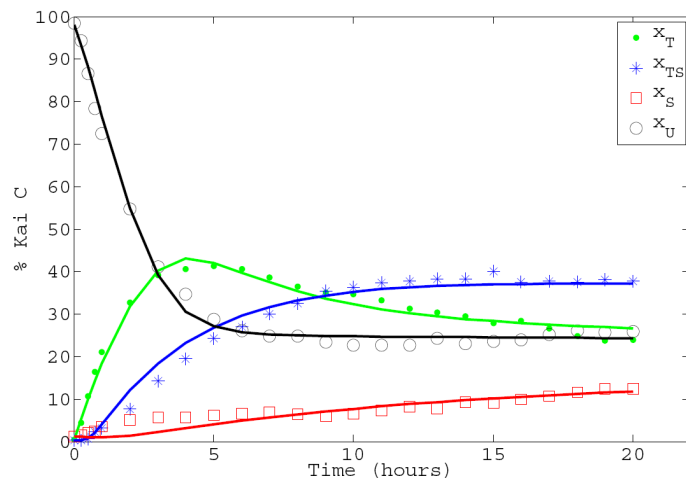
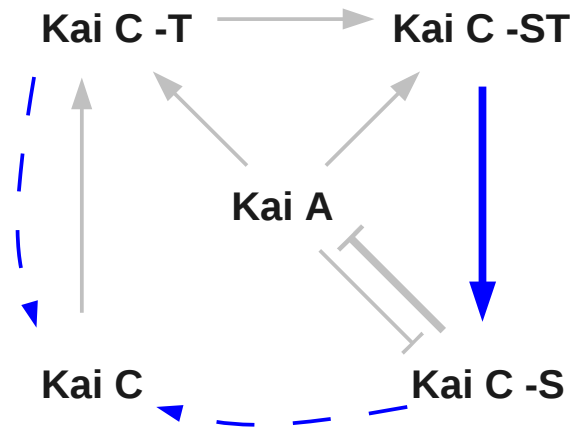
Need to **calibrate model** that is find the values of parameters:

$$k_A, k_T, k_{TS}, k_S, \gamma_A, \gamma_T, \gamma_{TS}, \gamma_S, \dots$$

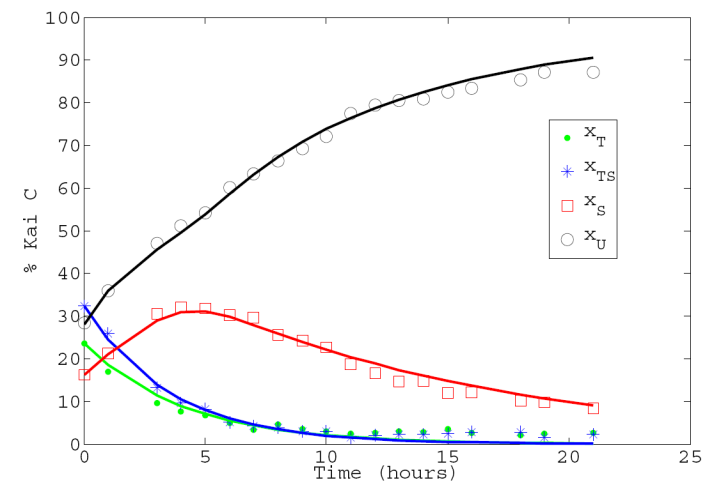
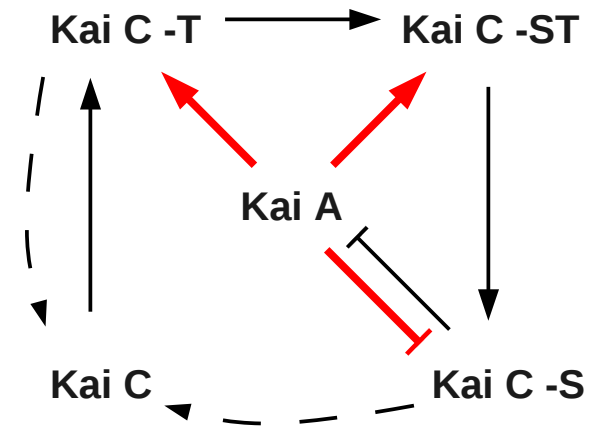


# Model calibration

## Experiment 1 Dephosphorylation



## Experiment 2 Phosphorylation

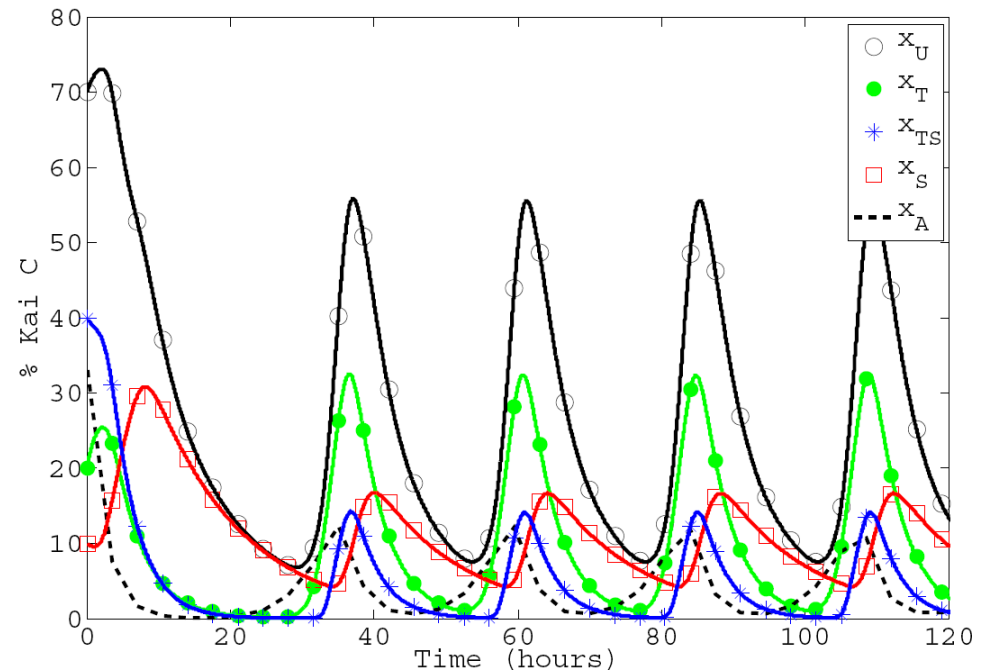
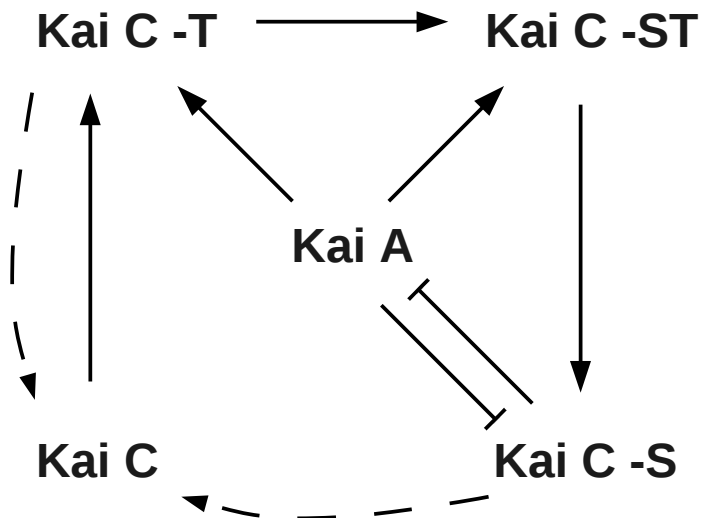


Data sets: Rust et al, Science 2007

# Model validation

Values of parameters were obtained from **two distinct sets of experiments, each for a “partial” model.**

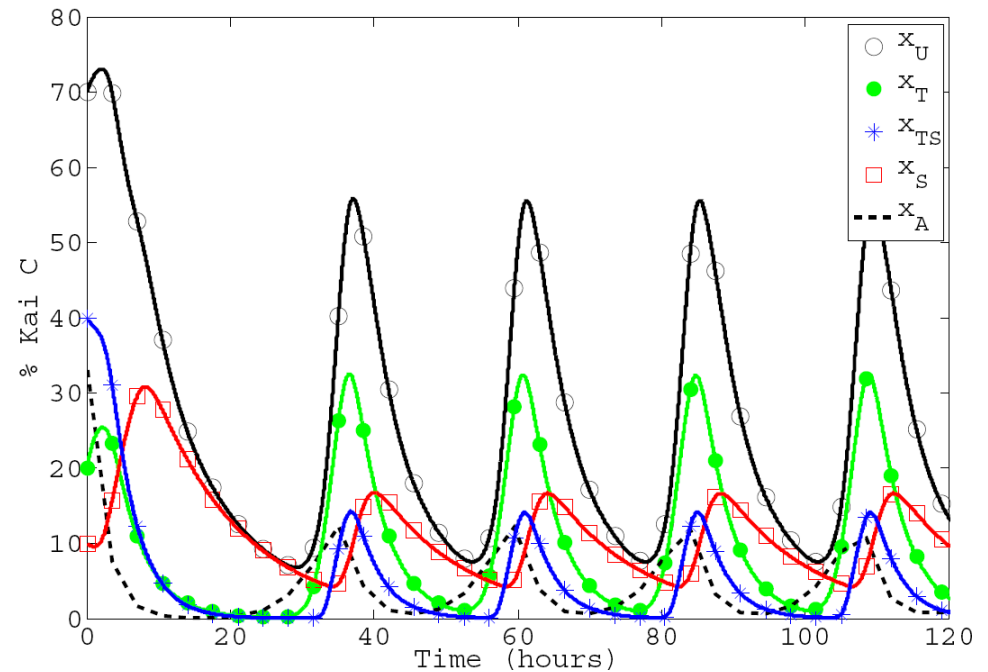
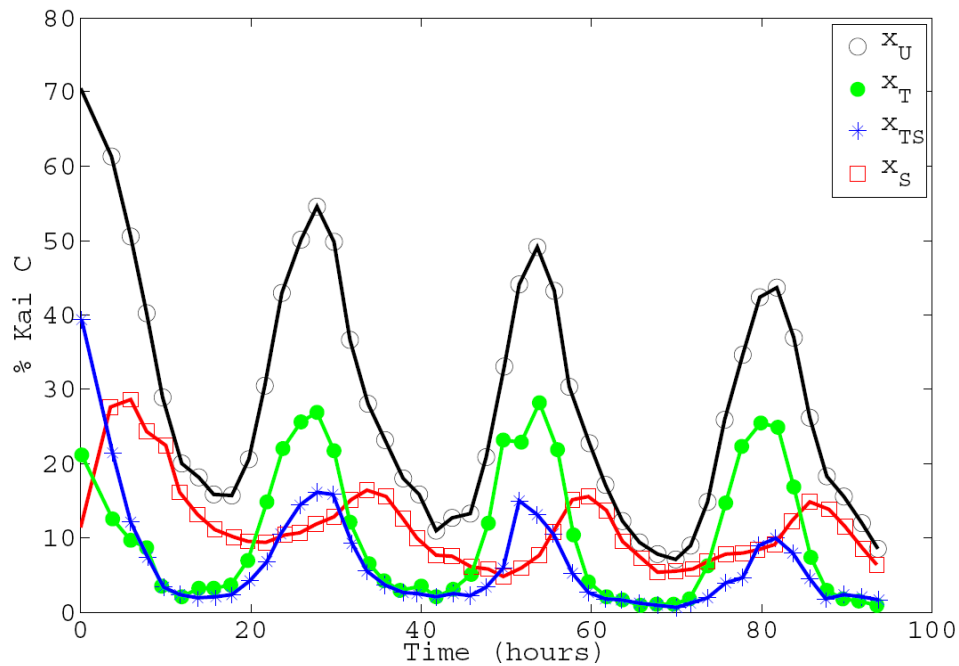
Putting all parameters together yields the correct oscillatory solution!



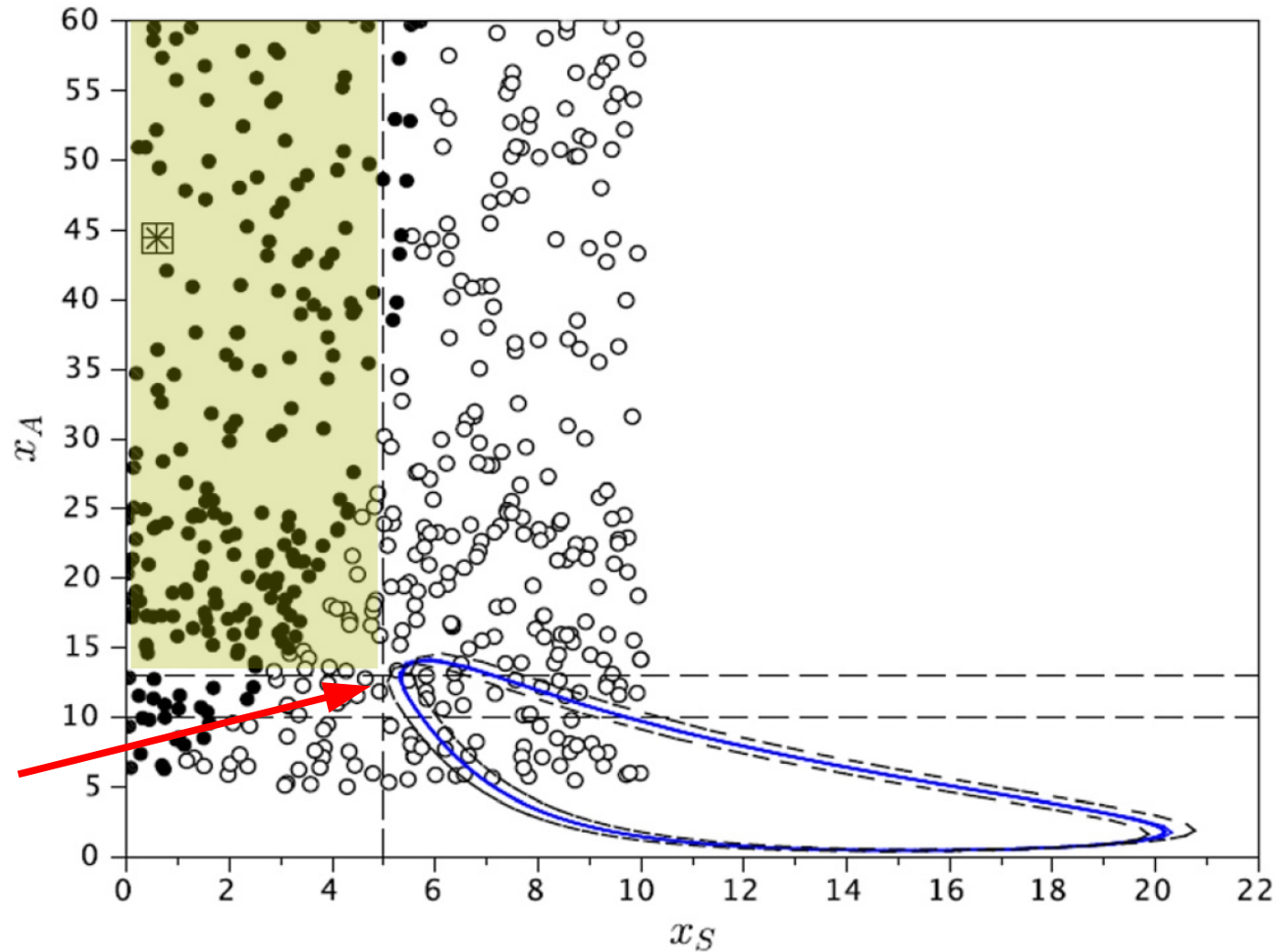
# Data vs. model comparison

Values of parameters were obtained from **two distinct sets of experiments, each for a “partial” model.**

Putting all parameters together yields the correct oscillatory solution!



# Model analysis



**Shaded:**  
Invariant  
Region (PWA)

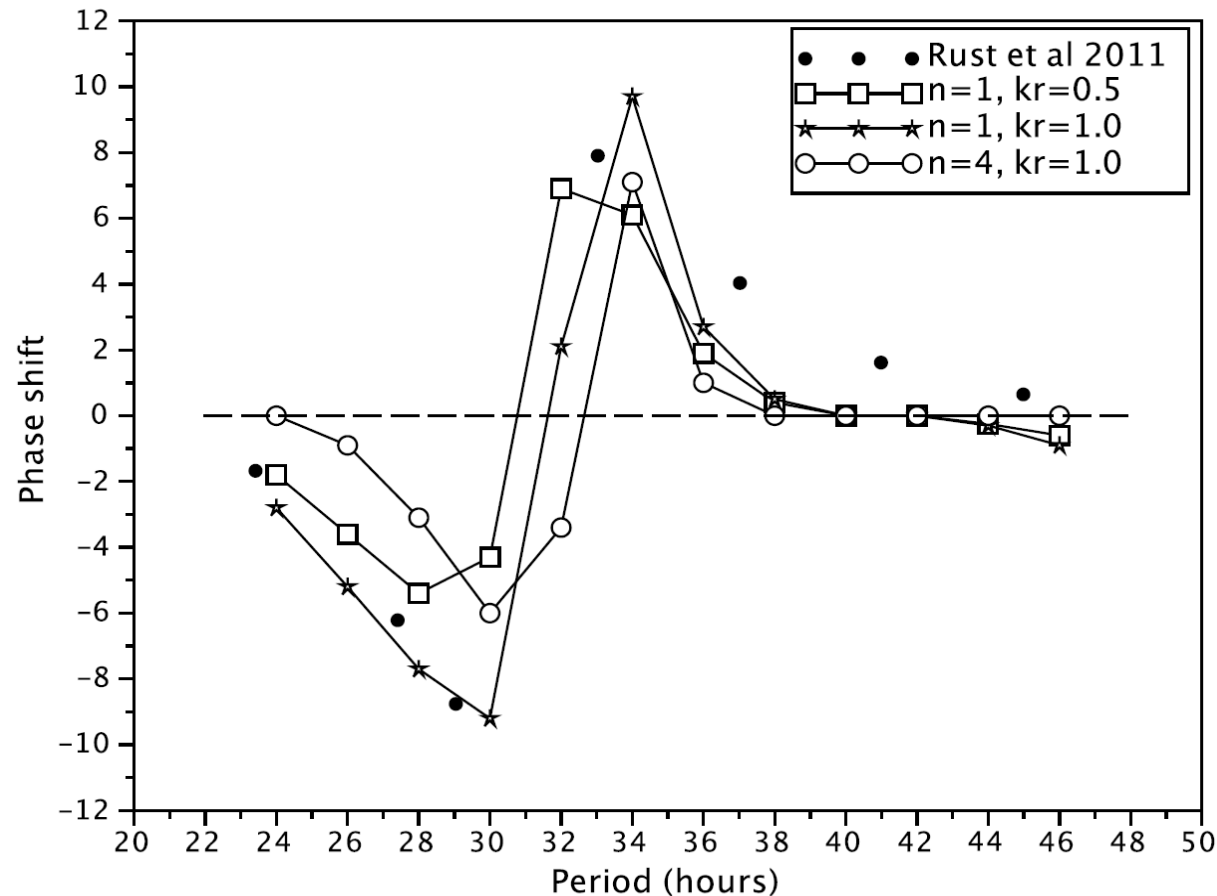
**Closed circles:**  
Basin of  
attraction of  $x^*$

**Open circles:**  
Basin of  
attraction  
of periodic orbit

$(\theta_S, \theta_{A,2})$

**PREDICTION:** there exist critical points in the periodic orbit, where the system may be perturbed and the **circadian cycle arrested** – such as when adding a large amount of Kai A.

# Model predictions: response to light

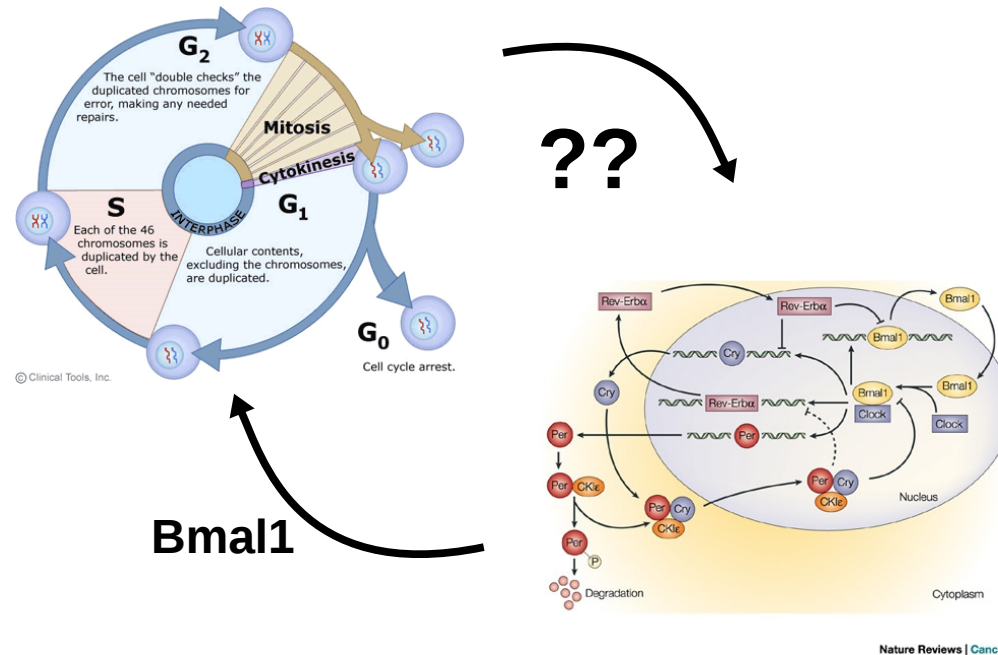


Chaves & Preto,  
Chaos 2013

Phase response to 5h pulses of ADP, applied at different instants during the circadian cycle. This experiment mimics clock entrainment by light – which varies the ratio  $ATP/(ATP+ADP)$ .

# Cell cycle and circadian rhythms

## How do they interact?



- The general belief (cf. cyanobacteria): **autonomous molecular clock**
- **Very few** possible links are known from clock to cell cycle (Bmal1 → Wee1)
- **Almost no knowledge** on how cell cycle affects clock (at mitosis gene expression shuts down)

# Cell cycle and circadian rhythms

## How do they interact?

### **Gating**

(cell division allowed only at certain clock phases)

**Observed in  
Cyanobacteria**



**Independent?**

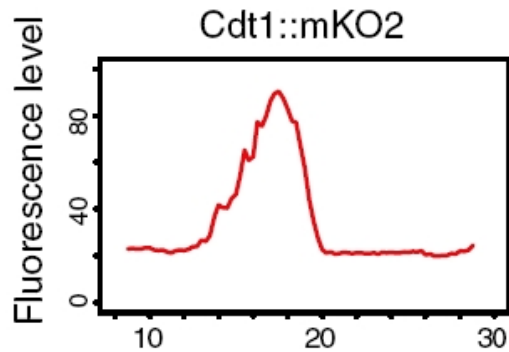
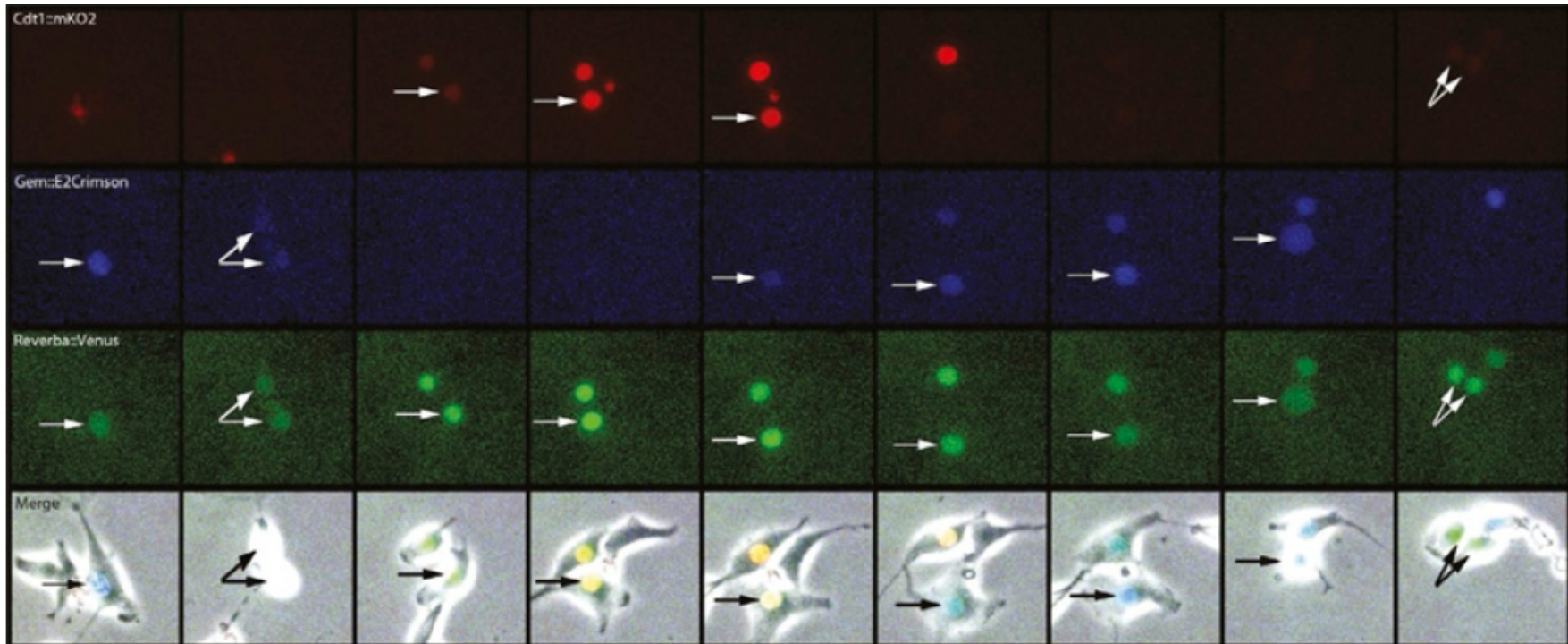
**Coordinated?**

**No gating in  
mammals**

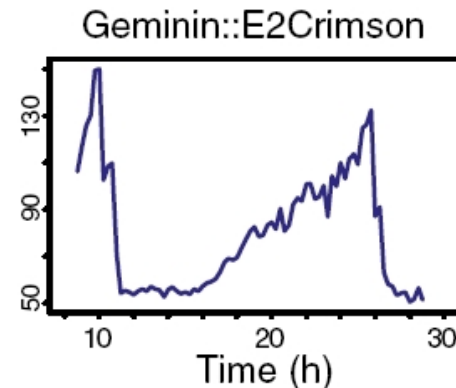


# Mammalian clock and cell cycle experiments

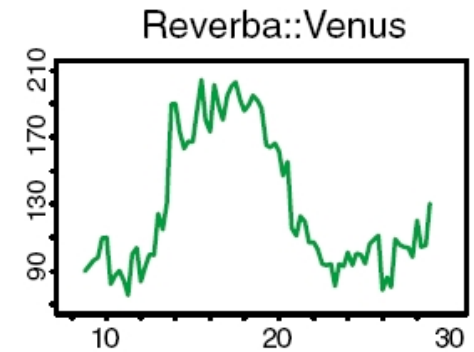
Feuillet et al, PNAS 2014 (Delaunay Lab) (Cells: mouse fibroblasts)



**Red:** cell cycle, G1 phase  
cells are growing



**Blue:** cell cycle, G2/S phase  
cells are getting ready to divide



**Green:** clock, high phase  
right after division

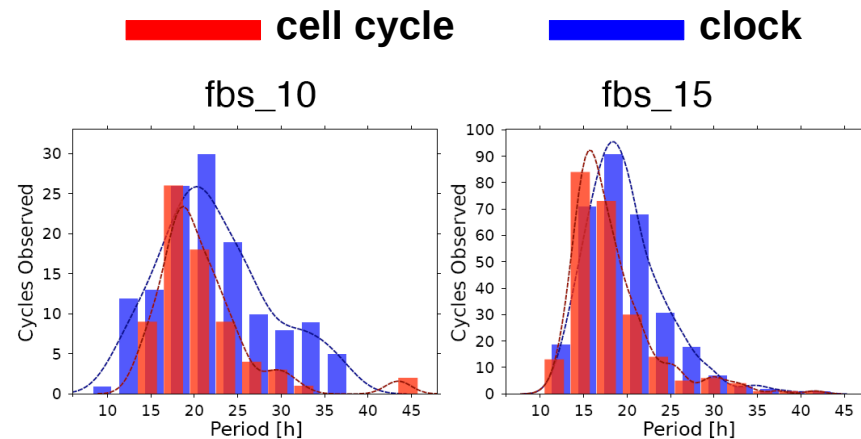


# Mammalian clock and cell cycle experiments

Feuillet et al, PNAS 2014 (Delaunay Lab) (Cells: mouse fibroblasts)

Change the cell cycle period ?

Apply different concentrations of growth hormone



- cell cycle period decreases
- clock decreases by same amount
- 1:1 lock

Evidence in favour of:

cell cycle



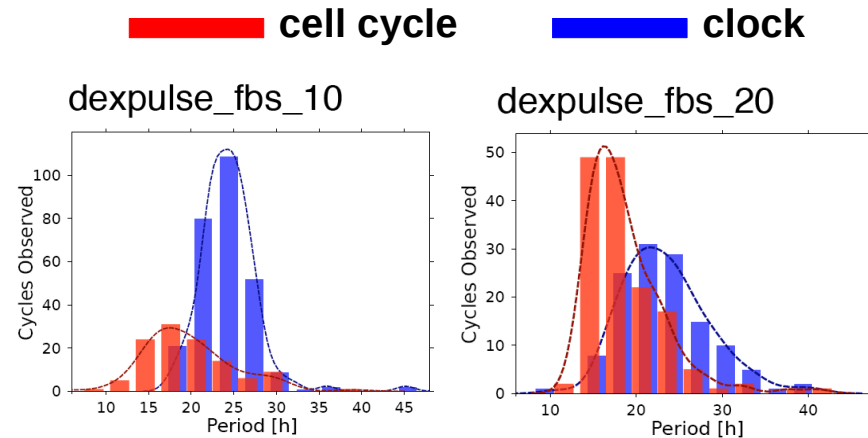
clock

# Mammalian clock and cell cycle experiments

Feuillet et al, PNAS 2014 (Delaunay Lab) (Cells: mouse fibroblasts)

Change the clock period ?

Apply a drug that synchronizes cells clock, dexamethasone



– synchronized cells

– two subpopulations (20% fbs):

1:1 lock

3:2 (cc:clock)

Evidence in favour of:

cell cycle



clock

# How to identify the coupling mechanism ?

Mammalian  
Clock +  
Cell cycle  
Too complex!

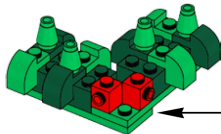
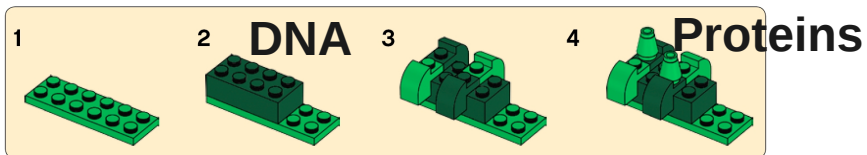
# How to identify the coupling mechanism ?

→ **SYNTHETIC BIOLOGY APPROACH**

collaboration  
F. Delaunay Lab

Mammalian  
Clock +  
Cell cycle  
Too complex!

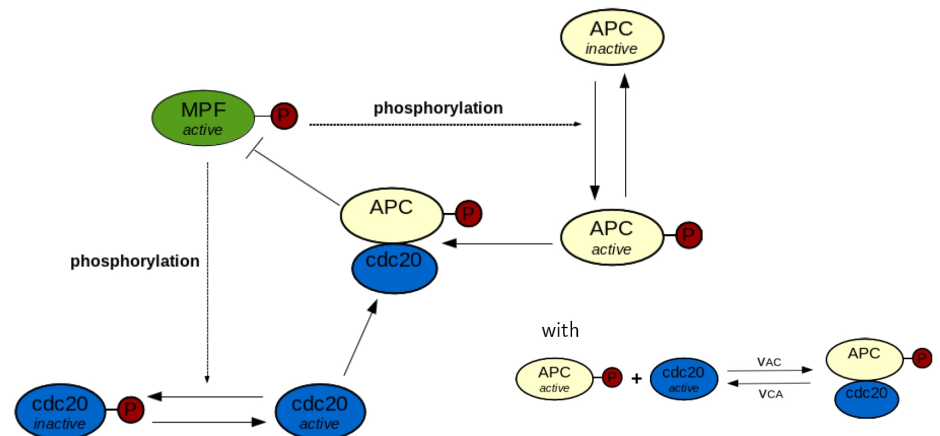
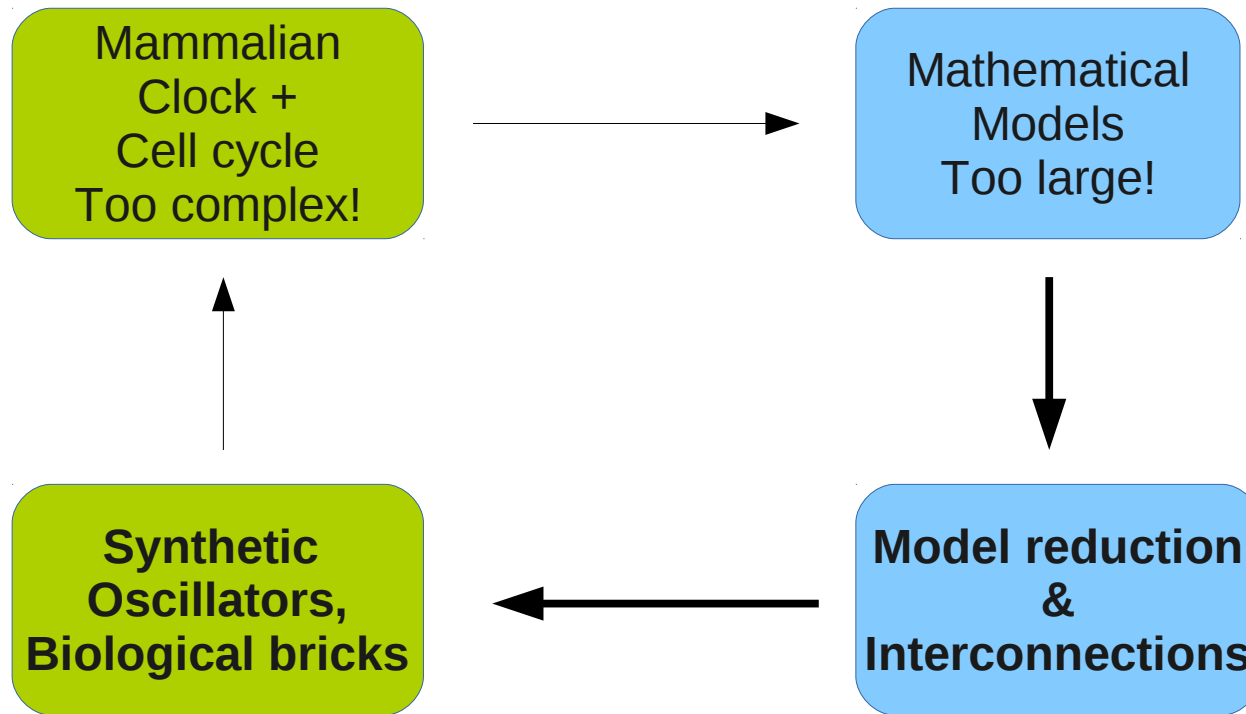
Synthetic  
Oscillators,  
Biological bricks



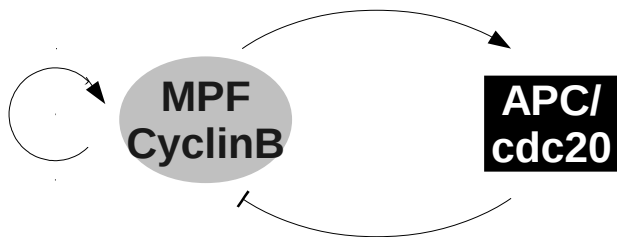
Activations,  
Inhibitions

# How to identify the coupling mechanism ?

→ **DYNAMICAL ANALYSIS & PREDICTIONS**

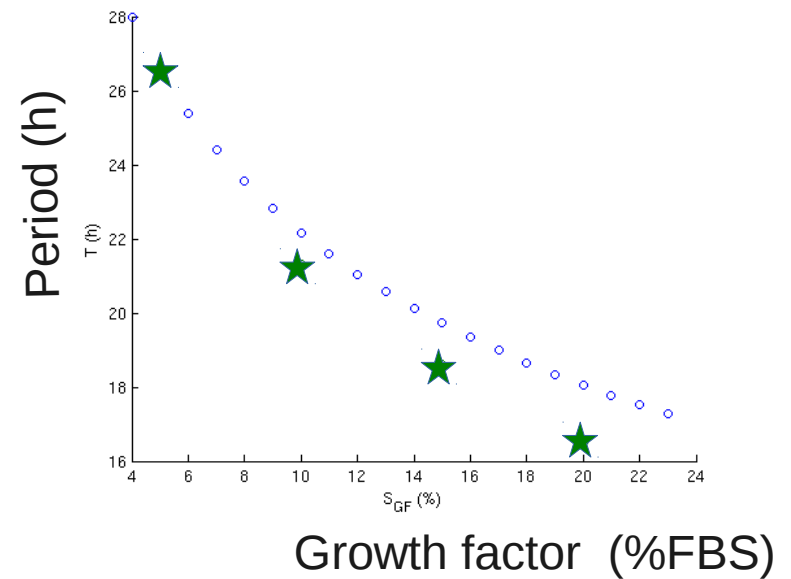
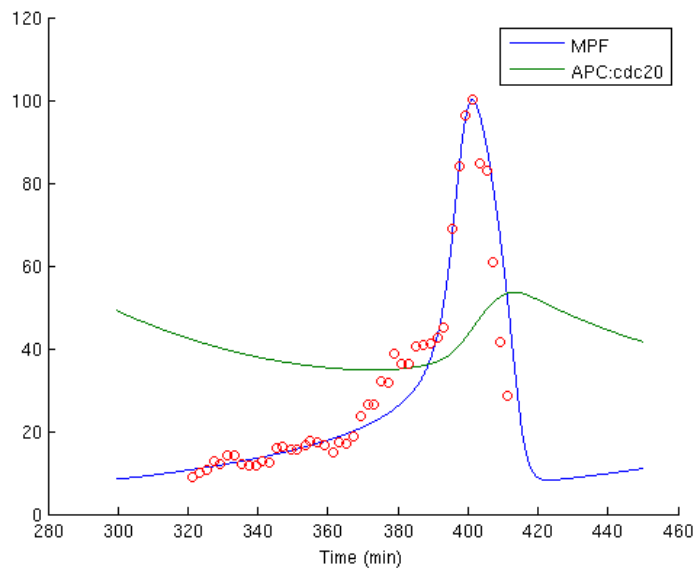


# Reduced cell cycle model

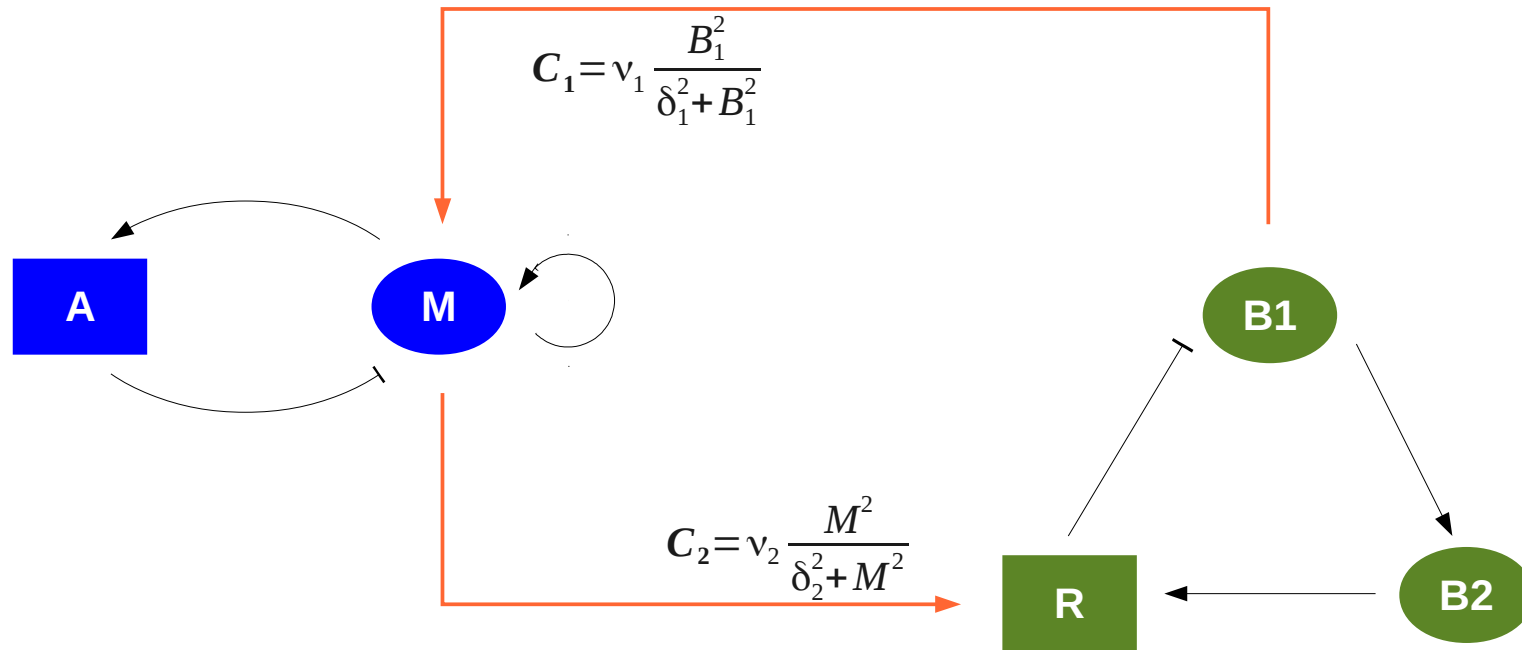


○ Model predictions  
(on growth factor)

★ Experimental data  
(fetal bovine serum)  
(F. Delaunay lab)



# Interconnecting cell cycle and clock



# Interconnecting cell cycle and clock

- Each oscillator has a different “individual” period
- When coupled, the two oscillators synchronize 1:1 (or stop oscillating)
- Question 1: **range of periods** over which the two oscillators synchronize?
- Question 2: is an oscillator either a **“controller”** or a **“follower”** ?  
  
ie., is the final period closer to the clock or cell cycle individual periods?
- Characterize dependence of these observations on the coupling strength



# In summary

- ▶ Cell cycle and circadian rhythms: Are they interconnected? And how? Many questions ! A current and lively topic
- ▶ Synthetic biology approach: minimal circuit design with desired properties
- ▶ Our tools: model reduction, mathematical analysis, and control

## Merci !

