

# The problem - The vision



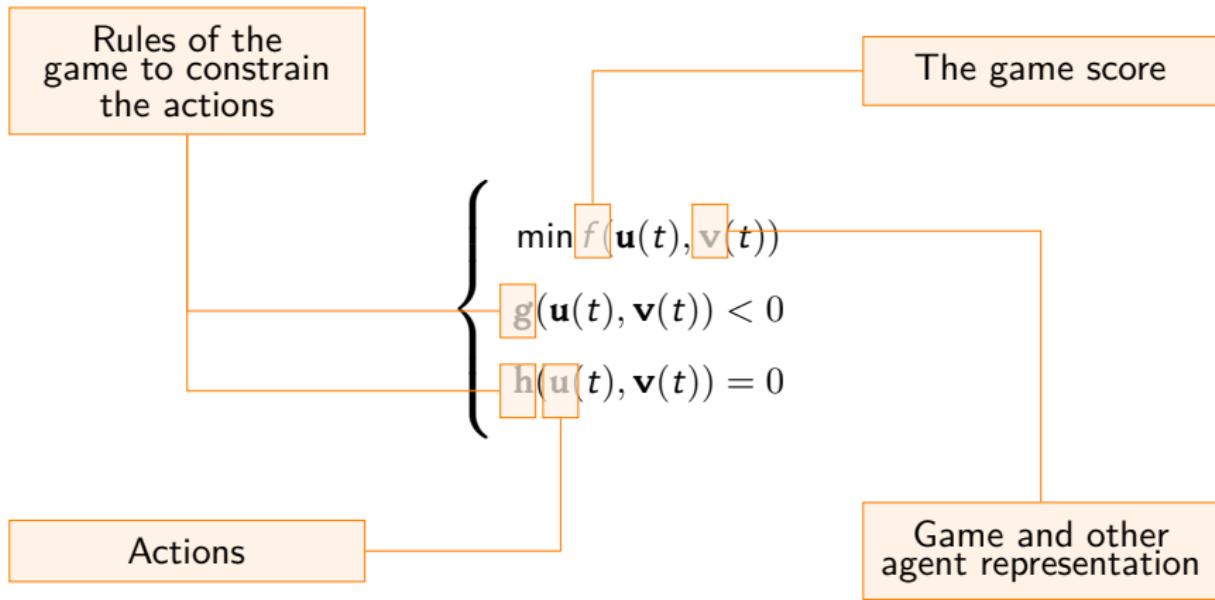
**Problem 1:** Variability according to the customers

**Problem 2:** Variability in the realization (humans)

**Problem 3:** Variability in the delivery

**Problem 4:** Collaboration with humans

**Problem 5:** Certification



What are the necessary and meaningful constraints ?

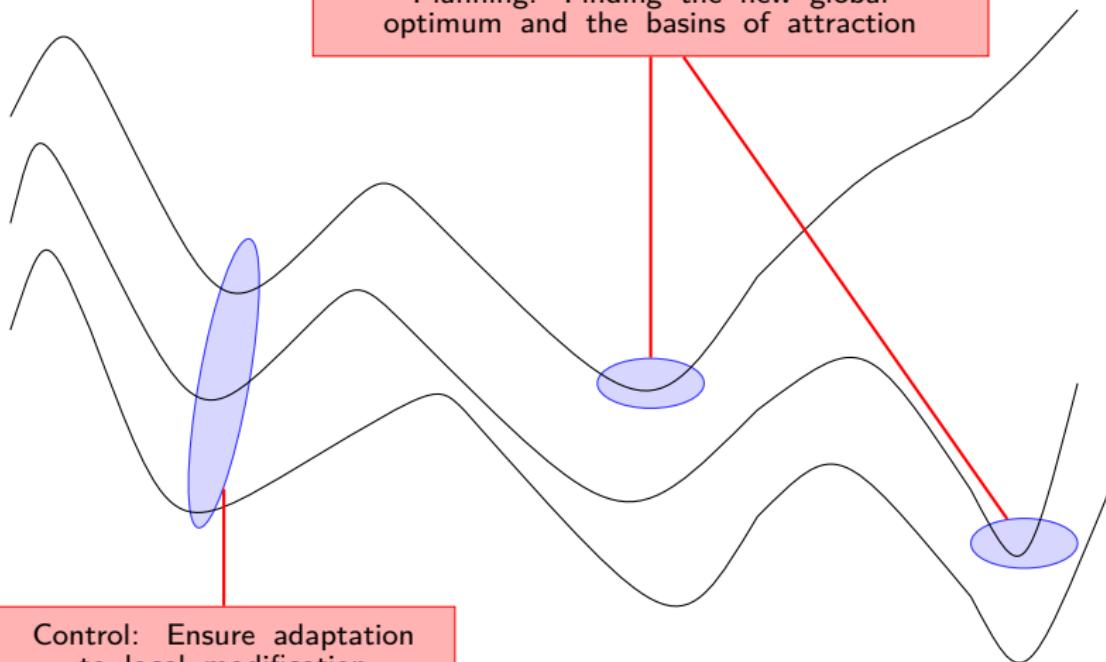
How to build the cost function for the behavior of interest ?

How to deal with such a huge search space ?

How to build an efficient world representation ?

$$\left\{ \begin{array}{l} \min f(\mathbf{u}(t), \mathbf{v}(t)) \\ g(\mathbf{u}(t), \mathbf{v}(t)) < 0 \\ h(\mathbf{u}(t), \mathbf{v}(t)) = 0 \end{array} \right.$$

Planning: Finding the new global optimum and the basins of attraction



Control: Ensure adaptation  
to local modification

$$\left\{ \begin{array}{l} \min f(\mathbf{u}(t), \mathbf{v}(t)) \\ \mathbf{g}(\mathbf{u}(t), \mathbf{v}(t)) < 0 \\ \mathbf{h}(\mathbf{u}(t), \mathbf{v}(t)) = 0 \end{array} \right.$$

[Saidi,IROS 2007]

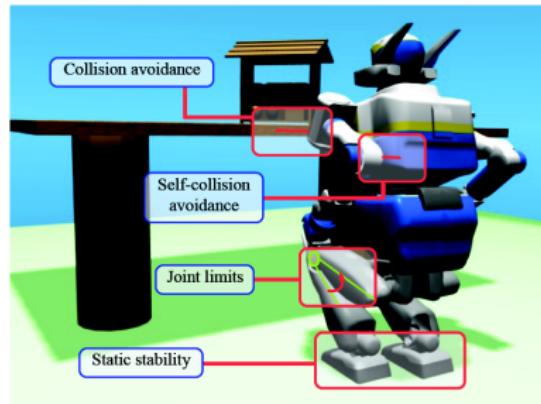
$\mathbf{f}(t)$ : The cost function

$\mathbf{u}(t)$ : The control vector

$\mathbf{g}(t)$ : The inequality constraints

$\mathbf{h}(t)$ : The equality constraints

$\mathbf{v}(t)$ : The environment representation



$$\left\{ \begin{array}{l} \min_{\mathbf{q}(\cdot), \mathbf{u}(\cdot)} \int_0^T L(t, \mathbf{q}(t), \mathbf{u}(t)) dt \\ \dot{\mathbf{q}}(t) = f(\mathbf{q}(t), \mathbf{u}(t)), \quad t \in [0, T] \\ \mathbf{q}(0) = \mathbf{q}_0, \quad T > 0 \\ 0 \leq \mathbf{g}\mathbf{h}(\mathbf{q}(t), \mathbf{u}(t)), \quad t \in [0, T] \end{array} \right.$$

[Saidi,IROS 2007]

**f:** The system dynamics

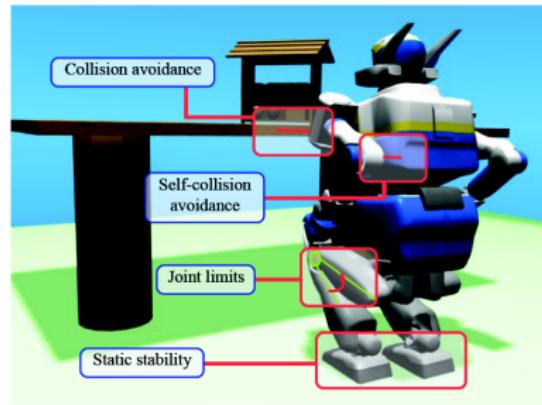
**u:** The control vector

**q:** The system state

**gh:** The (in)equality constraints

**v:** The environment representation

**L:** The cost



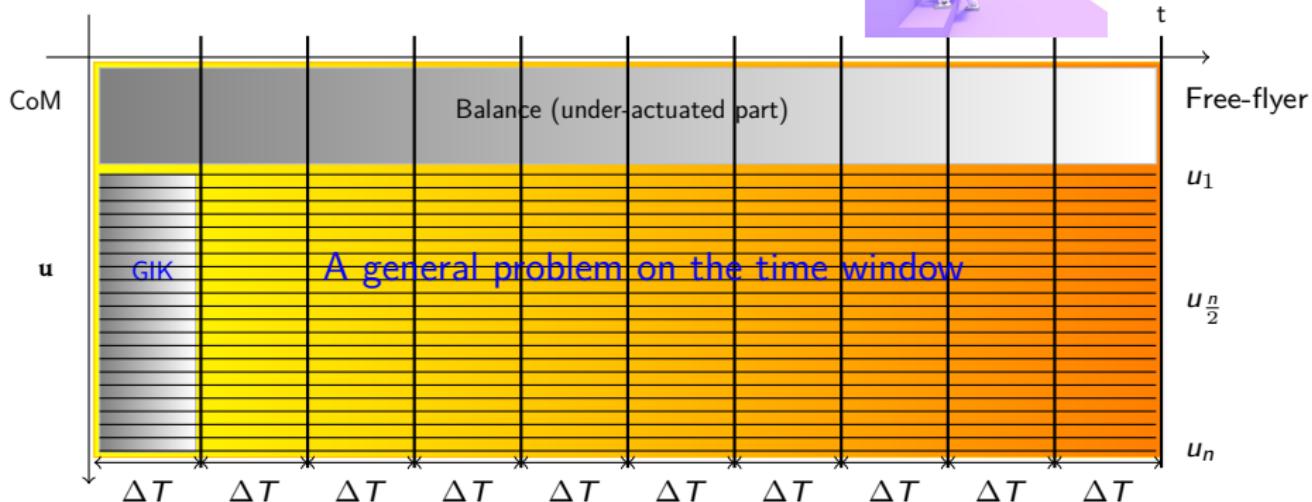
- Size of the problem

$$1.6 \times 200 \times 30 = 9600 \text{ variables}$$



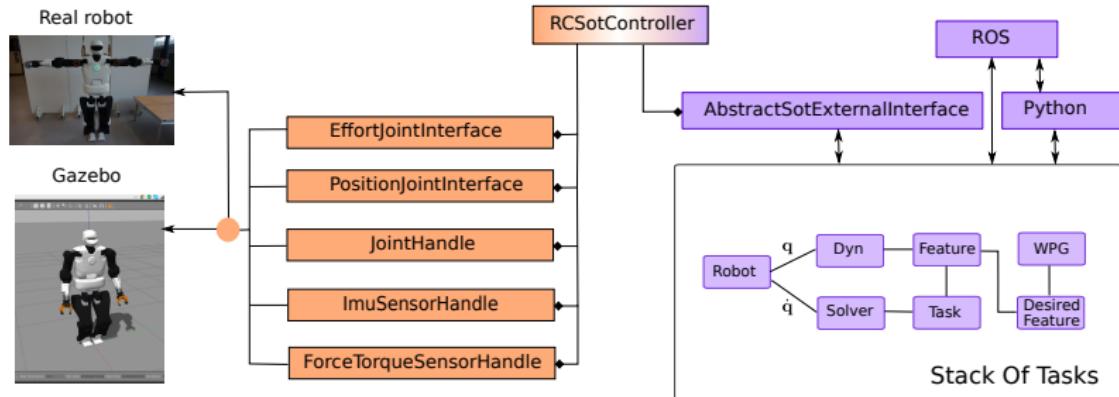
- Non linear constraints

- Discrete nature due to contacts

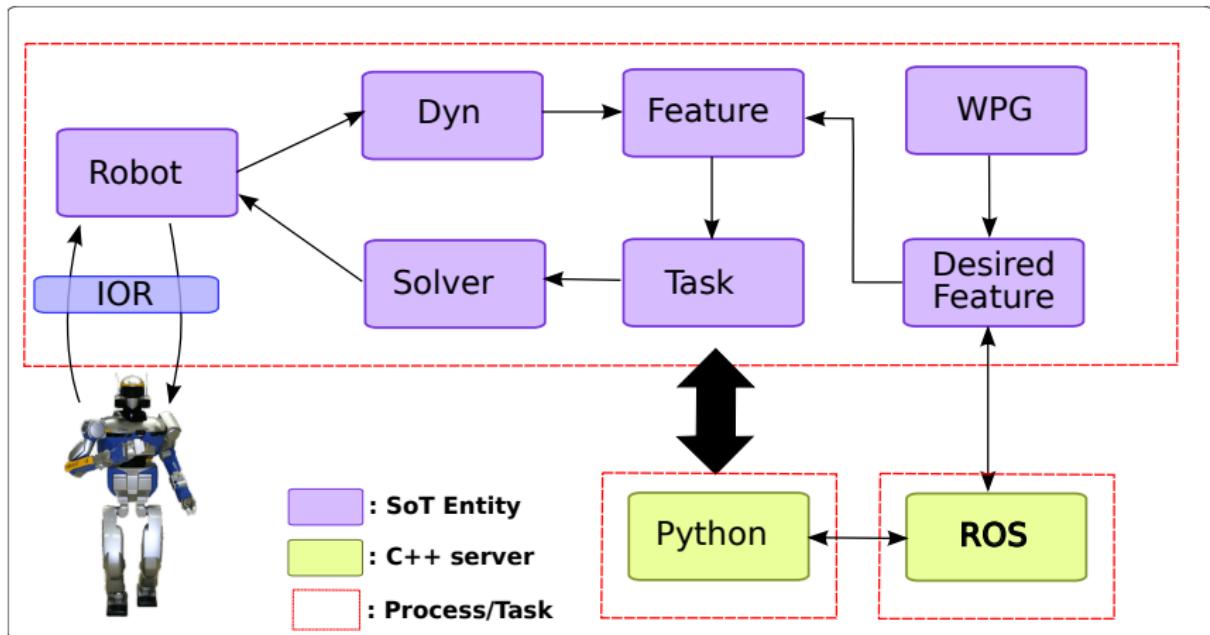


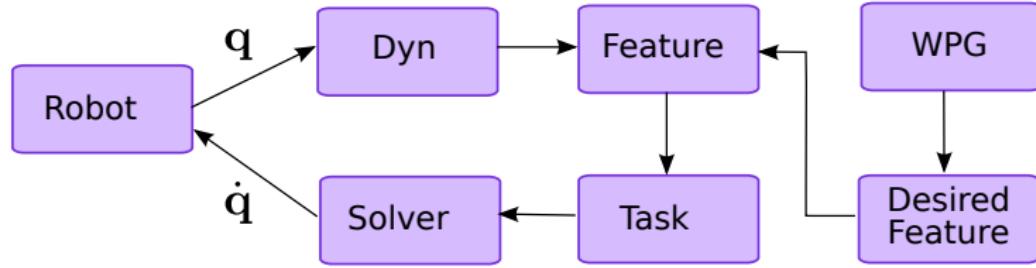
<https://www.youtube.com/watch?v=WbsQBPzQakc>

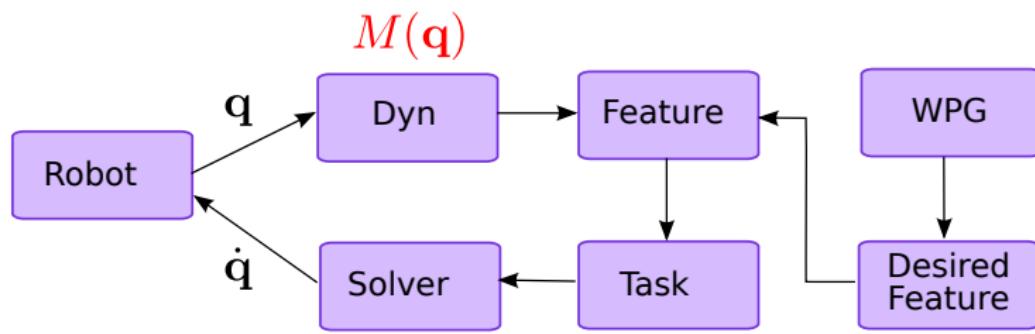
# Structure de l'encapsulation

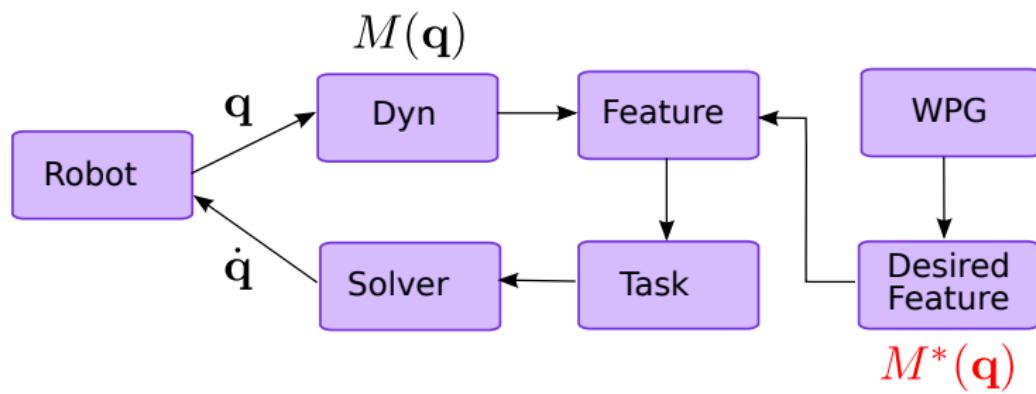


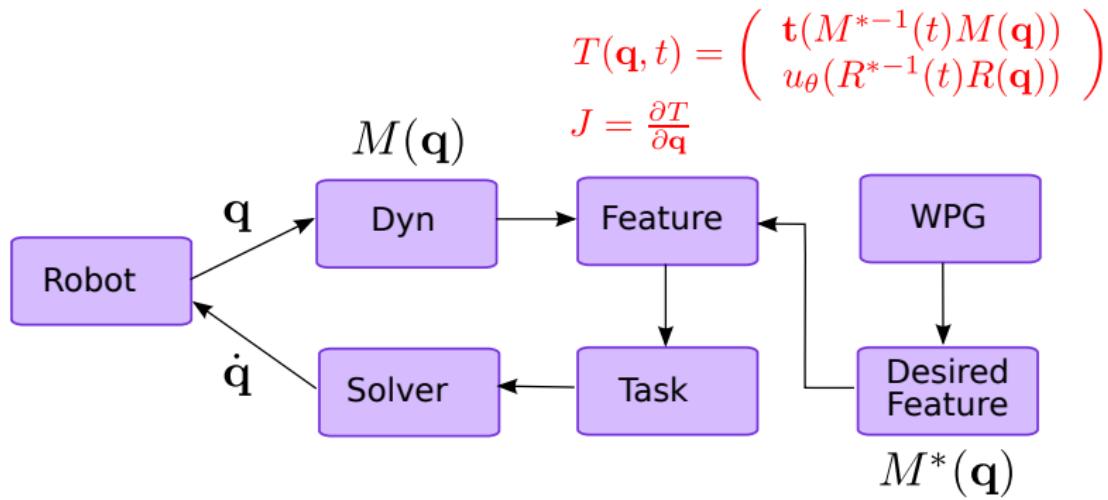
## Software structure - Conceptual view



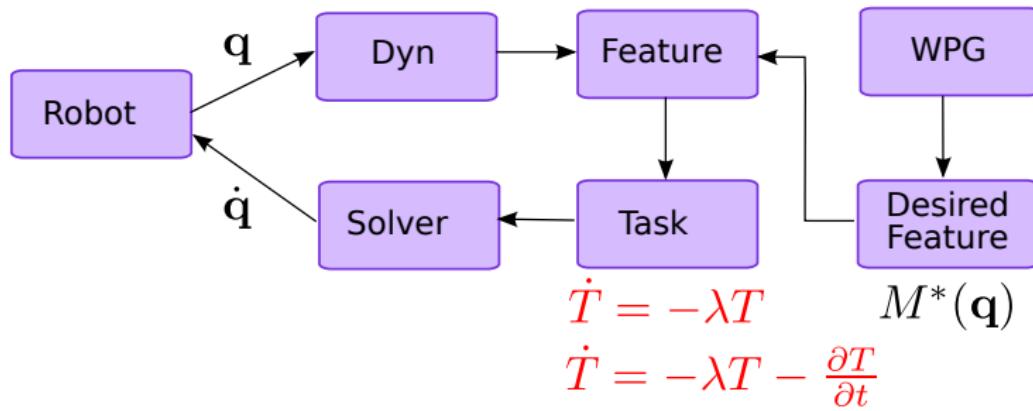




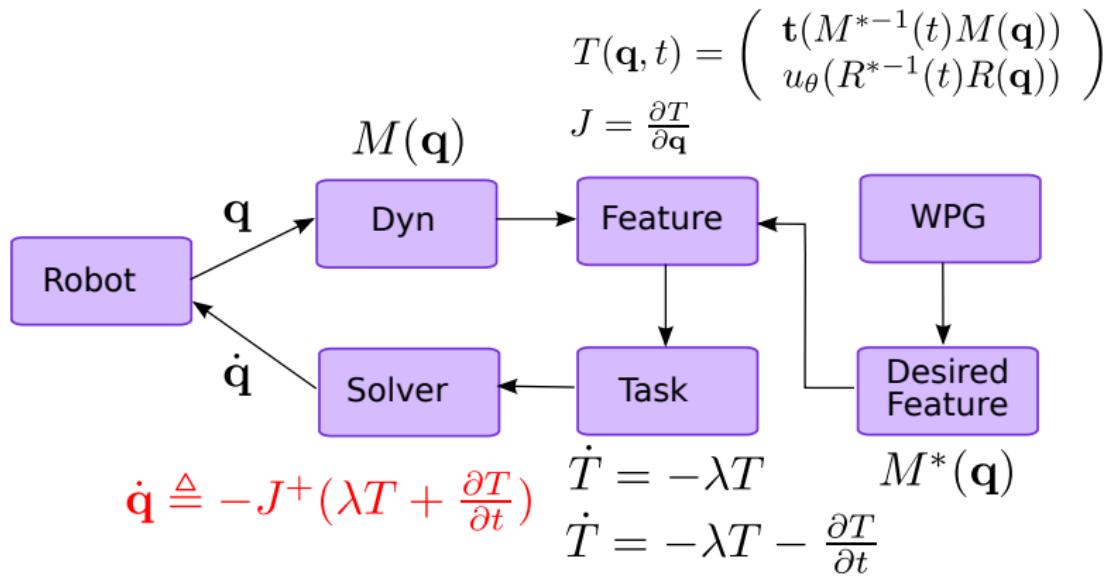


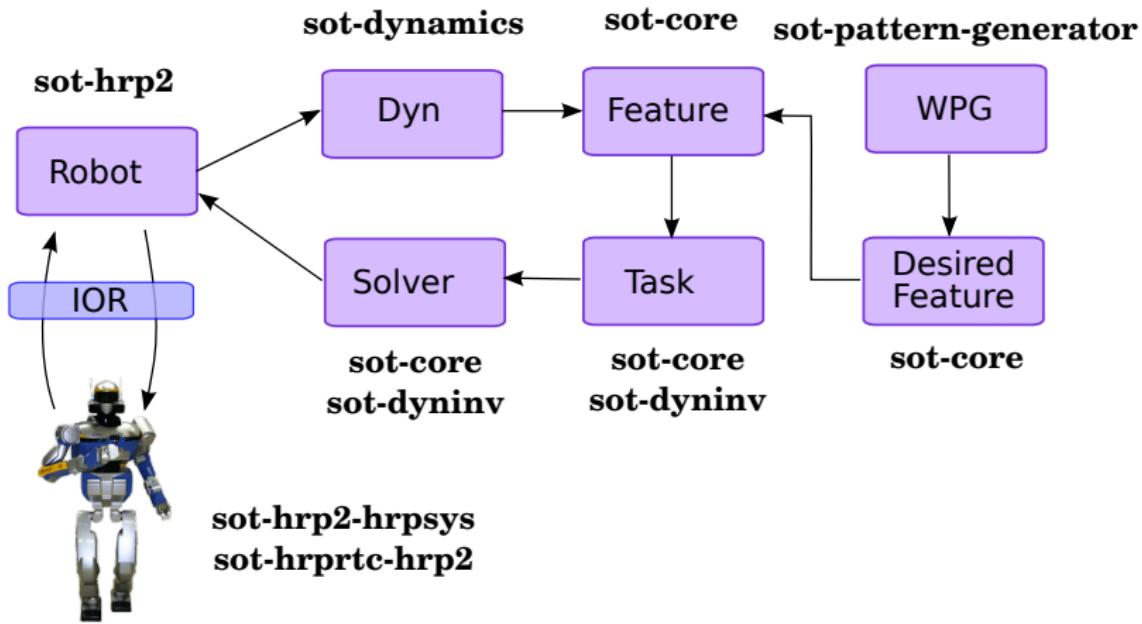


$$T(\mathbf{q}, t) = \begin{pmatrix} \mathbf{t}(M^{*-1}(t)M(\mathbf{q})) \\ u_\theta(R^{*-1}(t)R(\mathbf{q})) \end{pmatrix}$$
$$J = \frac{\partial T}{\partial \mathbf{q}}$$
$$M(\mathbf{q})$$



## Software structure - Link with Model





# Example



## Inverse Dynamics

## Weighted Pseudo Inverse

- Faster (!?) computation
- Easier to formulate
- Do not guarantee convergence
- Difficulty to tune the weights
- Do not handle properly inequalities

## Hierarchical Quadratic Program

- Slower (!?) computation time
- Warranty on priority
- Handle easily inequalities
- Difficult to formulate (here hidden in the solver)
- Known problems with cycles and singularities management

# Conclusions

## Pros

- Generic to put instantaneous controller together
- Allow code reusability
- Real-time performance
- Adapted to complex applications
- Binary packages support
- Eigen support

## Cons

- Research code
- The learning curve seems to be yet steep