

# Decision Making in (multi) Robot Systems

*Olivier Simonin*

*INSA Lyon – CITI Lab. - Inria Chroma team*



# Illustration ..



ANR Carotte Challenge - Final 2012  
Cartomatic team

# Outline

- I. Decision making ?
- II. Classical architectures
- III. Learning based architectures

---

- IV. Decision in multi-robot systems
- V. Strategies for multi-robot exploration

# Outline

- I. Decision making ?
- II. Classical architectures
- III. Learning based architectures

---

- IV. Decision in multi-robot systems
- V. Strategies for multi-robot exploration

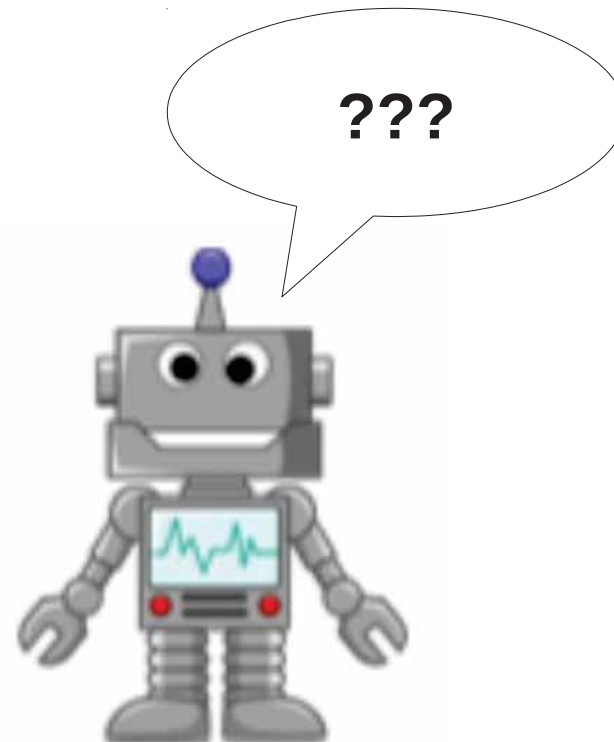
# Decide what ?

**Actions to fulfill my task**

**To avoid collisions / risks / breakdown**

**To cooperate with other robots**

...



# Decide what ?

**Actions to fulfill my task**

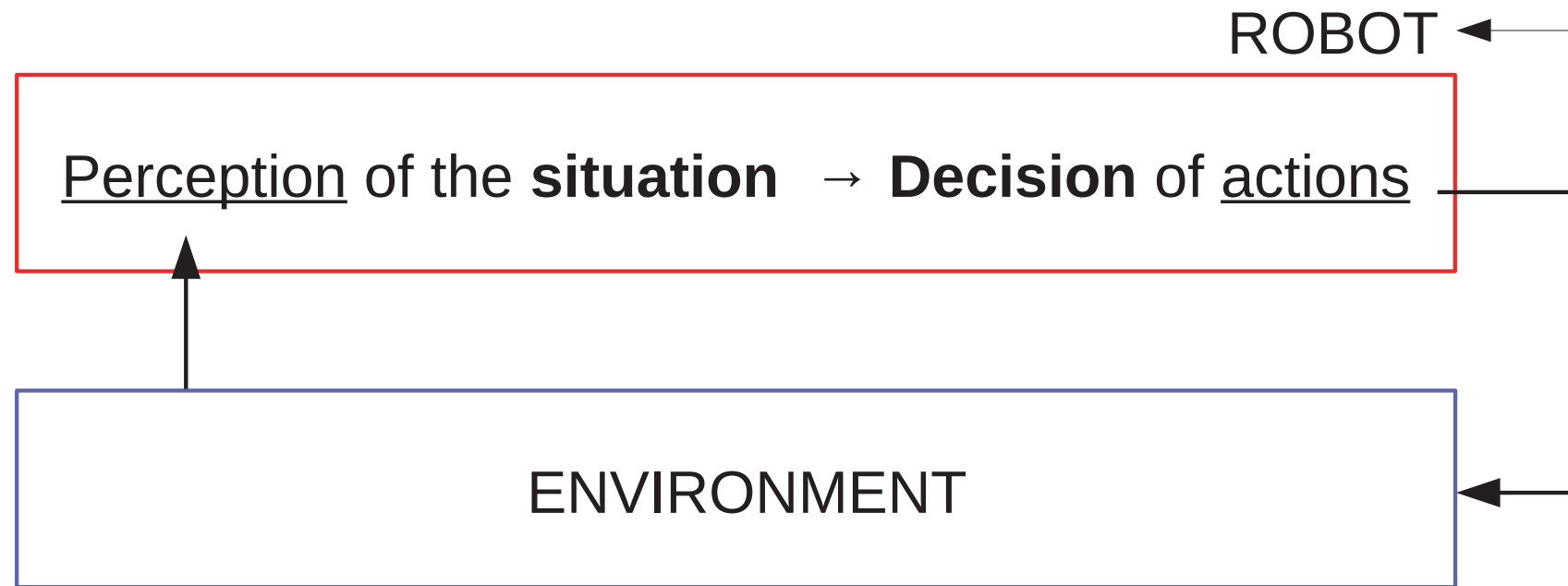
**To avoid collisions / risks / breakdown**

**To cooperate with other robots**

...

Perception of the **situation** → **Decision** of actions

# Loop Perception-Decision-Action



# Loop Perception-Decision-Action

ROBOT

Perception of the **situation** → **Decision** of actions

A.I.

Control



# Loop Perception-Decision-Action

ROBOT

Perception of the **situation** → **Decision** of actions

Modeling the environment

Situation awareness

Predict

# Ex.1 Situation awareness with probabilistic grid



Occupancy grid + veloc. + Bayesian F.

[Laugier et al. 2012-2018]

# Ex.1 Situation awareness with probabilistic grid

## Bayesian Occupancy Filtering (BOF<sup>1</sup>, CMCDOT<sup>2</sup>)

Occupancy grid

Velocity distribution / cell

Object identification (cell clustering)

Prediction of motion (bayes. filtering)

### Occupancy grid :

Probability of occupancy in each cell,  $P_{occ}(x,y)$

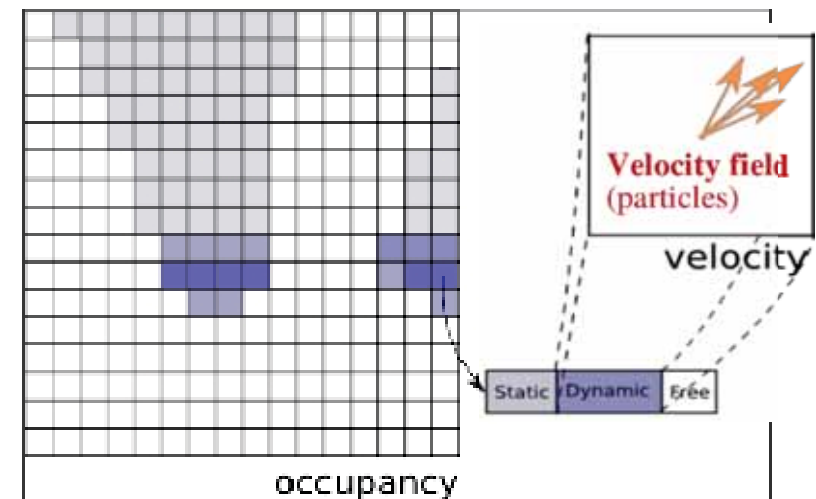
1 : occupied cell (black)

0.5 : unknown (gray)

0 : free cell (white)

e.g. Frequency approach (counting) :

$$P_{occ}(x,y) = \text{occ}(x,y) / (\text{empty}(x,y) + \text{occ}(x,y))$$



<sup>1</sup> C. Laugier et al., IJRR 2005, <sup>2</sup> Rummelhardt et al. ITS 2015

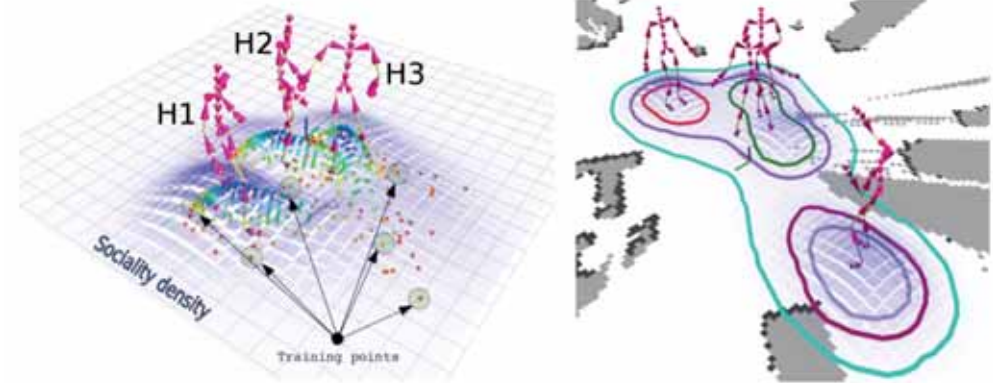
# Ex.2 Social navigation : Proxemics approach

Identify humans and predict their motion

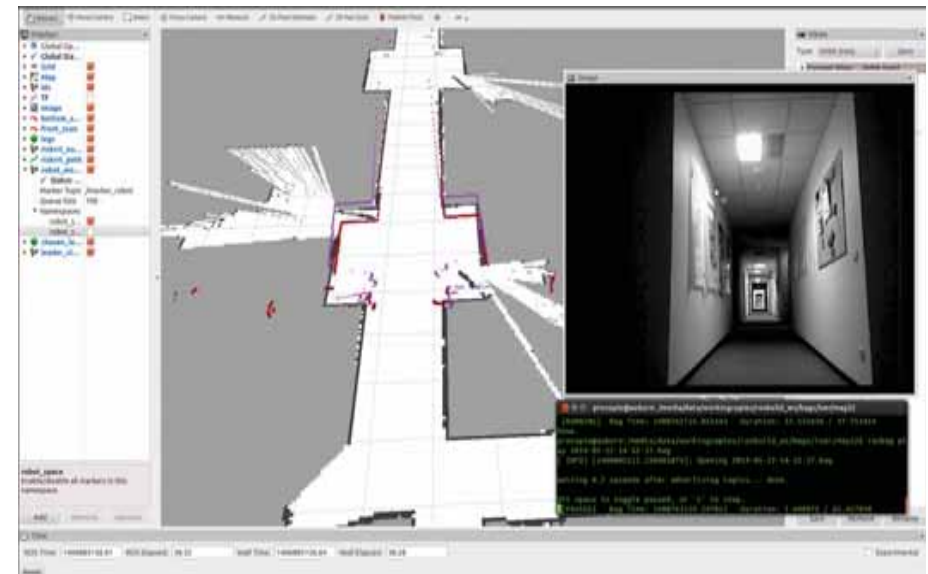
Comply with **social rules**

**Map** human activities

Compute **secure** paths and decisions



Gaussian model of personal area + geometric formation



# Loop Perception-Decision-Action

ROBOT

Perception of the **situation** → **Decision** of actions

Reacting

Planning / Learning

# Reacting vs. Planning vs. Learning

**Reacting** : compute **one action** (real time)

**Planning** : compute a **sequence** of actions (eg. motion planning)

**Learning** : compute a **policy** (state → action)

+

**Cooperate/compete** : add **other agents** in the decision

# Reacting vs. Planning vs. Learning

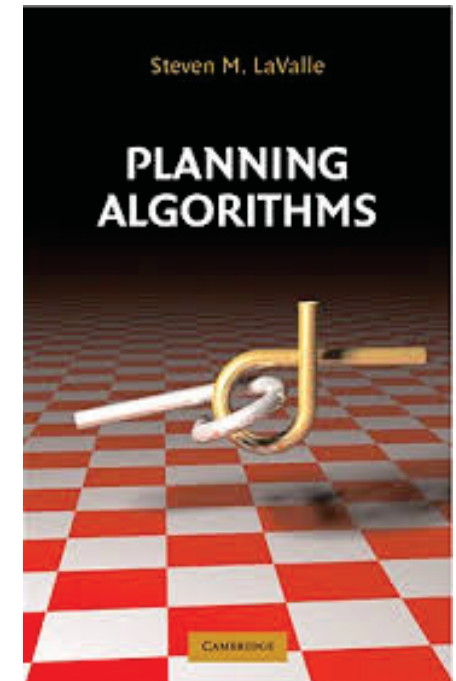
**Reacting** : Bio-inspired behaviors, Connexionism

**Planning** : STRIPS, PDDL, SAT, CSP, PRM ..

**Learning** : Reinforcement L., (PO)MDP, RNN, DeepLearning

+

**Cooperate/compete** : add other agents in the decision



# Outline

- I. Decision making ?
- II. Classical architectures
- III. Learning based architectures

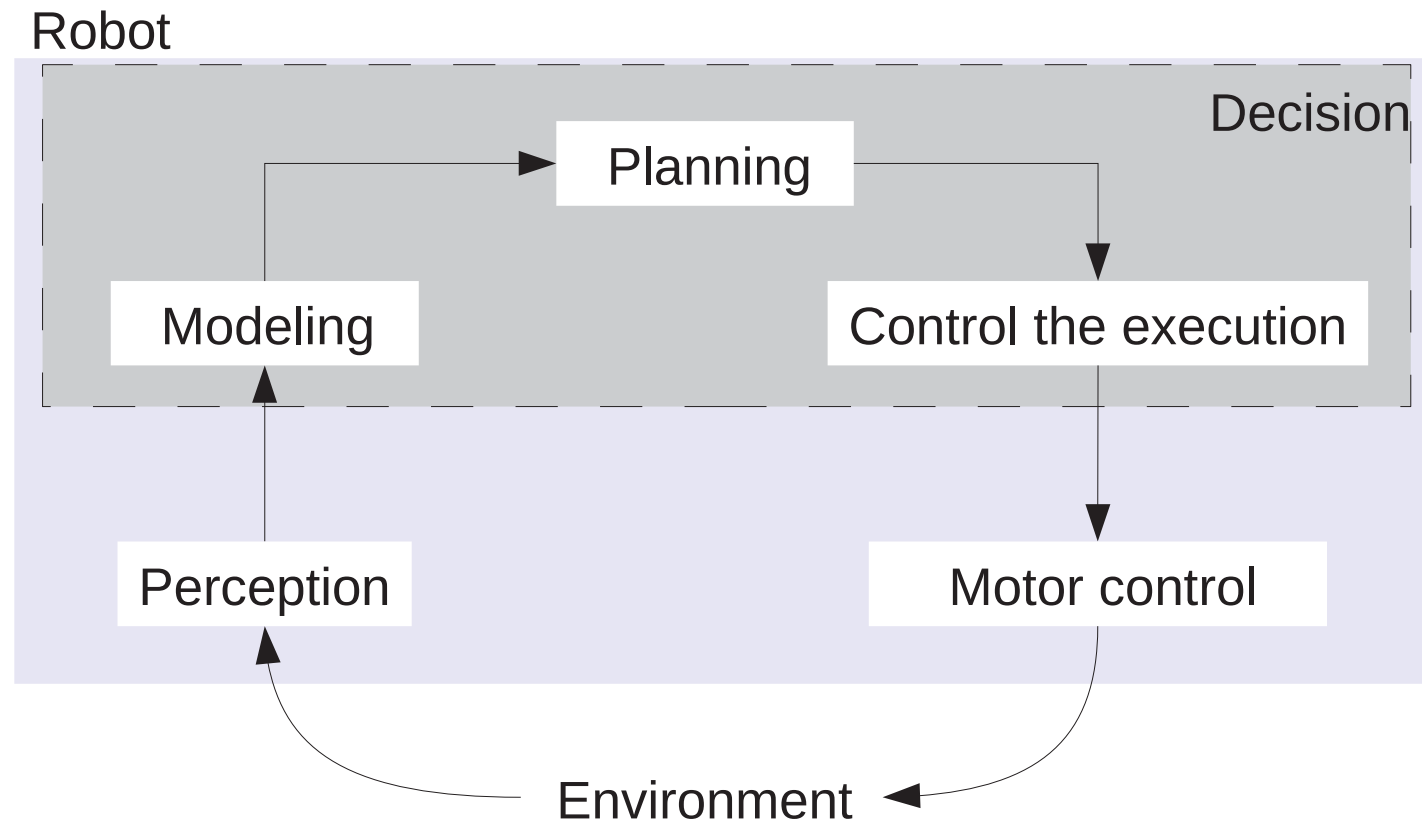
---

- IV. Decision in multi-robot systems
- V. Strategies for multi-robot exploration



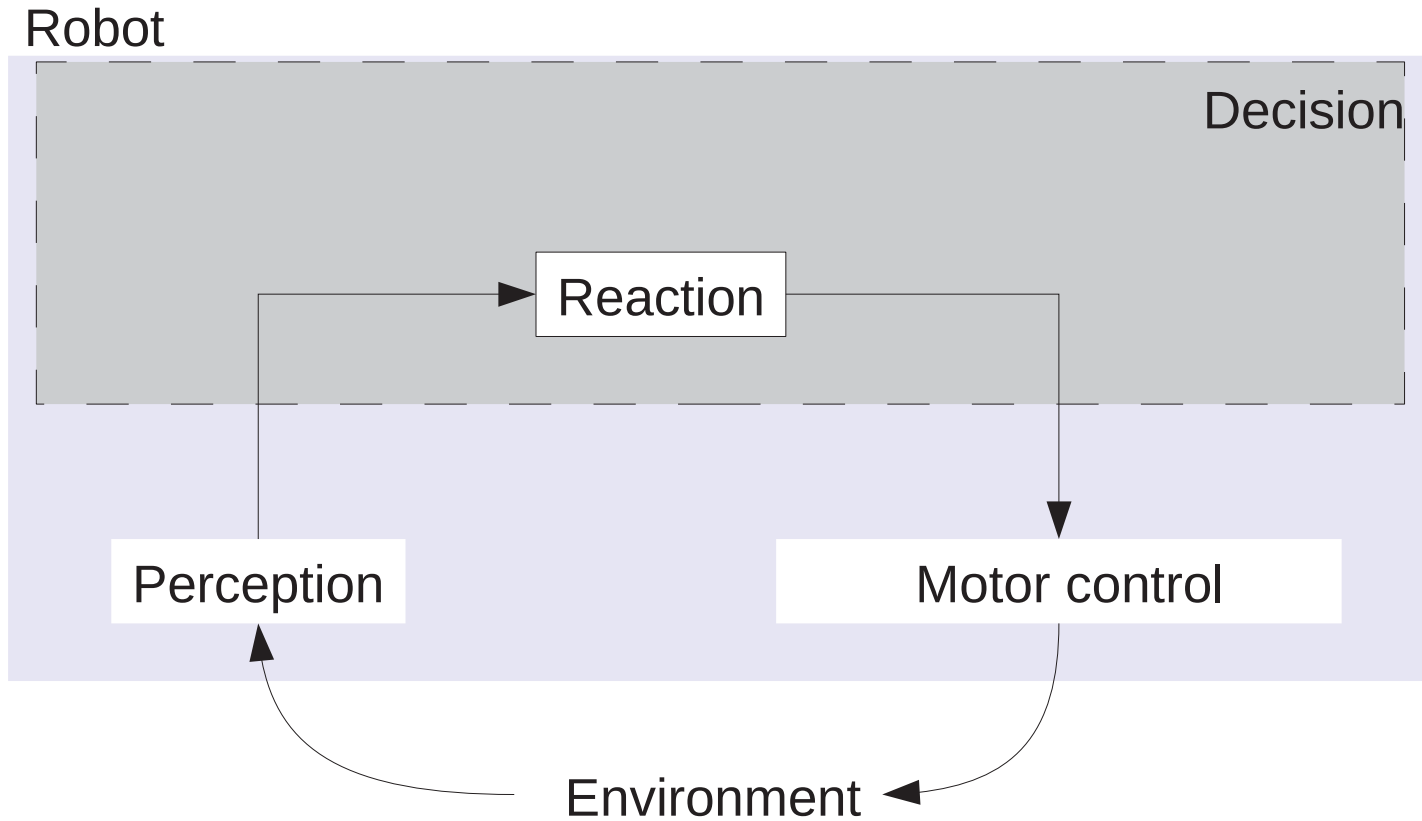
# Sense-Plan-Act

[Nilsson80]



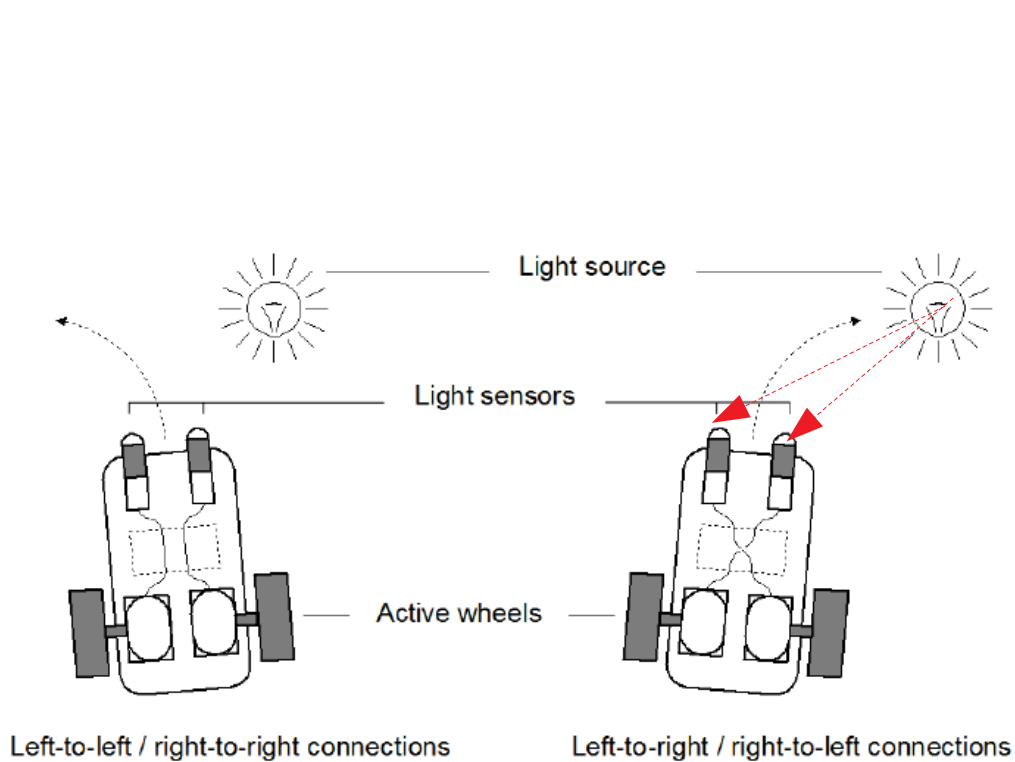
Slow planning → bottleneck !

# Reactive architecture

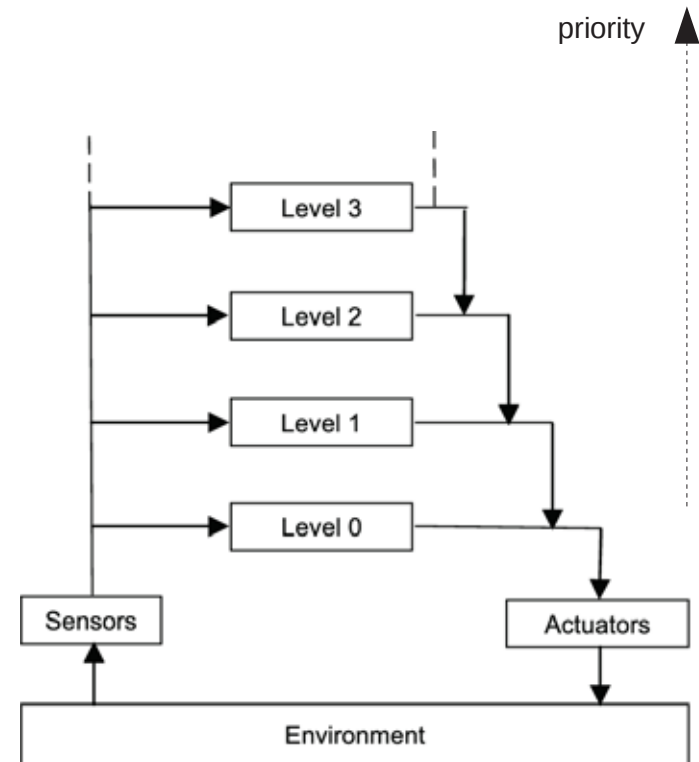


[Brooks 86] [Arkin 98]. Connecting sensors-motors, but **deadlocks** are possible !

# Reactive architecture : Braitenberg, Brooks



[Braitenberg 84] Vehicle (phototaxis)

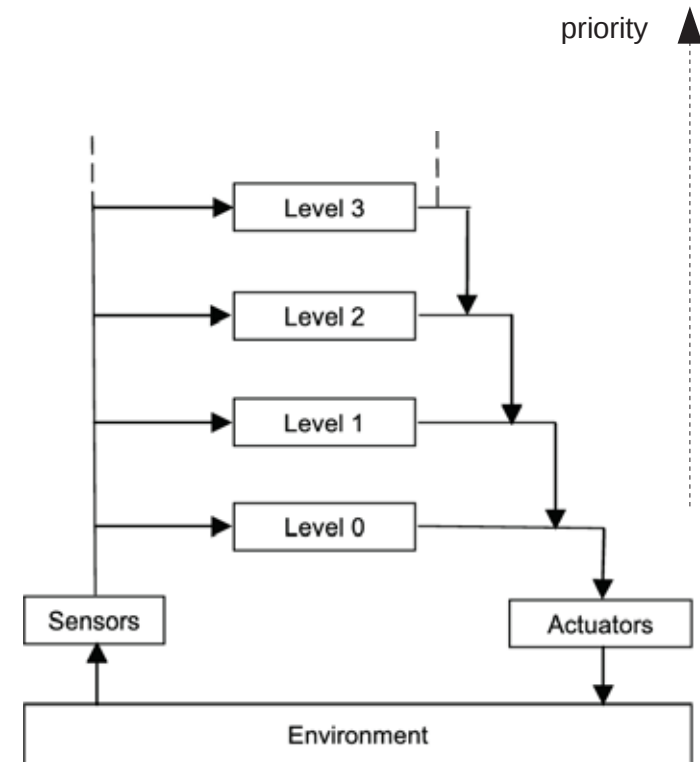


[Brooks 86] Subsumption architecture

# Reactive architecture : Braitenberg, Brooks

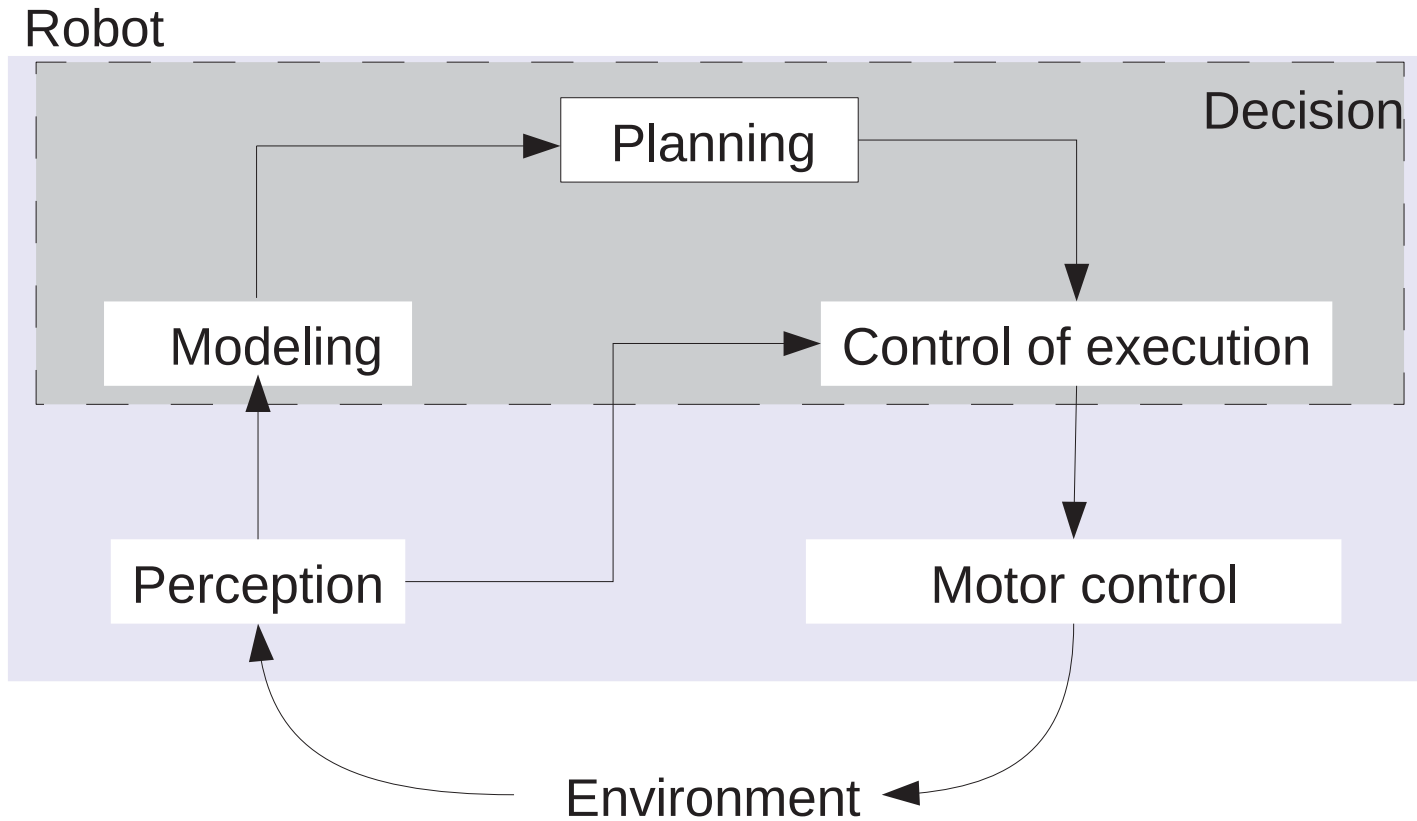


[Braitenberg 84] Vehicle (phototaxis)



[Brooks 86] Subsumption architecture

# Multi-level architecture



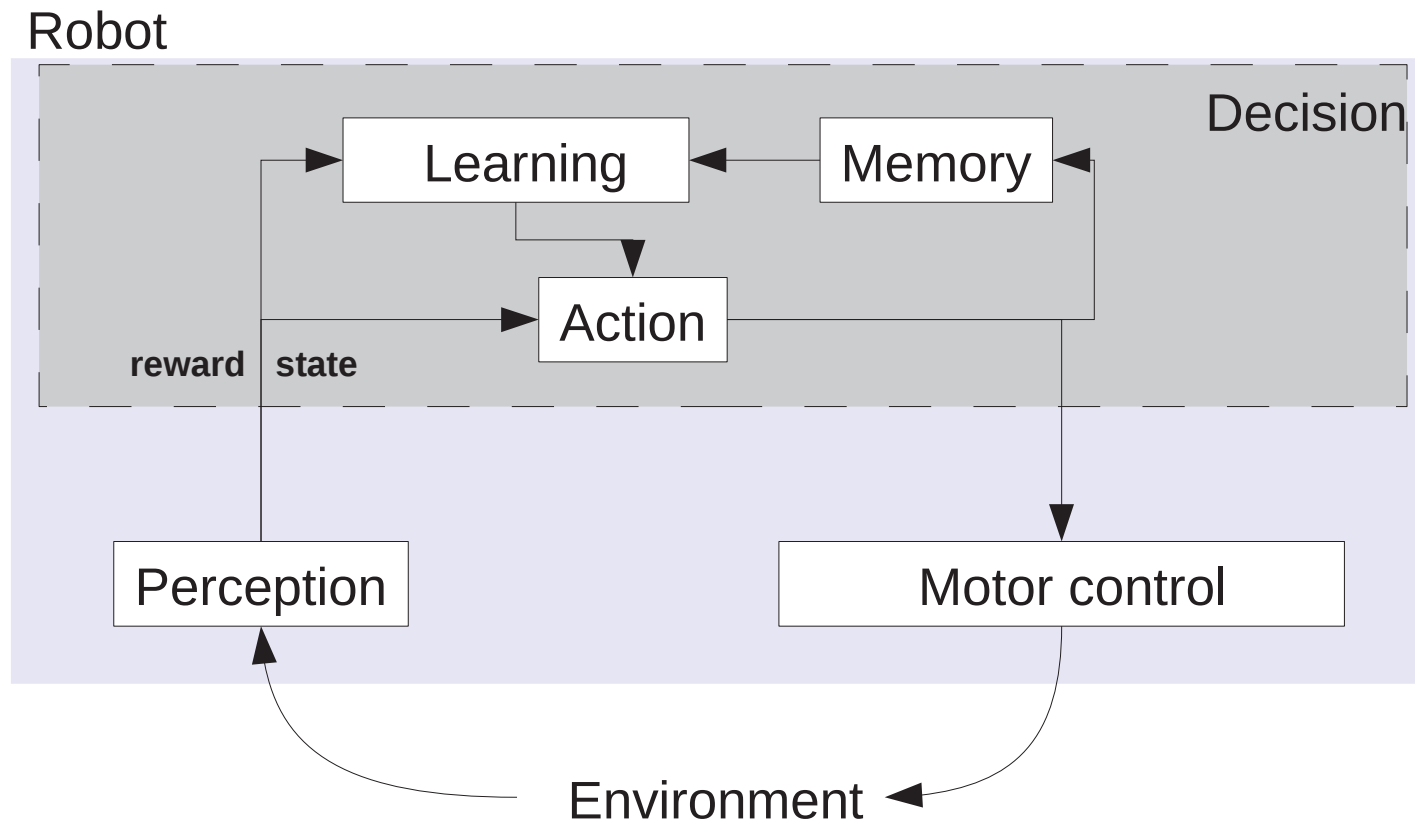
Allow to combine fast reaction and planning

# Outline

- I. Decision making ?
- II. Classical architectures
- III. Learning based architectures**

---
- IV. Decision in multi-robot systems
- V. Strategies for multi-robot exploration

# Learning architecture : non explicit knowledge repr.



Neuronal networks, Reinforcement Learning, Markov Decision Process (MDP) ..

# Q-Learning [Watkins 89] (Reinforcement Learning)

Compute the **quality of an action  $a$  in state  $s$**  ( $s \in S, a \in A$ )

$$Q : S \times A \rightarrow \mathbb{R}$$

Each time step  $t$  the agent selects an action  $a_t$ , **observes a reward  $r_t$** , enters in new state  $s_{t+1}$ .

**Then  $Q(s,a)$  is updated :**

$$Q^{new}(s_t, a_t) \leftarrow (1 - \alpha) \cdot \underbrace{Q(s_t, a_t)}_{\text{old value}} + \underbrace{\alpha}_{\text{learning rate}} \cdot \left( \underbrace{r_t}_{\text{reward}} + \underbrace{\gamma}_{\text{discount factor}} \cdot \underbrace{\max_a Q(s_{t+1}, a)}_{\text{estimate of optimal future value}} \right)$$

learned value

Converge to optimal policy that **maximizes the expected cumulative reward**  $\sum_{t=0}^{\infty} \gamma^t r_t$   
(proof [Watkins, Dayan 92] )



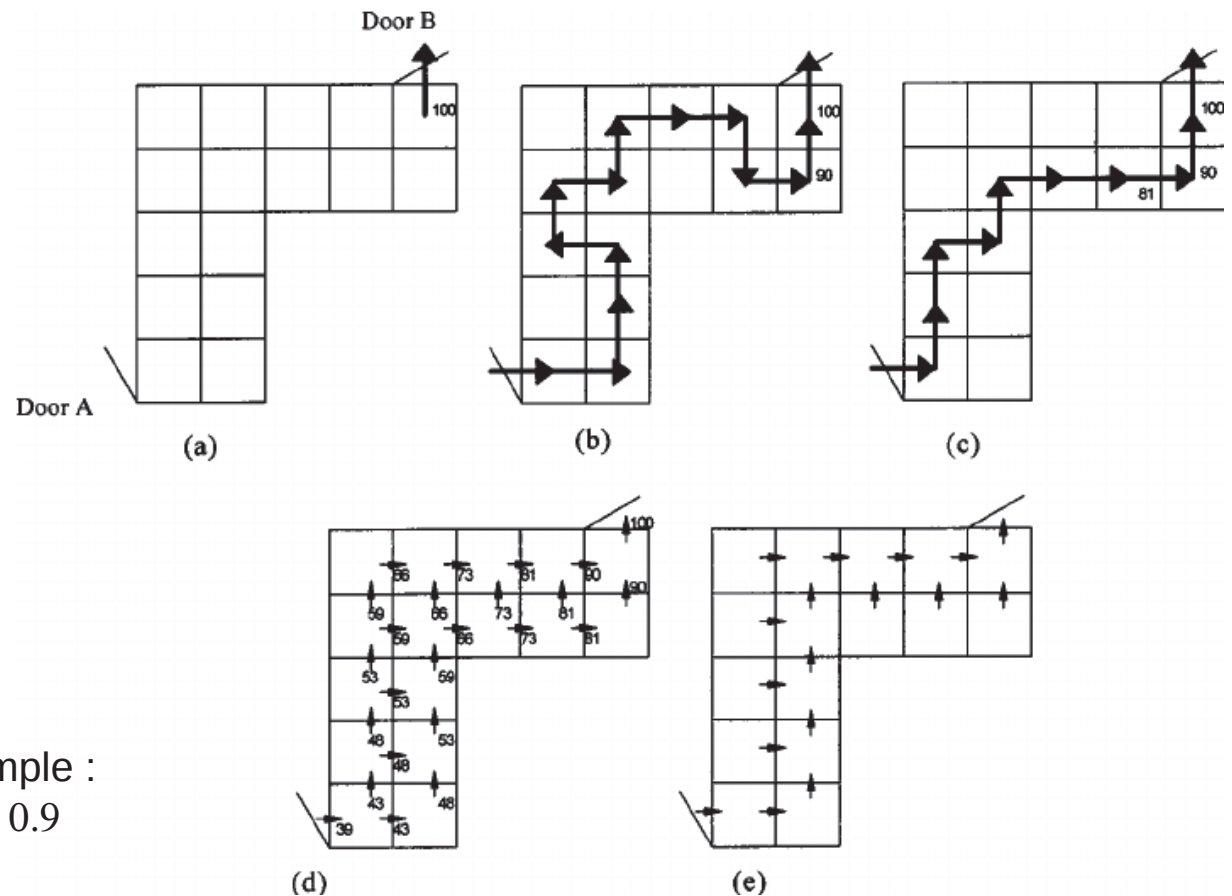
# Q-Learning [Watkins 89] (Reinforcement Learning)

$$Q^{new}(s_t, a_t) \leftarrow (1 - \alpha) \cdot \underbrace{Q(s_t, a_t)}_{\text{old value}} + \underbrace{\alpha}_{\text{learning rate}} \cdot \left( \underbrace{r_t}_{\text{reward}} + \underbrace{\gamma}_{\text{discount factor}} \cdot \underbrace{\max_a Q(s_{t+1}, a)}_{\text{estimate of optimal future value}} \right)$$

learned value

The agent must explore/experiment the environment

→ exploration/exploitation dilemma



Grid example :  
 $\alpha = 1$   $\gamma = 0.9$

# Modeling uncertainty : Markov Decision Process

MDP : 4-tuple  $(S, A, P_a, R_a)$

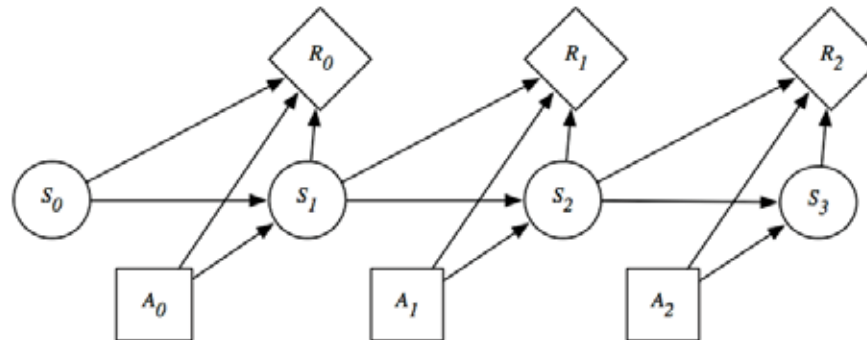
Actions' result is uncertain : that is true in robotics !

Exploit a [model of the environment/system dynamics](#) :

The probability that action  $a$  , in state  $s$  at time  $t$  will lead to state  $s'$  at time  $t+1$  is

$$P_a(s,s') = \Pr(s_{t+1} = s' \mid s_t = s, a_t = a)$$

Each action  $a$  , from state  $s$  to state  $s'$  gives an immediate [reward](#)  $R_a(s,s') \in \mathfrak{R}$



# Modeling uncertainty : Markov Decision Process

MDP : 4-tuple  $(S, A, P_a, R_a)$

**Actions' result is uncertain : that is true in robotics !**

Exploit a [model of the environment/system dynamics](#) :

The probability that action  $a$  , in state  $s$  at time  $t$  will lead to state  $s'$  at time  $t+1$  is

$$P_a(s,s') = \Pr(s_{t+1} = s' \mid s_t = s, a_t = a)$$

Each action  $a$  , from state  $s$  to state  $s'$  gives an immediate [reward](#)  $R_a(s,s') \in \mathfrak{R}$

**Problem** : finding a **policy**  $\pi$  that maximizes a cumulative function of the random rewards

$$\sum_{t=0}^{\infty} \gamma^t R_{a_t}(s_t, s_{t+1}) \quad a_t = \pi(s_t) \quad \rightarrow \text{Reinforcement Learning}$$

# Modeling uncertainty : Markov Decision Process

MDP : 4-tuple  $(S, A, P_a, R_a)$

**Actions' result is uncertain : that is true in robotics !**

Exploit a [model of the environment/system dynamics](#) :

The probability that action  $a$  , in state  $s$  at time  $t$  will lead to state  $s'$  at time  $t+1$  is

$$P_a(s,s') = \Pr(s_{t+1} = s' \mid s_t = s, a_t = a)$$

Each action  $a$  , from state  $s$  to state  $s'$  gives an immediate [reward](#)  $R_a(s,s') \in \mathfrak{R}$

**Problem** : finding a **policy**  $\pi$  that maximizes a cumulative function of the random rewards

**Several solutions :**

- Value iteration [Bellman 57]
- Policy iteration [Howard 60]
- ..

$$\pi(s) := \arg \max_a \left\{ \sum_{s'} P(s'|s, a) (R(s'|s, a) + \gamma V(s')) \right\}$$

$$V(s) := \sum_{s'} P_{\pi(s)}(s, s') (R_{\pi(s)}(s, s') + \gamma V(s'))$$

Computation can be very expensive..

# Modeling uncertainty : Markov Decision Process

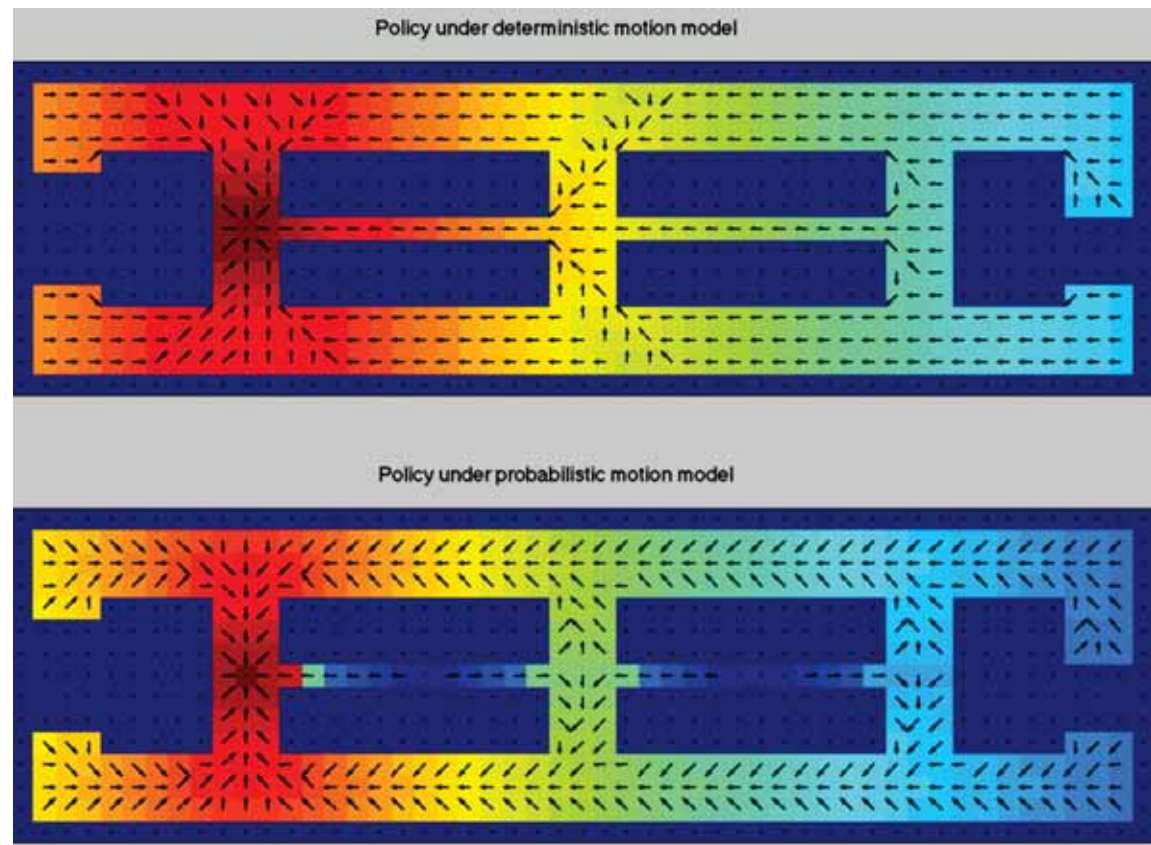
MDP : 4-tuple  $(S, A, P_a, R_a)$

Actions' result is uncertain : that is true in robotics !

Exploit a [model of the environment/system dynamics](#) :

The probability that action  $a$  , in state  $s$  at time  $t$  will lead to state  $s'$  at time  $t+1$  is

$$P_a(s,s') = \Pr(s_{t+1} = s' \mid s_t = s, a_t = a)$$



# Modeling uncertainty : Markov Decision Process

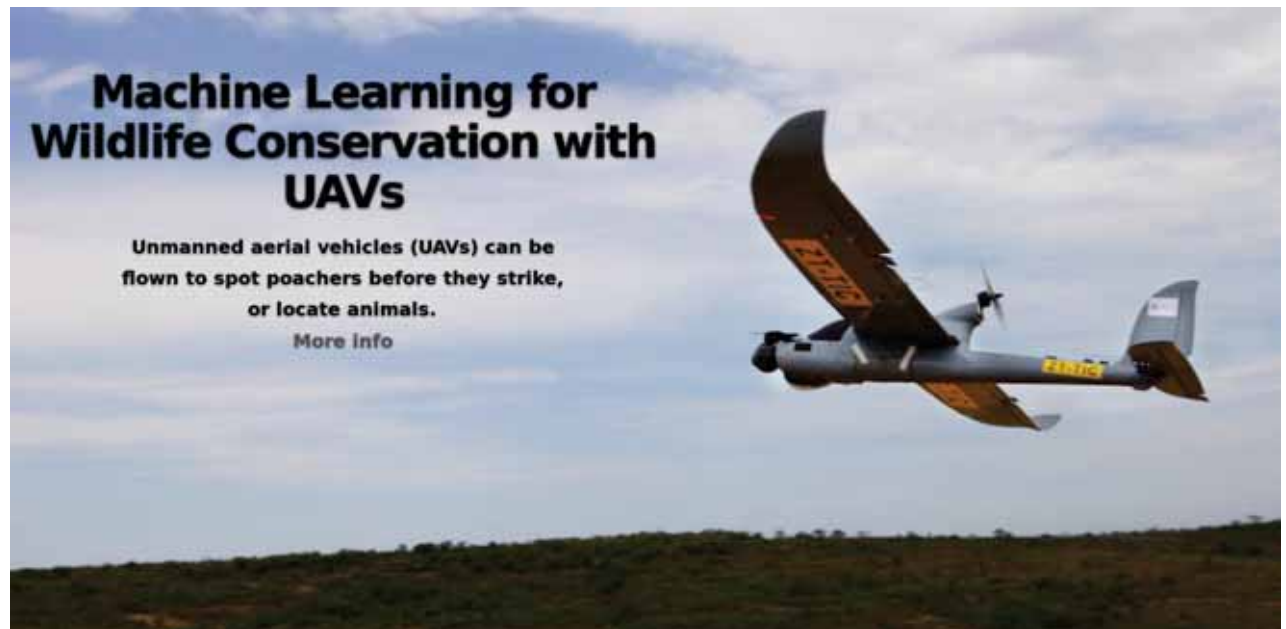
MDP : 4-tuple  $(S, A, P_a, R_a)$

**Actions' result is uncertain : that is true in robotics !**

Exploit a [model of the environment/system dynamics](#) :

The probability that action  $a$  , in state  $s$  at time  $t$  will lead to state  $s'$  at time  $t+1$  is

$$P_a(s,s') = \Pr(s_{t+1} = s' \mid s_t = s, a_t = a)$$



Good introduction :

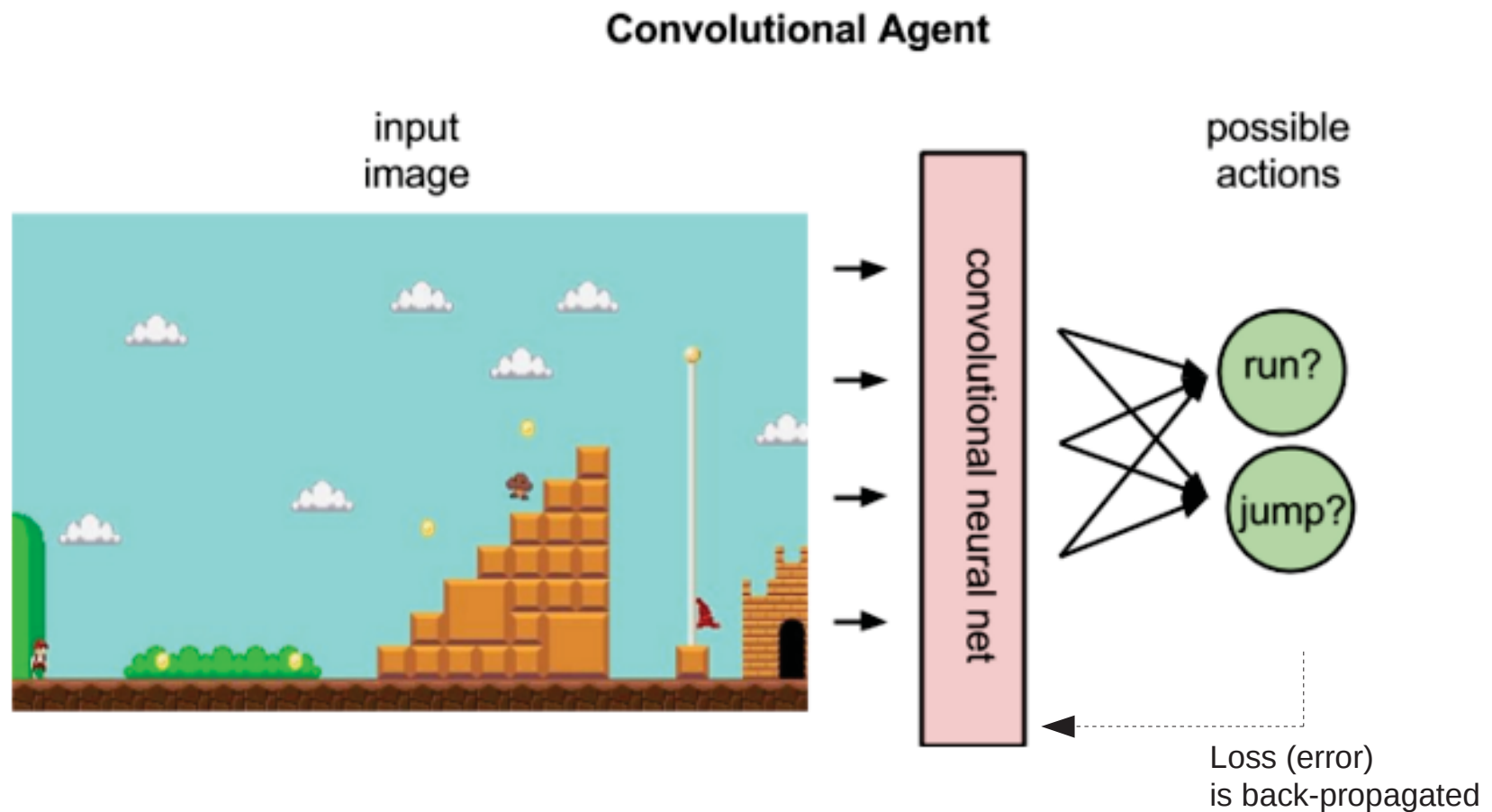
*Reinforcement Learning: a Survey*

L. P. Kaelbling, M. L. Littman, W. Moore  
1996.

Milind Tambe team USC, CAIS

# End to End Deep Learning

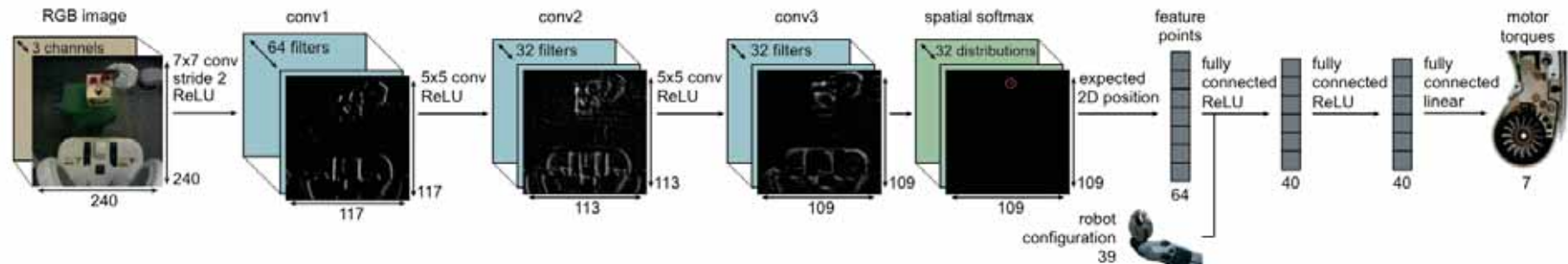
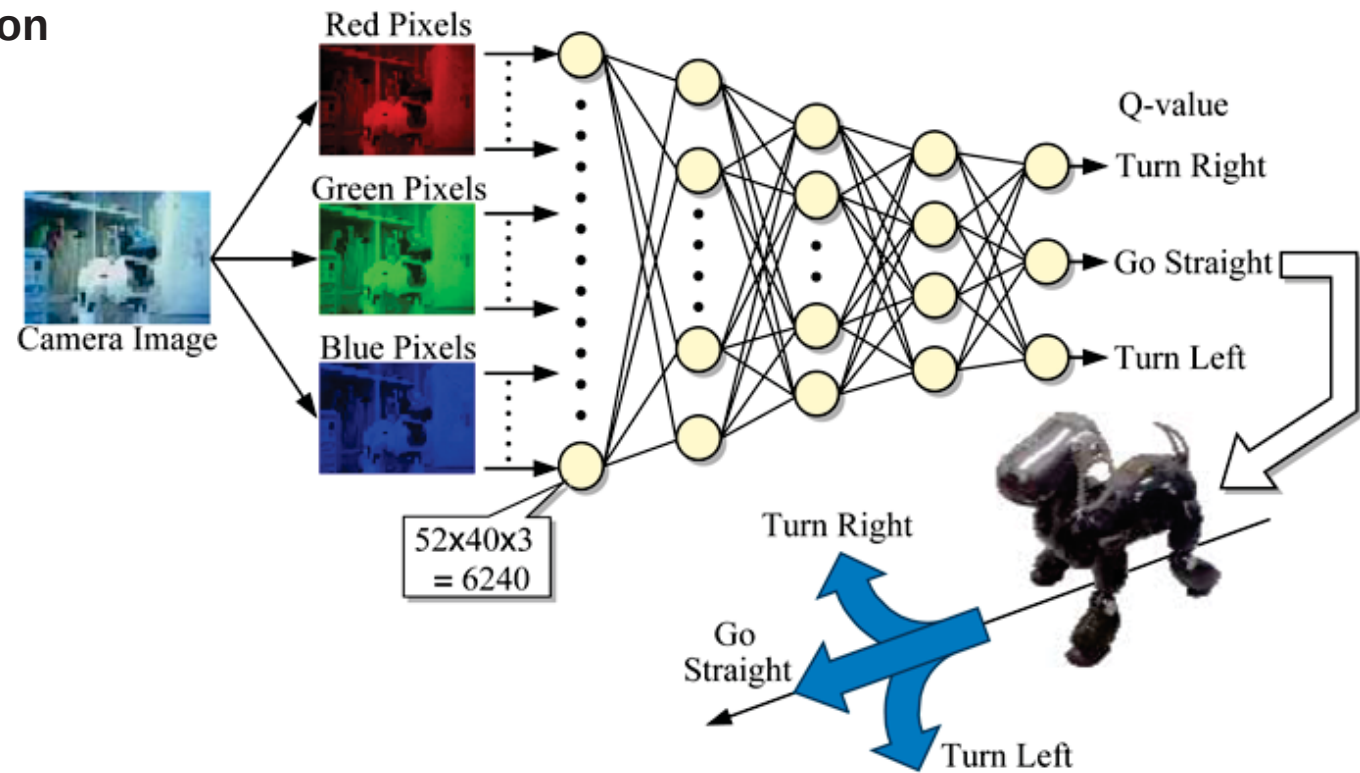
n processes → 1 single Neural Network





# End to End Deep Learning

CNN allows generalization





# Outline

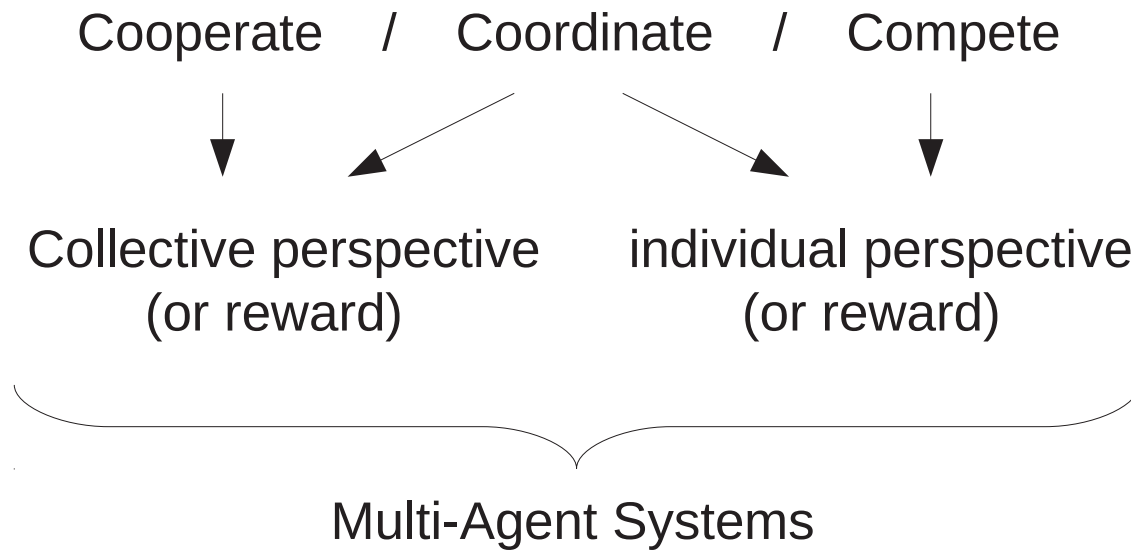
- I. Decision making ?
- II. Classical architectures
- III. Learning based architectures

---

- IV. Decision in multi-robot systems
- V. Strategies for multi-robot exploration



# Multi-Agent Systems (MAS)



*Autonomous agents that interact in a common environment  
in order to fulfill collective and/or individual objectives*

J. Ferber, Multi-Agent Systems, Addison Wesley, London, 1999

# Multi-robot missions

EXPLORATION

Mapping (eg. SLAM)

Search, Coverage, Patrolling

Tracking, Active perc.

OBSERVATION

TRANSPORT

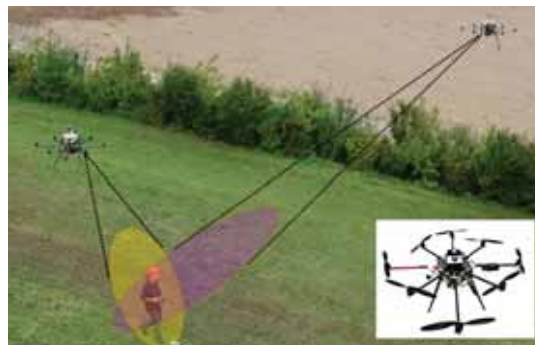
Collective Trans.  
(eg. box pushing)

Traffic regulation

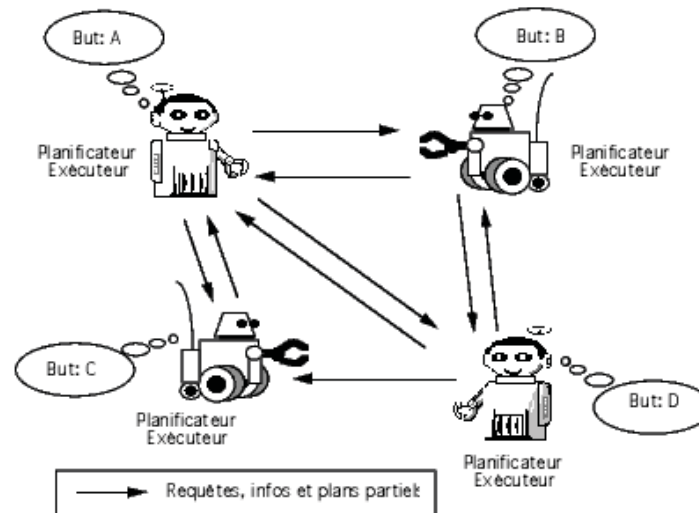
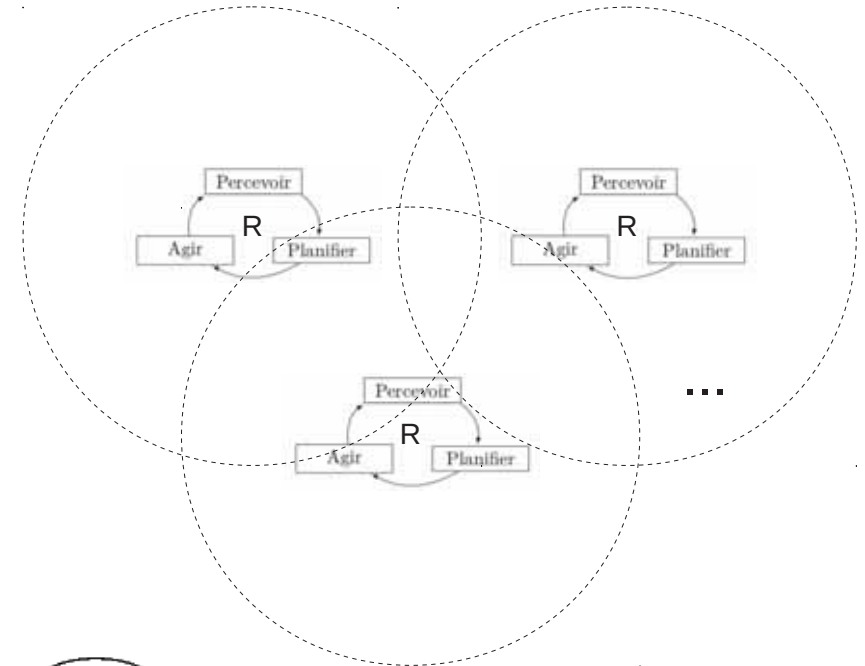
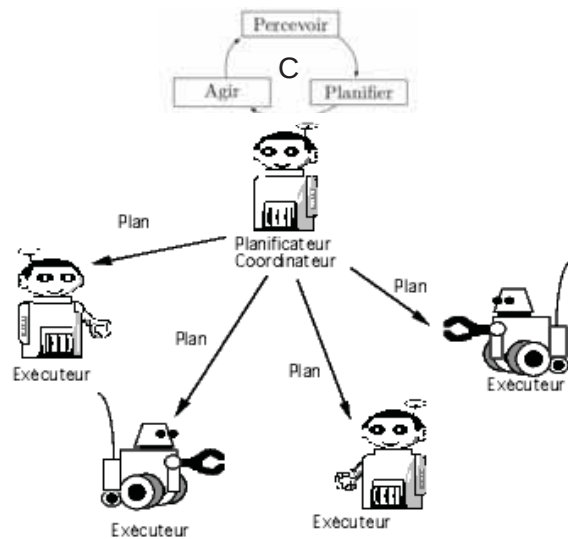
Autonomous fleet navig.

Connectivity

FORMATION MAINT.



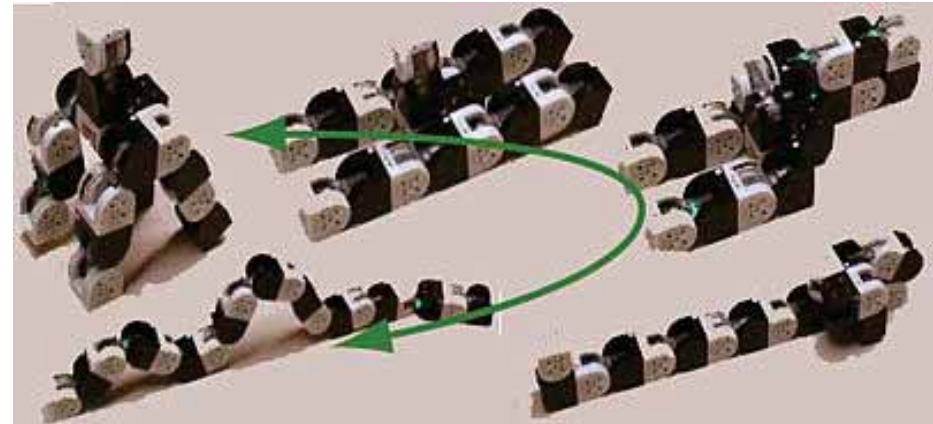
# Centralized, Decentralized and Distributed systems



# Decentralized : collective navigation and self-config.



Box-pushing 1988



Self-configurable robots (M-TRAN III) 2005



Kilobots (2011)

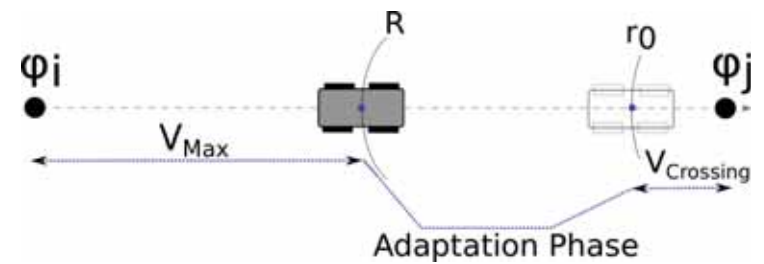
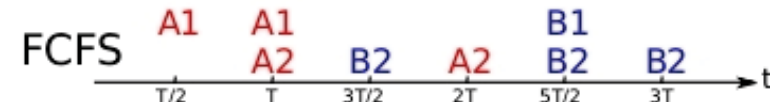
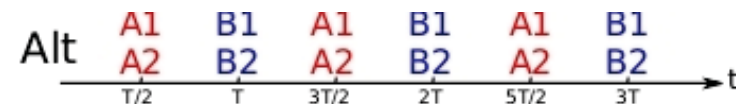
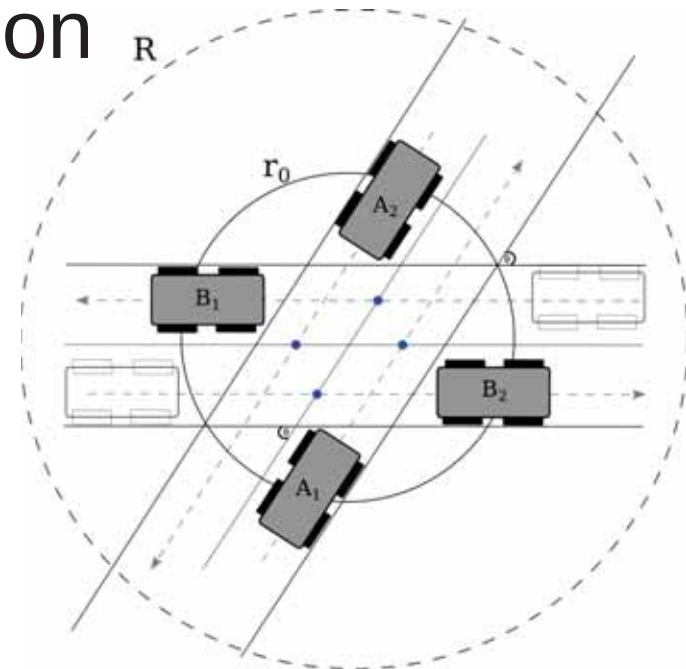


CollMot project (UAV **flocking**) Pennsylvania 2012

# Local coordination at intersection

## Non stop strategies

- First Come First Serve (FCFS) [Dresner Stone, 2005]
- **Alternate** [Tlig PhD, 2015]

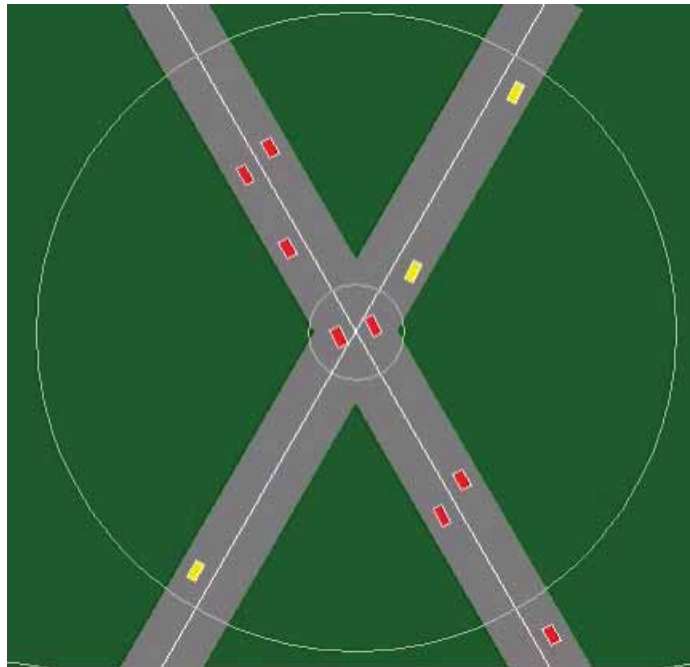
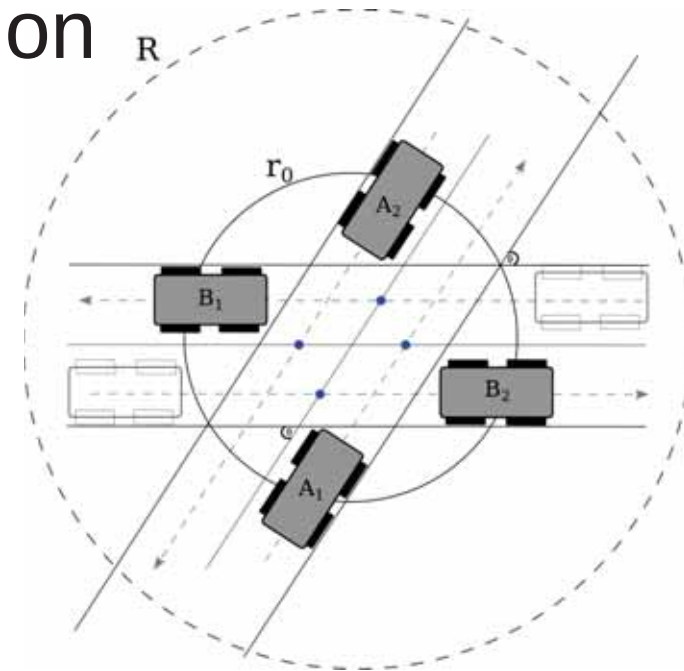




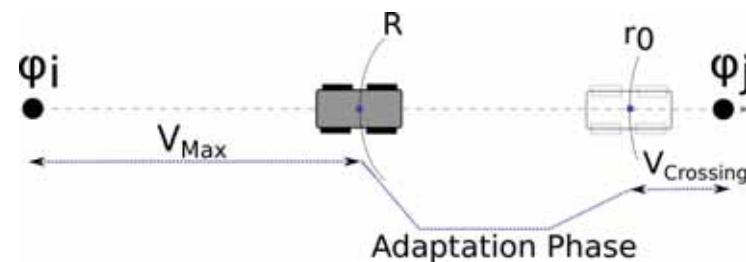
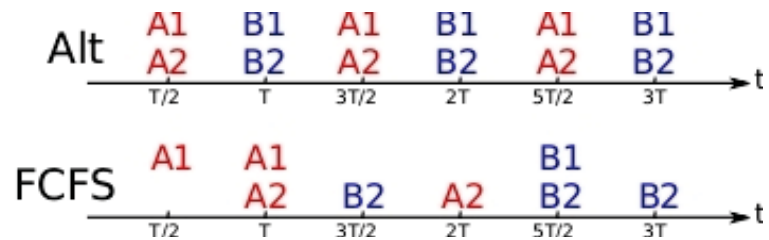
# Local coordination at intersection

## Non stop strategies

- First Come First Serve (FCFS) [Dresner Stone, 2005]
- **Alternate** [Tlig PhD, 2015]



Tlig, Buffet, Simonin, ECAI 2014



# Local coordination at intersection

## Cooperation between intersections

Decentralized (global) optimization

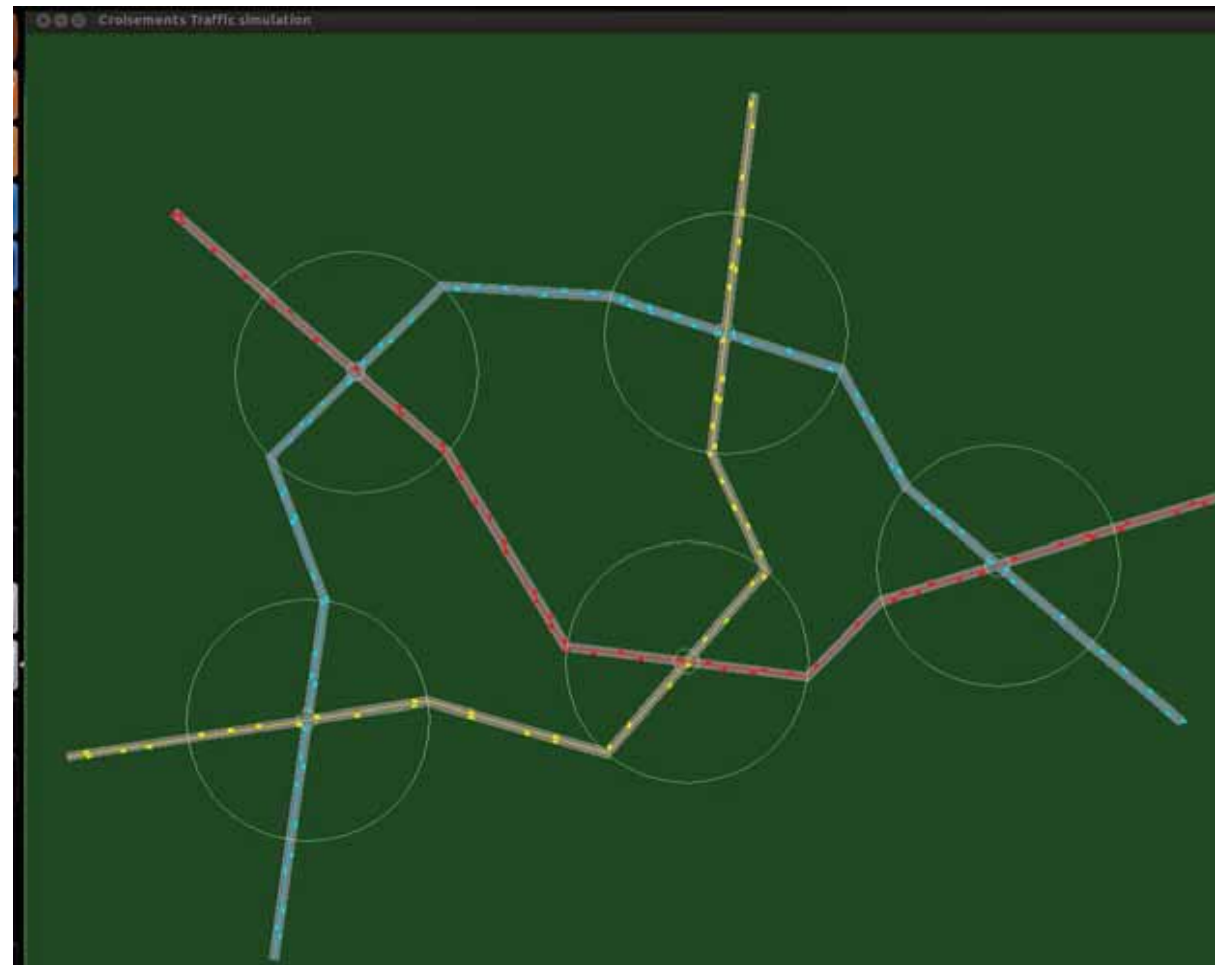
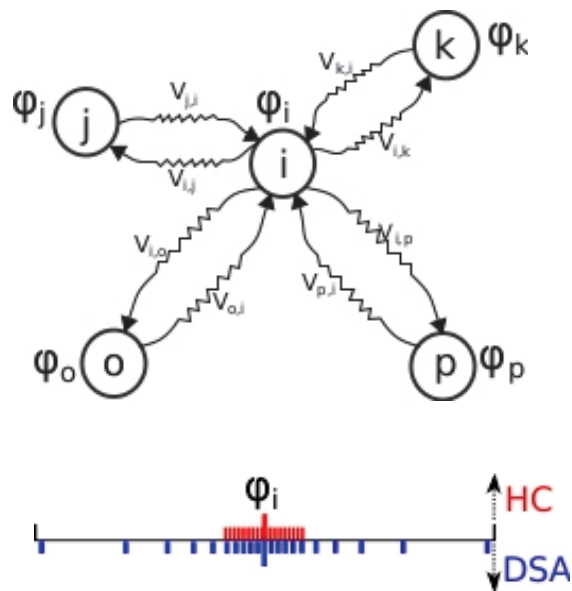
parameters : temporal phases  $\varphi_i$

Optimizing time / energy

Hill Climbing,  $\rho$ -DSA

→ emergence of **green waves**

→ **online adaptation** to traffic changes





# Outline

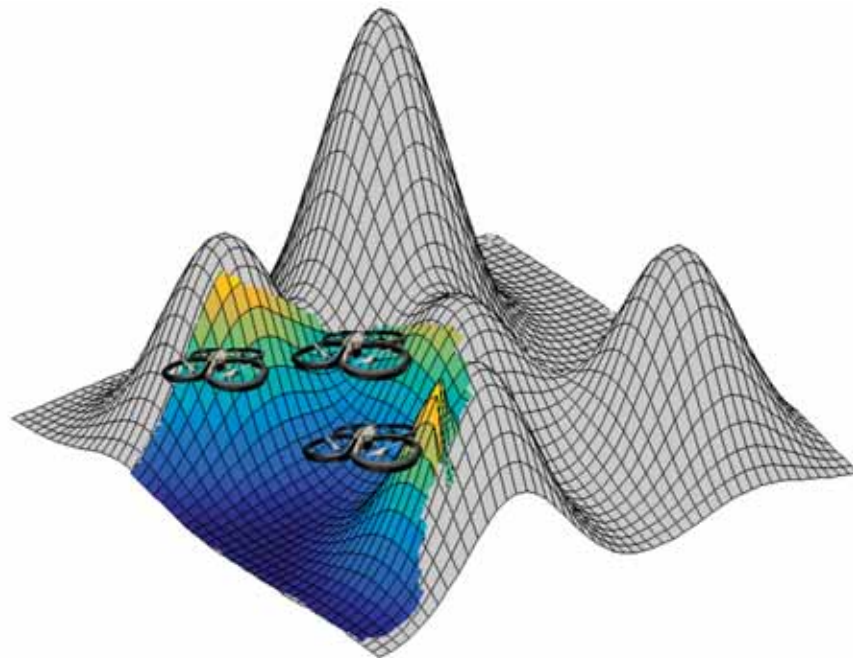
- I. Decision making ?
- II. Classical architectures
- III. Learning based architectures

---

- IV. Decision in multi-robot systems
- V. Strategies for multi-robot exploration

# 3D Mapping with a fleet of drones

A. Renzaglia, J. Dibangoye, O. Simonin

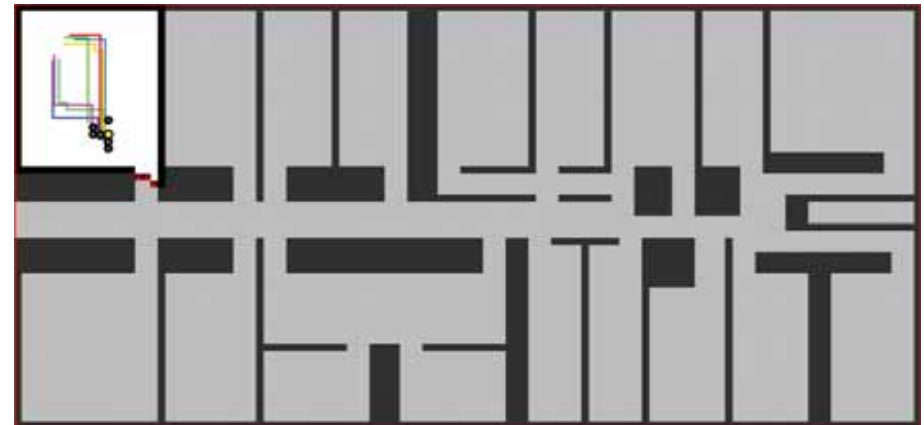
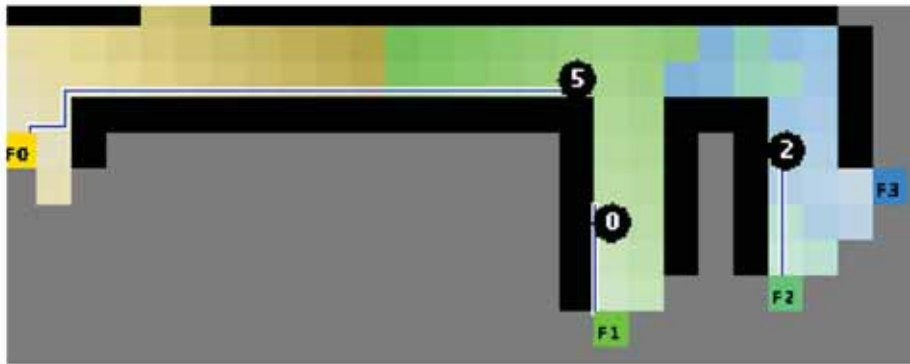




# Strategy of exploration: approaches and limits

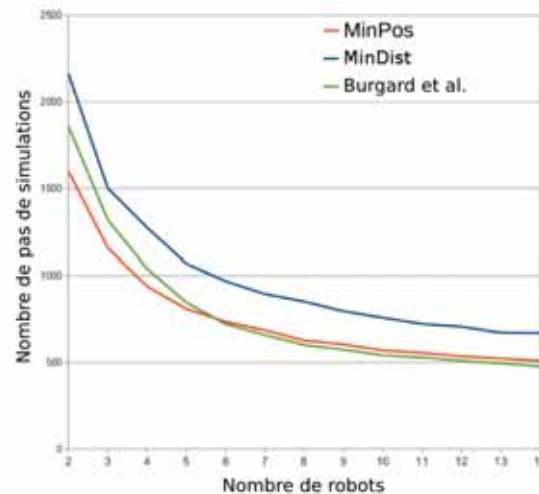
**Mapping relies on visiting frontiers** (known-unknown areas)

→ Repeat assignation robot-frontier :  $\min \sum_{(i,j)} \text{cost-Dist}(r_i, f_j)$   
[Yamauchi98] (mindist), [Burgard05] (greedy), [Bautin12] (minpos) ..



Multi-robot exploration : MinPos

[Bautin, Simonin, Charpillat, 2012], ANR Cartomatic



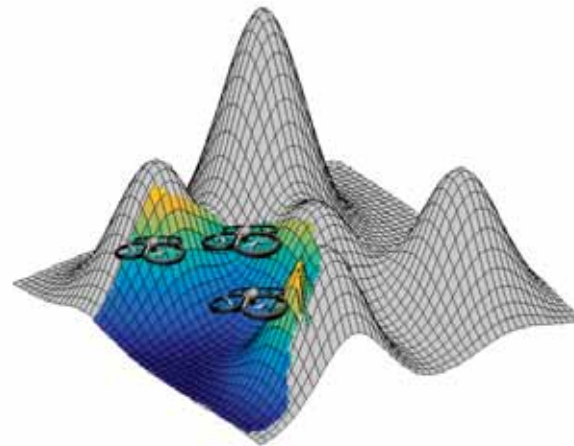
# 3D mapping : exploit optimal coverage

**Mapping relies on visiting frontiers** (known-unknown areas)

→ Repeat assignation robot-frontier :  $\min \sum_{(i,j)} \text{cost-Dist}(r_i, f_j)$   
[Yamauchi98] (mindist), [Burgard05] (greedy), [Bautin12] (minpos) ..

Sub-problem: **optimal coverage**

→ deploying robots such as **maximizing the observed area**



# 3D mapping : exploit optimal coverage

**Mapping relies on visiting frontiers** (known-unknown areas)

→ Repeat assignation robot-frontier :  $\min \sum_{(i,j)} \mathbf{cost-Dist}(r_i, f_j)$   
[Yamauchi98] (mindist), [Burgard05] (greedy), [Bautin12] (minpos) ..

Sub-problem: **optimal coverage**

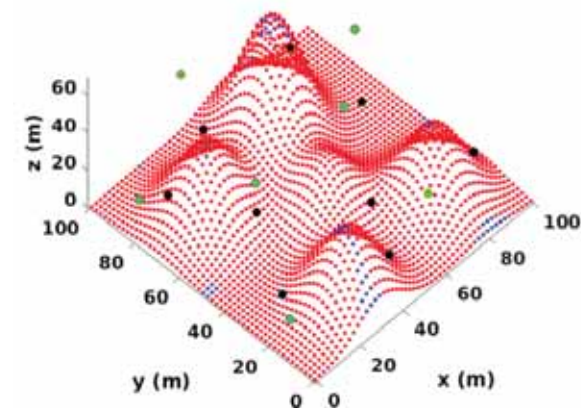
→ deploying robots such as **maximizing the observed area**

CAO (Cognitive-based Adaptive Optimization) [Renzaglia et al. 12]

**Local approx.** of the **objective** function :  $\hat{J}(x_1(t), .. x_N(t)) \leftarrow \mathbf{measures}$  (short T)

Move : **Stochastic search** on  $\hat{J}$

→ converge to a local optimum



# Combining local search and frontier-based app.

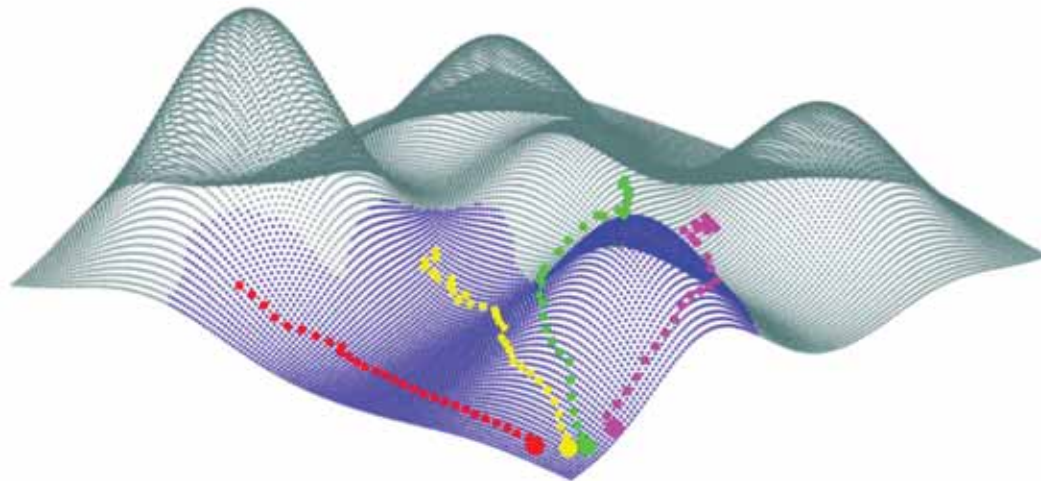
For each robot

Repeat

**Follow** local search

**When** a local minima is reached **Move** to the closest frontier

Until no more frontier



# Combining local search and frontier-based app.

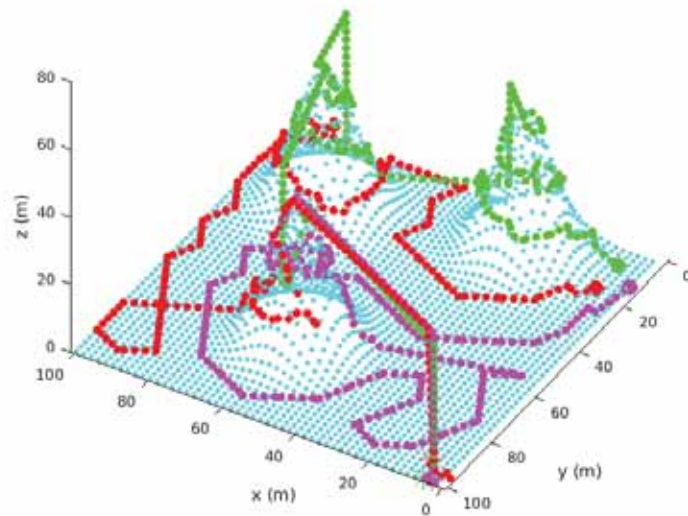
For each robot

Repeat

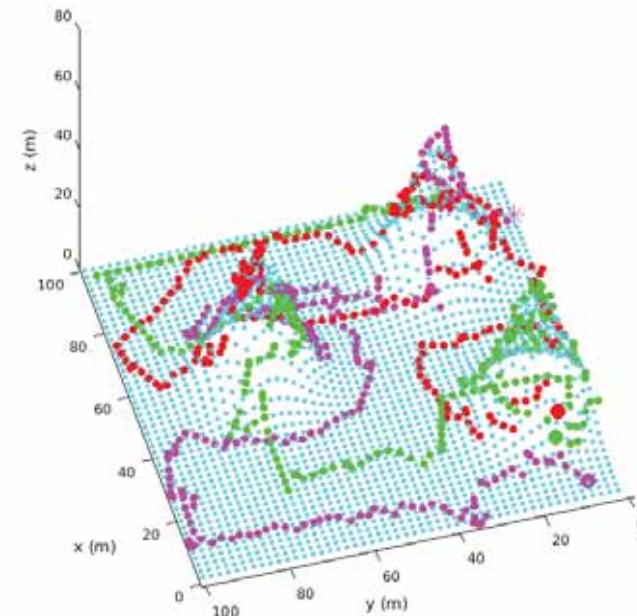
**Follow** local search

**When** a local minima is reached **Move** to the closest frontier

Until no more frontier



Only frontiers



Local search + frontiers



# Combining local search and frontier-based app.

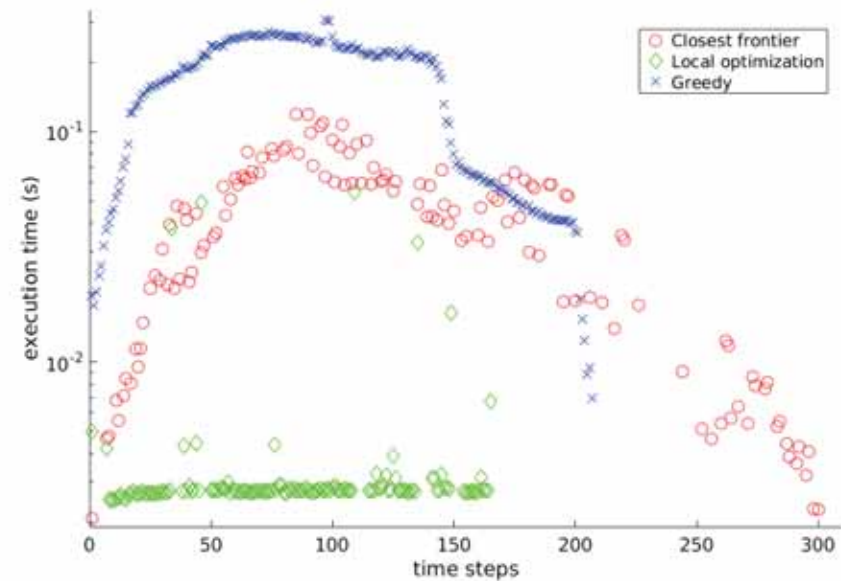
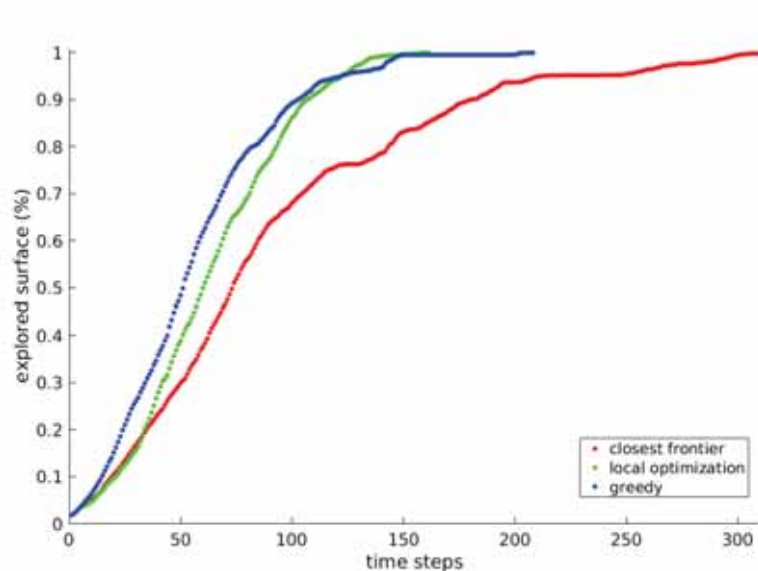
For each robot

Repeat

**Follow** local search

**When** a local minima is reached **Move** to the closest frontier

Until no more frontier



Thank you !



<https://team.inria.fr/chroma/>