

Motion planning

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Motion planning

Introduction

Definitions

Random Sampling

Collision testing

Software

Context

industrial robot



aerial vehicle



autonomous
vehicle



Autonomous mobile systems

- ▶ moving in an environment cluttered by obstacles
- ▶ possibly subject to kinematic or dynamic constraints

Motion planning : automatically compute a feasible collision-free path between two given configurations.

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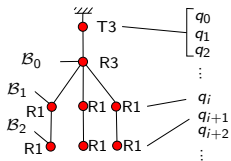
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Robot

Set of rigid bodies $\mathcal{B}_0, \dots, \mathcal{B}_m$, linked to one another by *joints*.

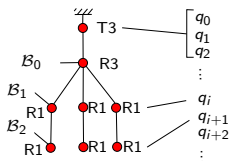


Joint : mobility of a body in the reference frame of its parent, parameterized by one or several numbers.



Robot configuration

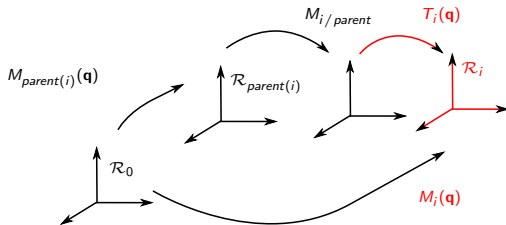
The configuration \mathbf{q} of a robot is represented by the concatenation of the parameters of each joint.



Forward kinematics

Computation of the position of each joint in world frame.

$$M_i(\mathbf{q}) = M_{parent(i)}(\mathbf{q}) M_{i/parent} T_i(\mathbf{q})$$



Definitions

- ▶ **Workspace** : $\mathcal{W} = \mathbb{R}^2$ or \mathbb{R}^3 : space in which the robot moves
- ▶ **Workspace obstacle** : compact subset of \mathcal{W} , denoted by \mathcal{O} .
- ▶ **Configuration space** : \mathcal{C} .
- ▶ **Position in configuration** \mathbf{q} of a point $M \in \mathcal{B}_i$: $\mathbf{x}_i(M, \mathbf{q})$.
- ▶ **Configuration space obstacle** :

$$\mathcal{C}_{obst} = \{ \mathbf{q} \in \mathcal{C}, \exists i \in \{1, \dots, m\}, \exists M \in \mathcal{B}_i, \mathbf{x}_i(M, \mathbf{q}) \in \mathcal{O} \text{ ou} \\ \exists i, j \in \{1, \dots, m\}, \exists M_i \in \mathcal{B}_i, \exists M_j \in \mathcal{B}_j, \\ \mathbf{x}_i(M_i, \mathbf{q}) = \mathbf{x}_j(M_j, \mathbf{q}) \}$$

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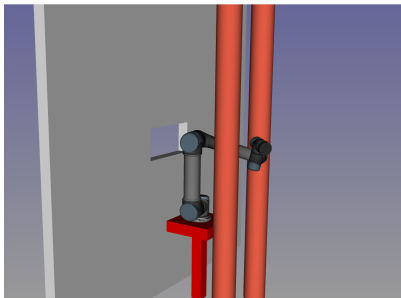
Motion

- ▶ Motion :
 - ▶ continuous mapping from $[0, 1]$ into \mathcal{C} .
- ▶ Collision free motion :
 - ▶ continuous mapping from $[0, 1]$ into \mathcal{C}_{free} .

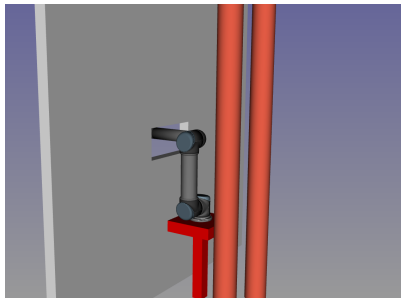
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Motion planning problem



initial configuration



goal configuration

$$\mathcal{C} = [-2\pi, 2\pi]^6$$

History

- ▶ before the 1990's : mainly a mathematical problem
 - ▶ Real algebraic geometry
 - ▶ Decidability : Schwartz and Sharir 1982
 - ▶ Tarski theorem, Collins decomposition
 - ▶ Approximate cell decomposition
- ▶ from the 1990's : an algorithmic problem
 - ▶ random sampling (1993)
 - ▶ asymptotically optimal random sampling (2011)

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Random sampling

- ▶ Random sampling motion planning methods appeared in the early 1990's
- ▶ Principle
 - ▶ sample random configurations
 - ▶ test whether they are collision-free
 - ▶ build a roadmap the nodes of which are the free configurations, and the edges of which are collision-free linear interpolations.

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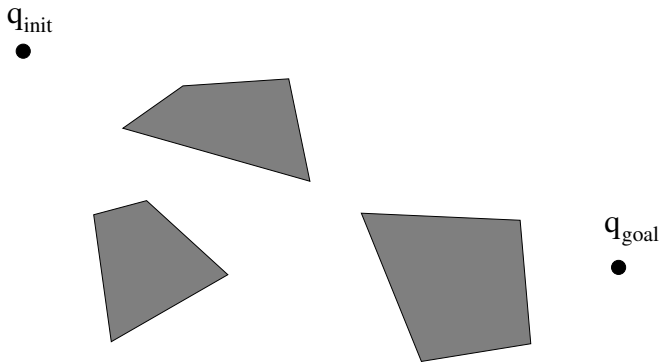
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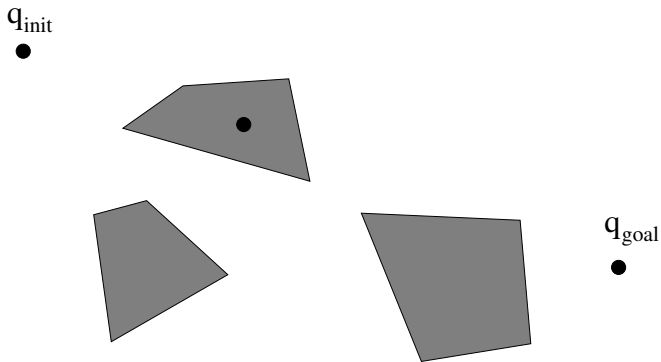
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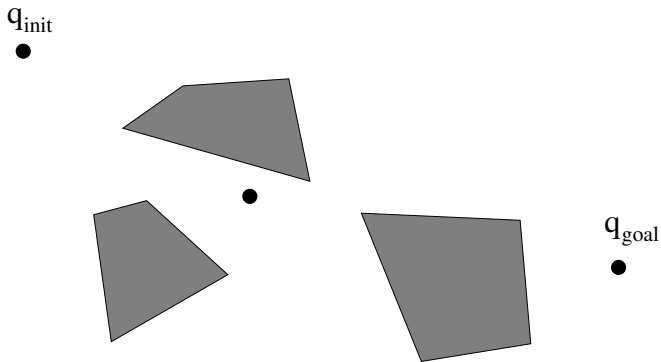
Probabilistic roadmap (PRM) 1994



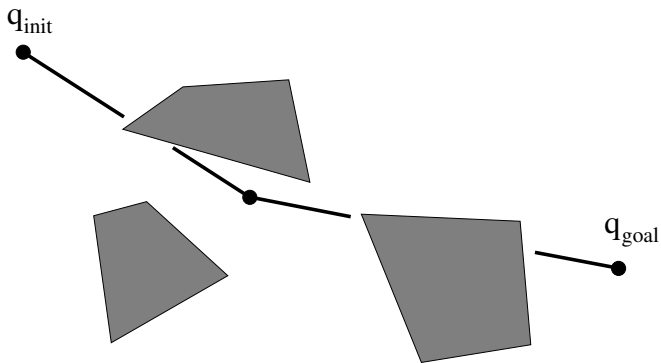
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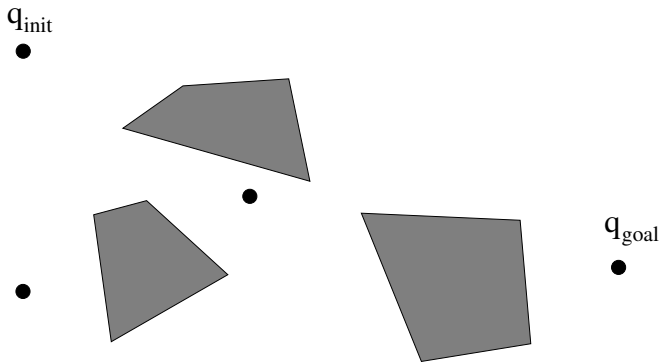
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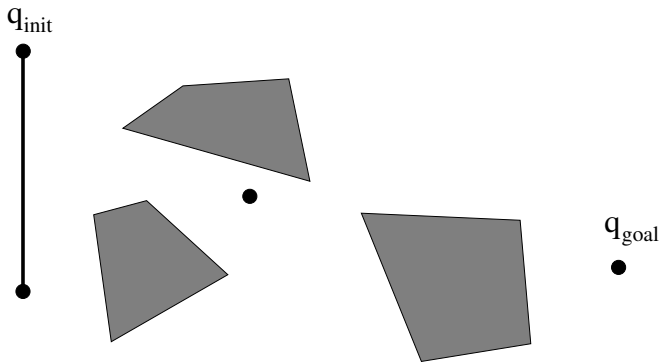
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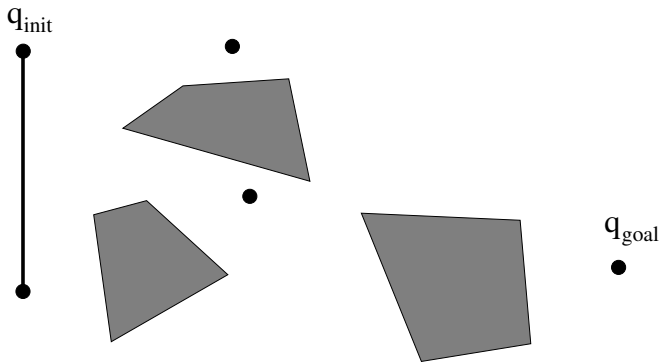
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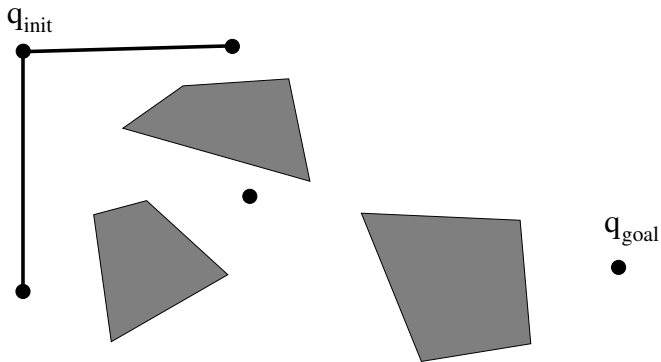
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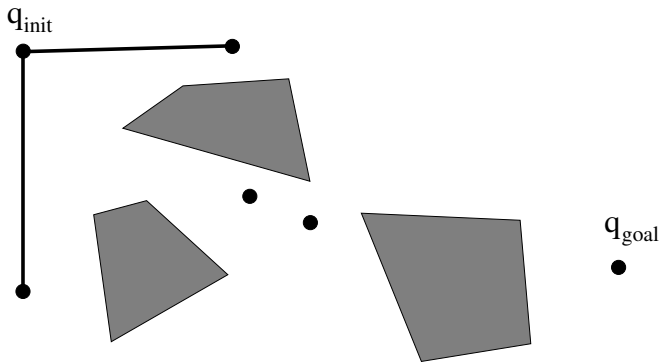
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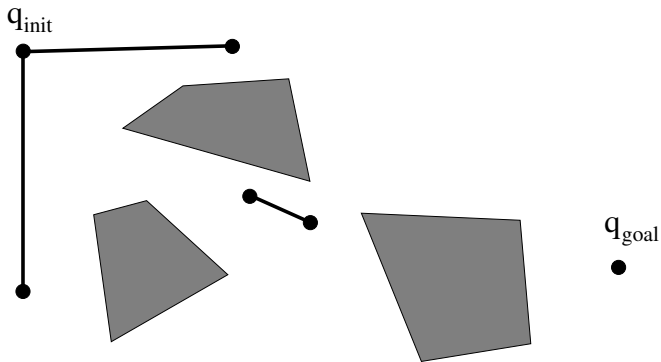
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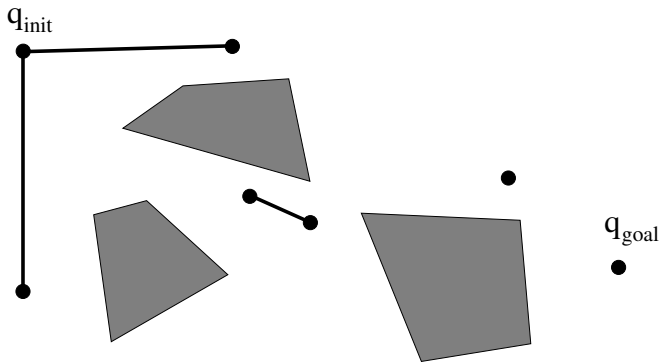
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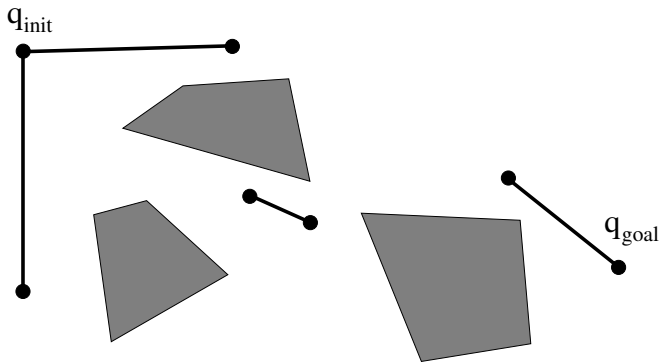
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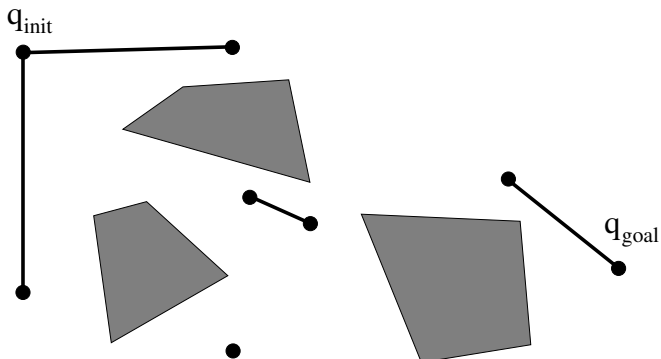
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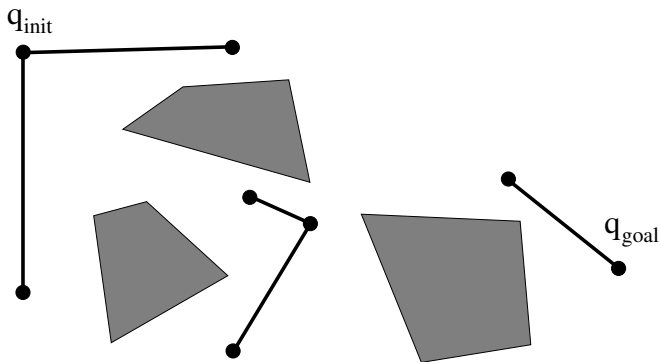
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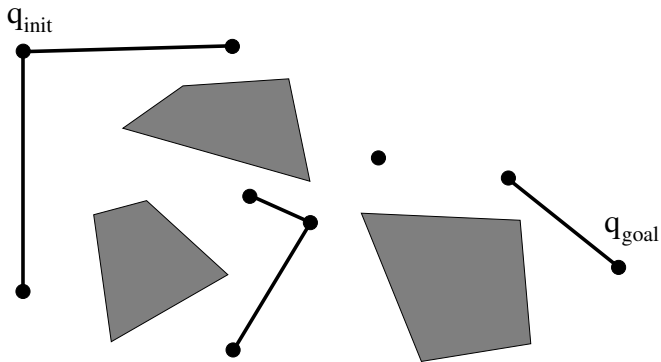
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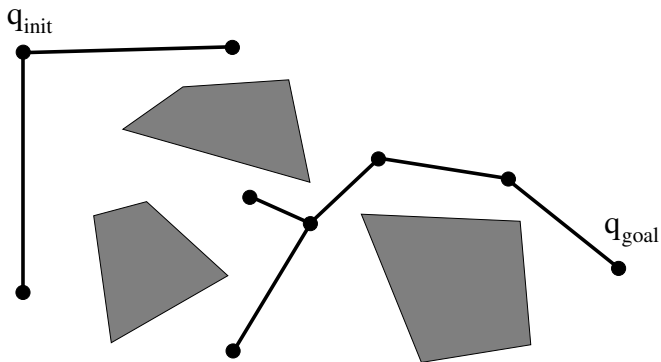
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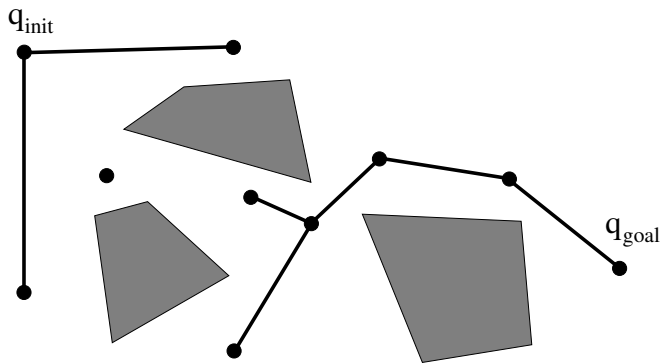
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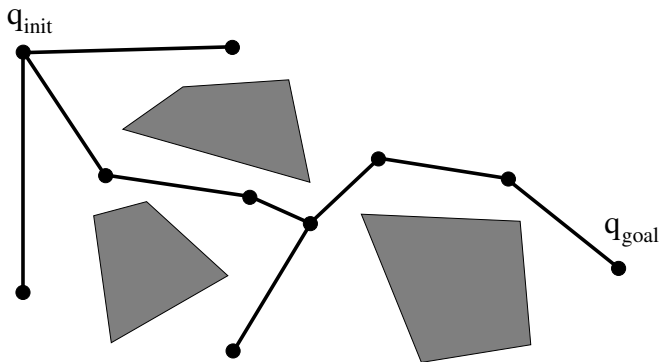
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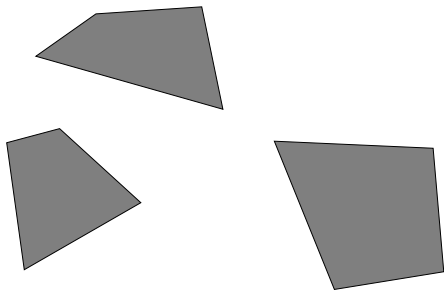


Probabilistic roadmap (PRM)

- ▶ Numerous useless nodes are created
 - ▶ this makes the connection of new nodes more time consuming
- ▶ Variant : visibility-based PRM
 - ▶ only *interesting* nodes are kept.

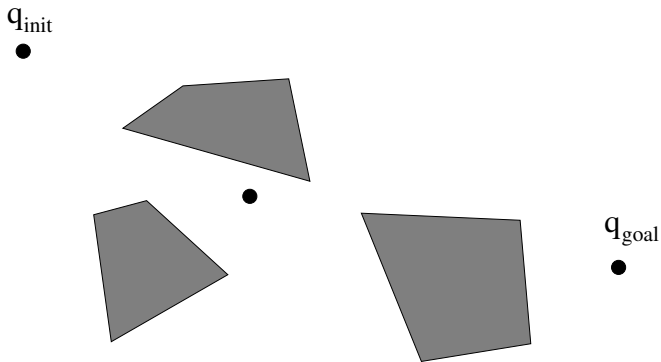
Visibility-based probabilistic roadmap (Visi-PRM) 1999

q_{init}
●

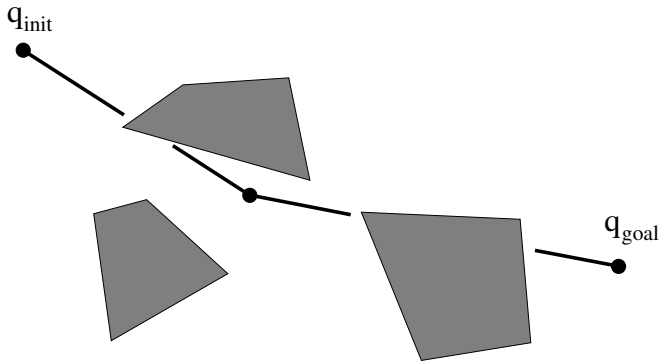


q_{goal}
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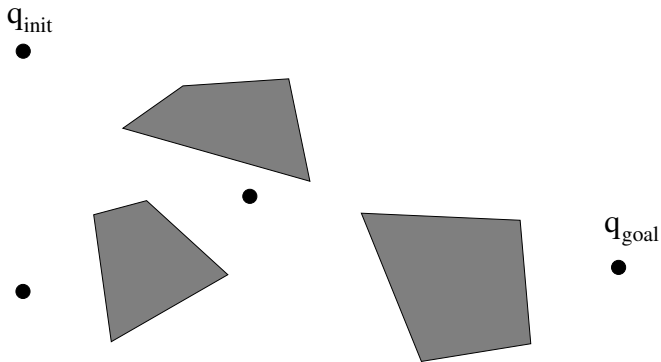
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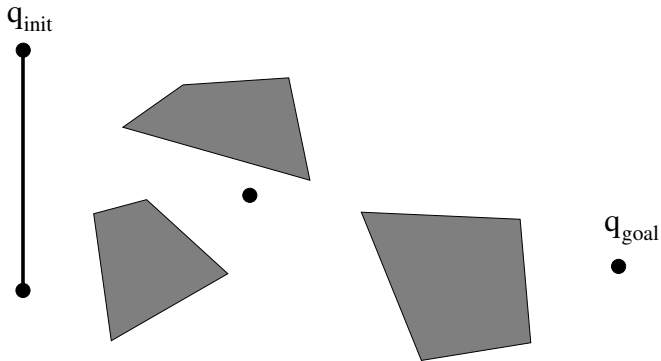
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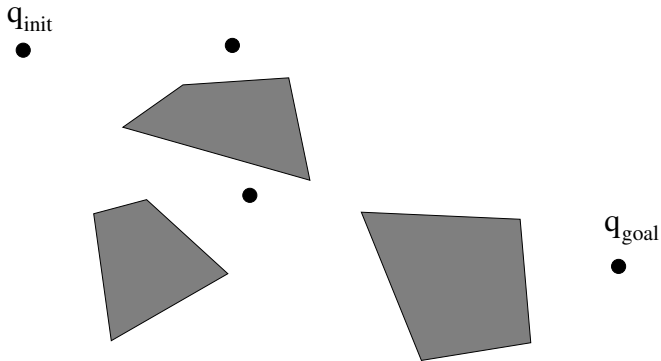
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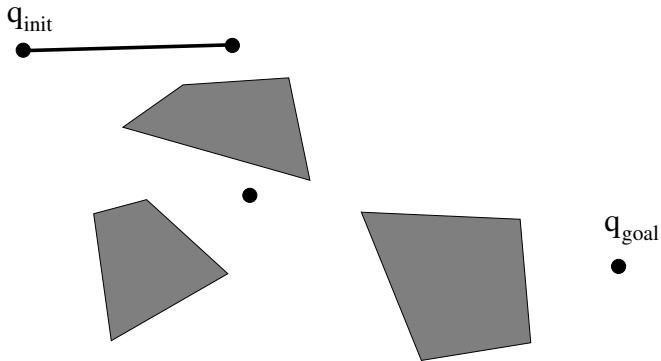
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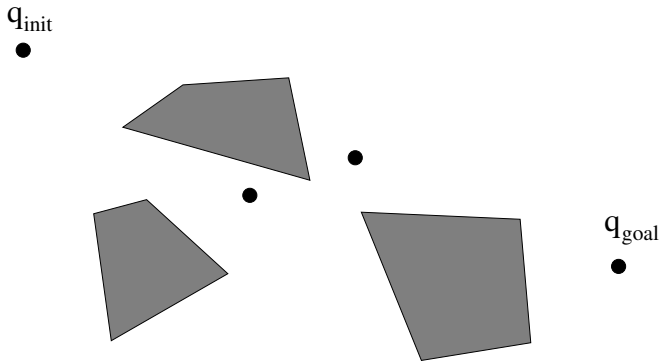
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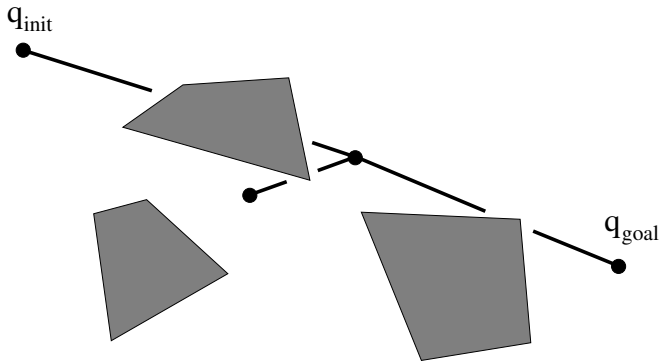
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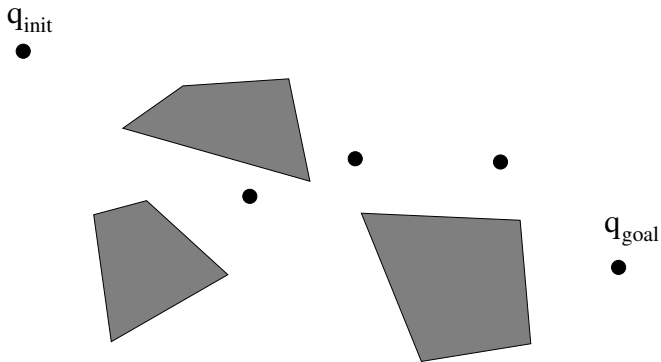
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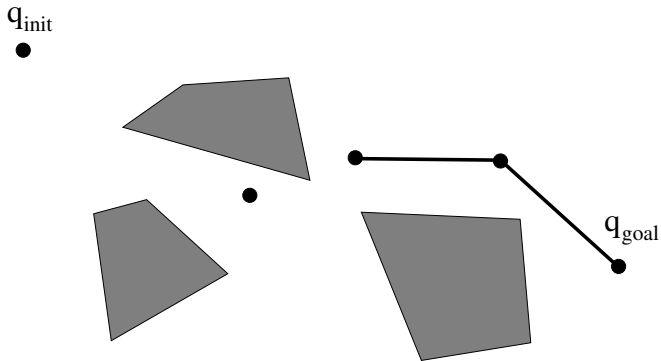
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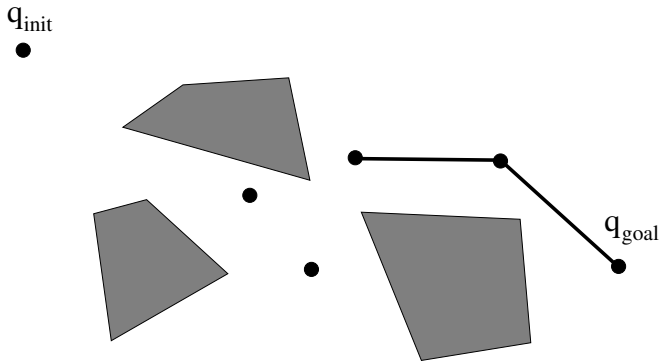
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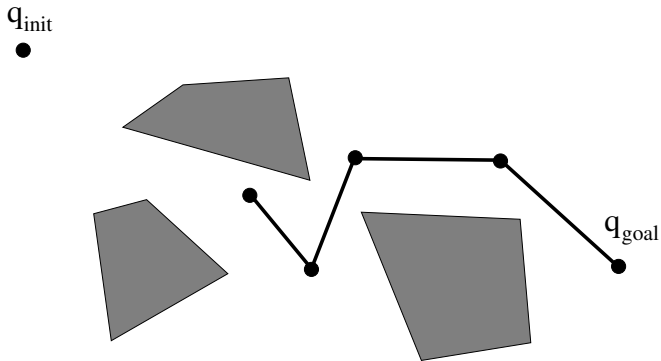
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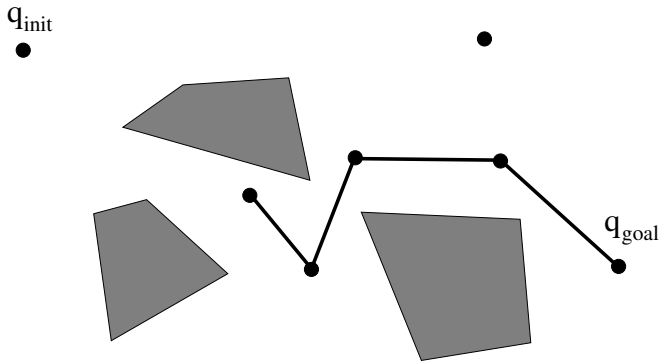
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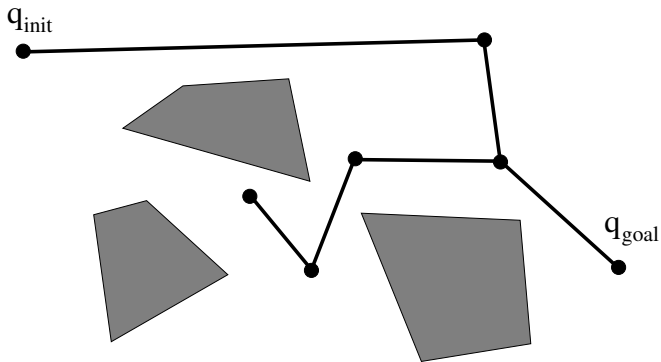
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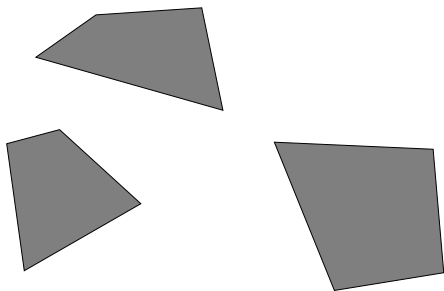


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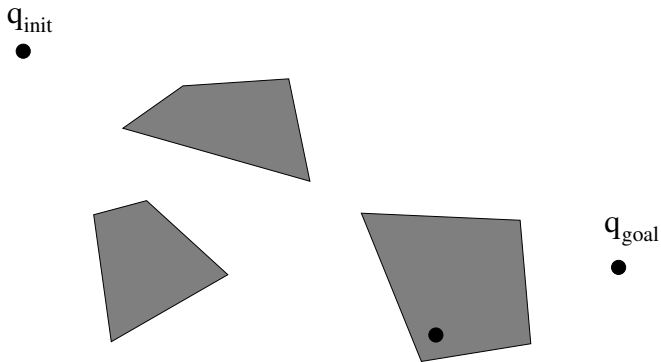
Rapidly exploring Random Tree (RRT) 2000

q_{init}
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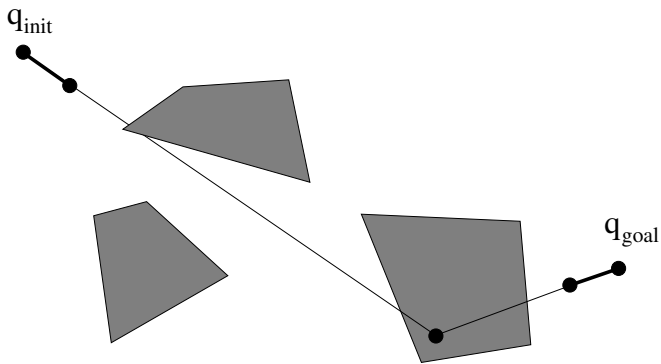


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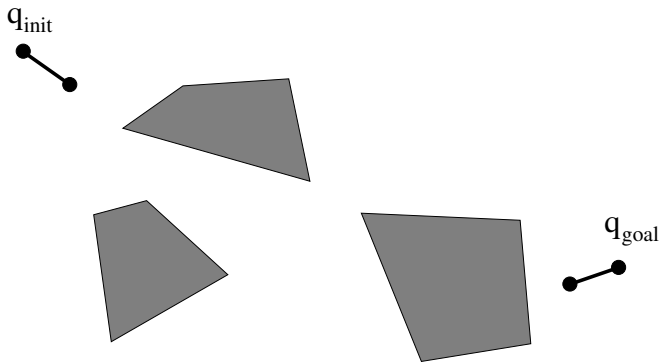
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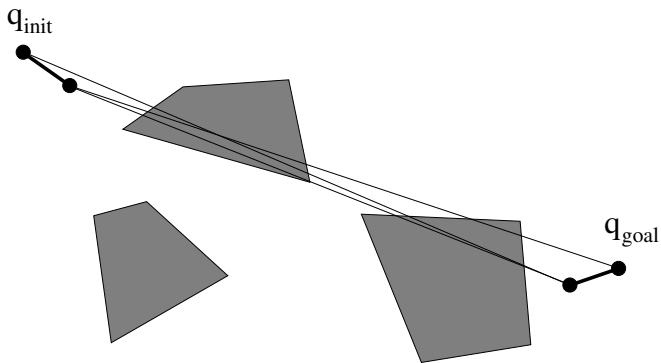
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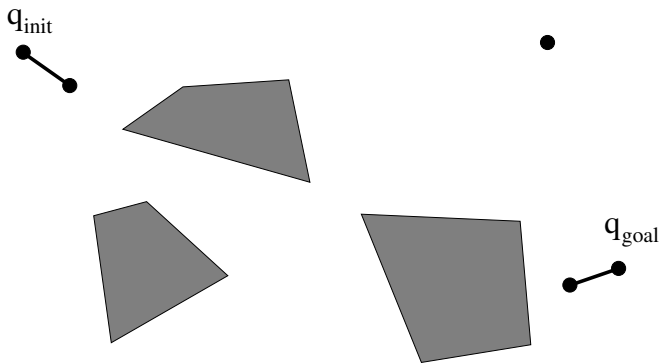
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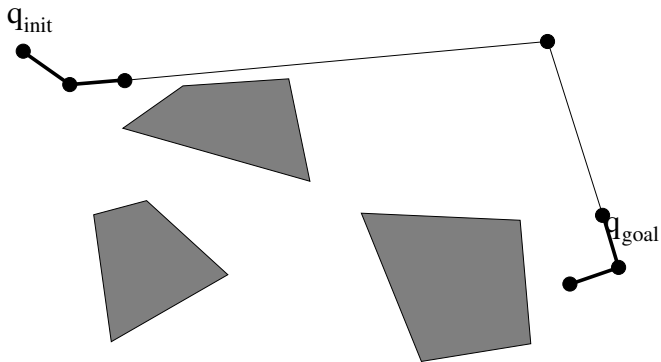
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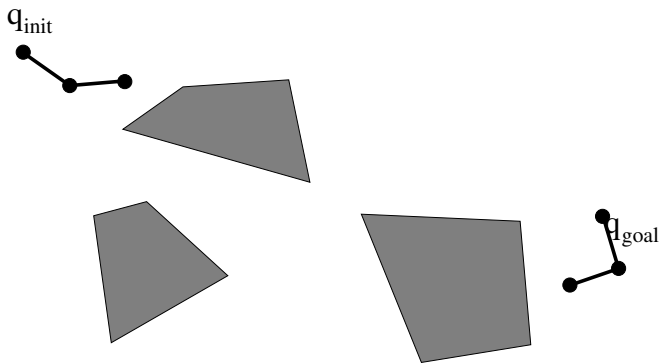
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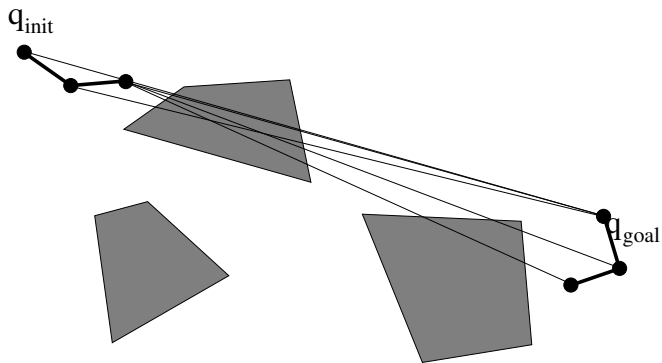
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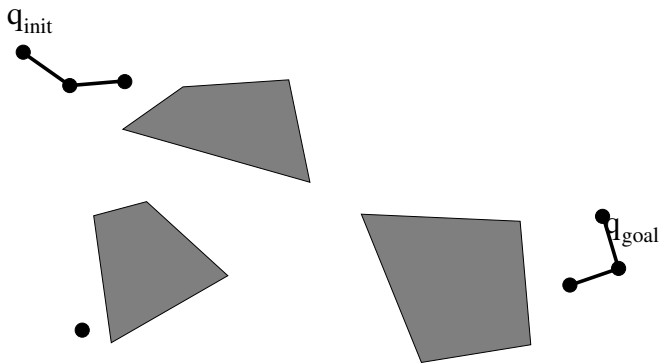
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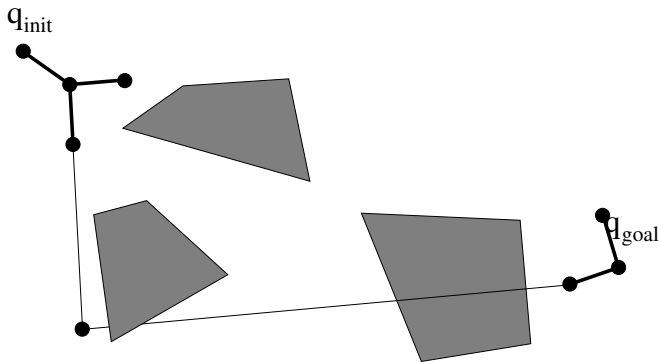
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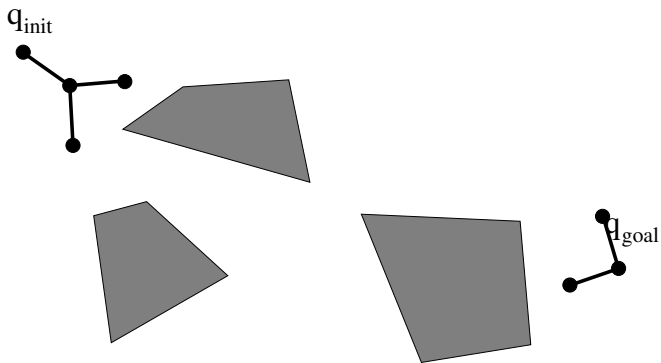
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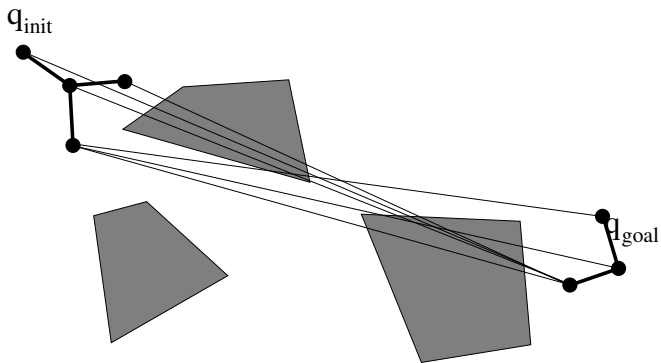
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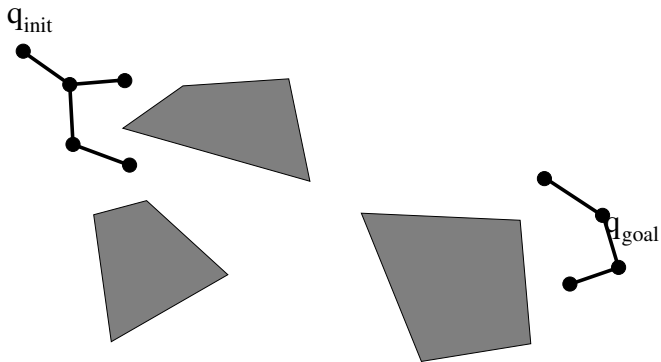
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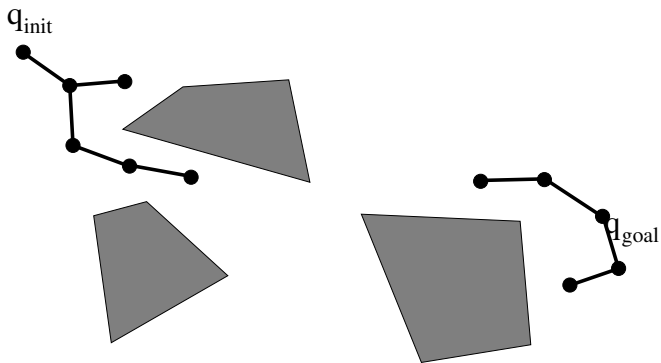
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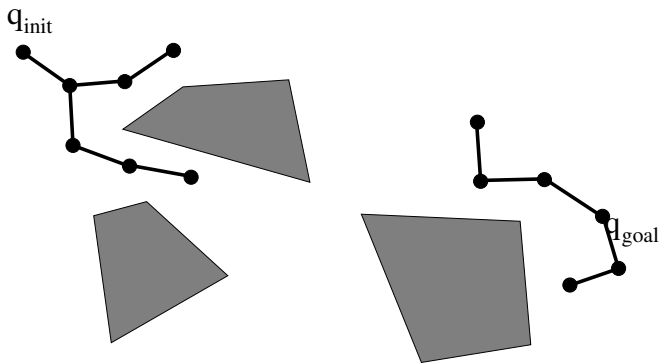
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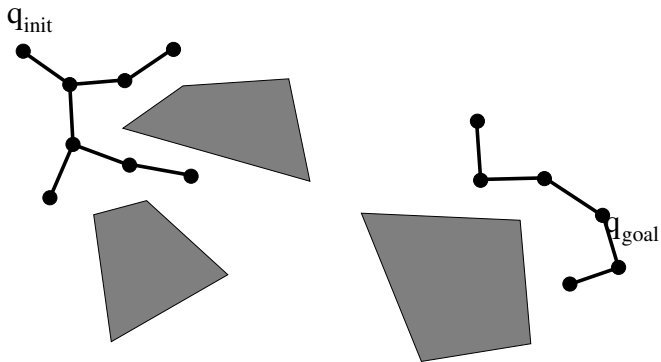
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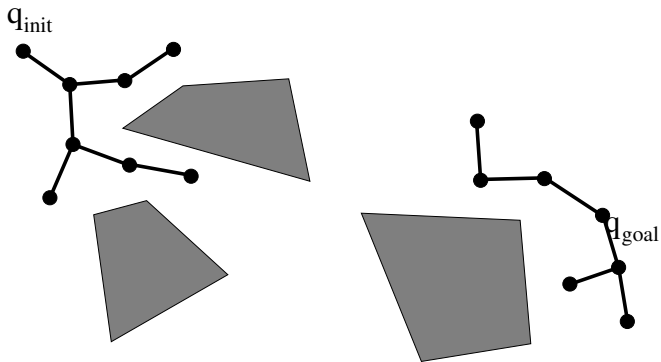
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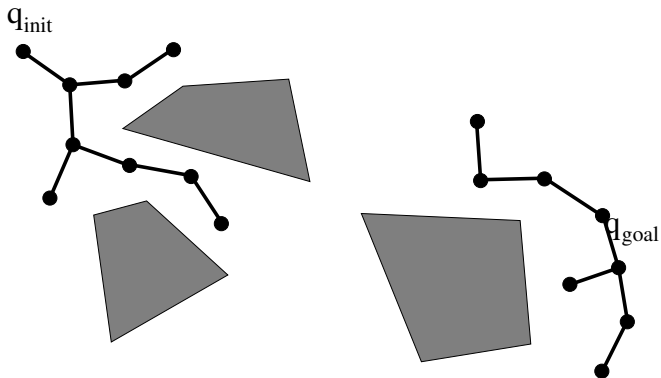
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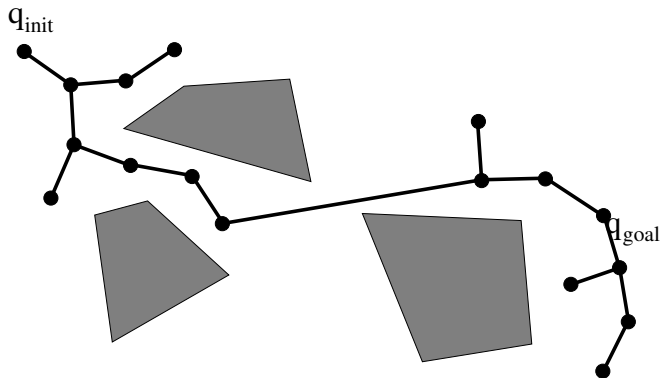
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Random sampling

- ▶ Pros :
 - ▶ no explicit computation of the configuration space
 - ▶ easy to implement,
 - ▶ robust.
- ▶ Cons :
 - ▶ no completeness, only *probrabilistic* completeness
 - ▶ difficult to find narrow passages.
- ▶ required operators :
 - ▶ collision checking
 - ▶ for configurations (static)
 - ▶ for linear interpolation (dynamic)

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Asymptotically optimal random sampling

Variants of PRM and RRT exist, and are asymptotically optimal :

- ▶ when the number of nodes tends to infinity,
- ▶ the solution computed by the algorithm tends to the optimal collision-free path.

PRM*

PRM

```

 $V \leftarrow \emptyset, E \leftarrow \emptyset$ 
for  $i \in \{0, \dots, n\}$  do
   $x_{rand} \leftarrow \text{SampleFree}_i$ 
   $U \leftarrow G.\text{Near}(x_{rand}, r)$ 
  for all  $u \in U$  in order of increasing  $\|u - x_{rand}\|$  do
    if  $x_{rand}$  and  $u$  in different
    connected components
    then
       $\text{TryConnect}(x_{rand}, u)$ 
    end if
  end for
end for

```

PRM*

```

 $V \leftarrow \text{SampleFree}_{i=1, \dots, n}, E \leftarrow \emptyset$ 
for  $v \in V$  do
   $U \leftarrow G.\text{Near}(x_{rand}, r^*) \setminus v$ 
  for all  $u \in U$  do
    if  $x_{rand}$  and  $u$  in different connected
    components then
       $\text{TryConnect}(v, u)$ 
    end if
  end for
end for
 $r^* = \gamma_{PRM} (\log(n)/n)^{\frac{1}{d}}$ 

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    end for
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```

kPRM*

PRM

```

V ← ∅, E ← ∅
for i ∈ {0, …, n} do
    xrand ← SampleFree;
    U ← G.Nearest(xrand, k)
    for all u ∈ U in order of increasing ||u - xrand|| do
        if xrand and u in different
        connected components then
            TryConnect (xrand, u)
        end if
    end for
end for
    
```

kPRM*

```

V ← SampleFreei=1, …, n, E ← ∅
for v ∈ V do
    U ← G.Nearest(xrand, k*) \ v
    for all u ∈ U do
        if xrand and u in different
        connected components then
            TryConnect (v, u)
        end if
    end for
end for
    
```

$k^* = k_{PRM} \log(n), k_{PRM} > e(1 + \frac{1}{d})$

kPRM*

PRM

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 $V \leftarrow \emptyset, E \leftarrow \emptyset$ 
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 $k^* = k_{PRM} \log(n), k_{PRM} > e(1 + \frac{1}{d})$ 
    
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PRM*, kPRM*

Note that :

- ▶ PRM*, kPRM* are not iterative anymore,
- ▶ making them iterative is not trivial.

Rapidly Exploring Random trees

There exists also asymptotically optimal variants of RRT

- ▶ RRG, RRT*

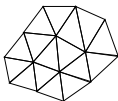
but they are specific to a given problem ($\mathbf{q}_{init}, \mathbf{q}_{goal}$).

Collision tests

- ▶ static : for configurations
 - ▶ problem : given
 - ▶ two rigid objects made of triangles
 - ▶ the relative position of one with respect to the other one
- determine whether they are colliding.

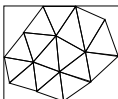
Bounding volume hierarchies

- ▶ binary tree of bounding volumes such that
 - ▶ each node has two children,
 - ▶ leaves are triangles.



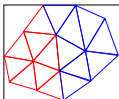
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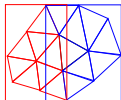
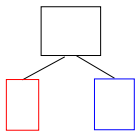
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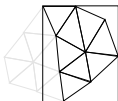
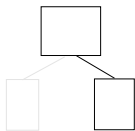
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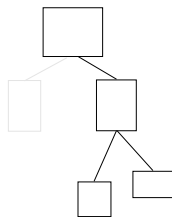
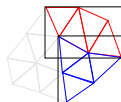
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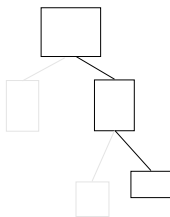
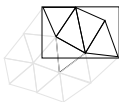
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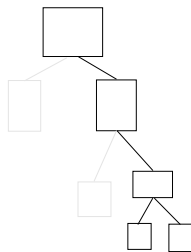
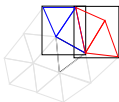
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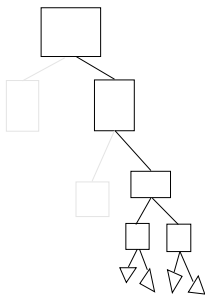
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Bounding volume hierarchies

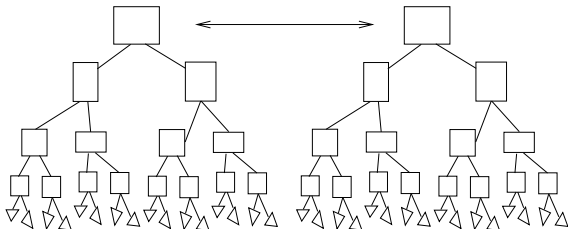
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Collision testing for configurations

► Algorithm

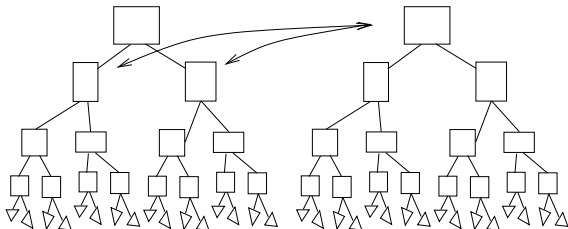
- test root nodes of each tree,
- if two bounding volumes collide, test one with the children of the other one.



Collision testing for configurations

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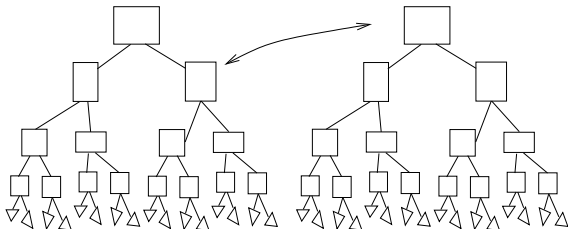
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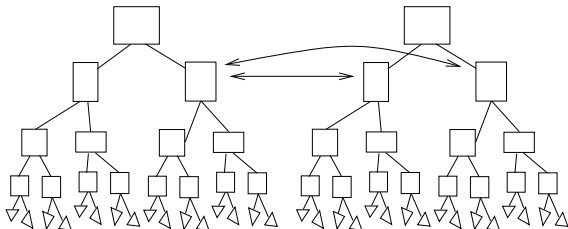
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Collision testing for configurations

► Algorithm

- test root nodes of each tree,
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Open source software platform

Several open-source platforms for motion planning are available

- ▶ OMPL (Rice University)
 - ▶ no kinematic chain,
 - ▶ no collision checking.
- ▶ Openrave (CMU)
- ▶ MoveIt (ROS)
 - ▶ Integration in ROS of
 - ▶ fcl (collision checking), KDL (kinematic chain)
- ▶ Humanoid Path Planner
 - ▶ numerical constraints (quasi-static equilibrium)
 - ▶ advanced manipulation planning

Humanoid Path Planner

<https://humanoid-path-planner.github.io/hpp-doc>