

ORTA DOĞU TEKNİK ÜNİVERSİTESİ
MIDDLE EAST TECHNICAL UNIVERSITY

Cause Mining with STL

Ebru Aydin Gol
Computer Engineering, METU

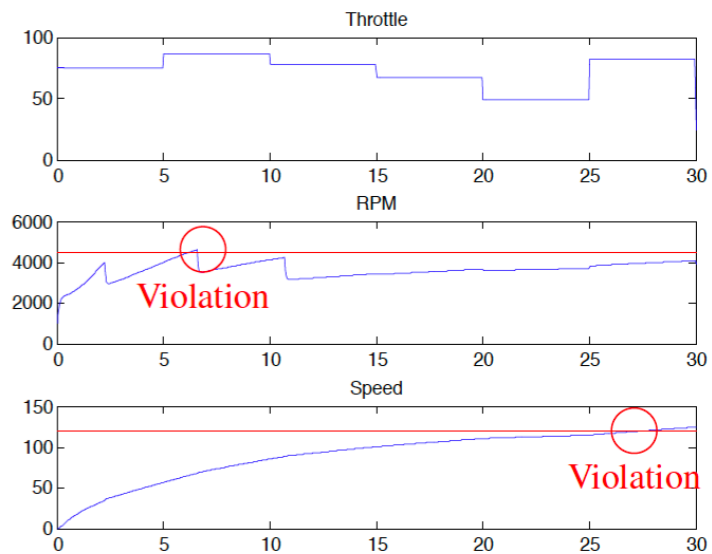
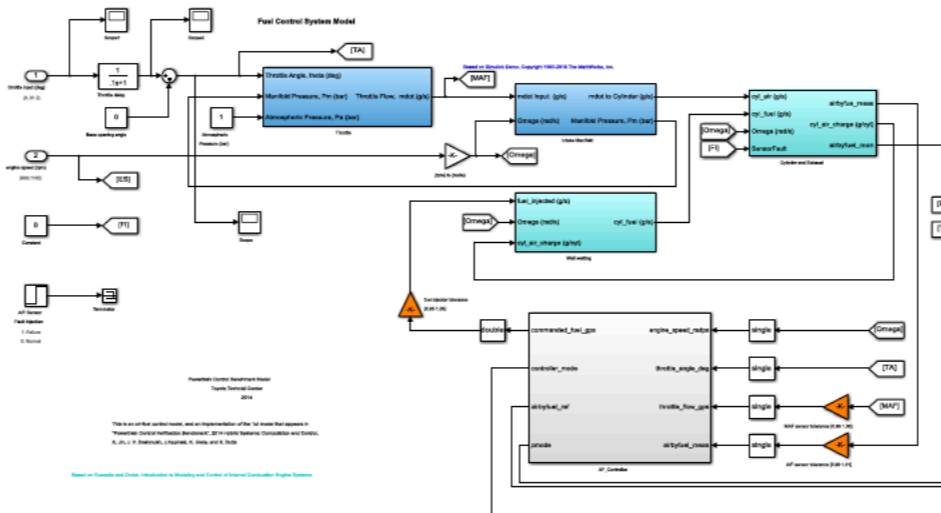
139th Shonan Meeting



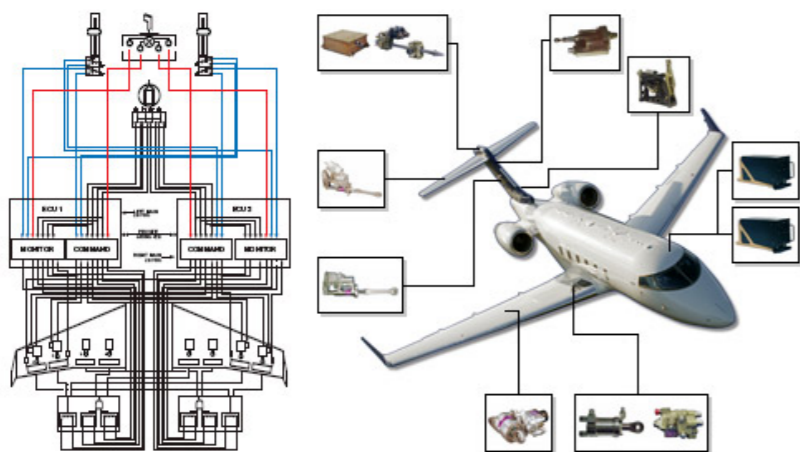
*H2020, MSCA – IF
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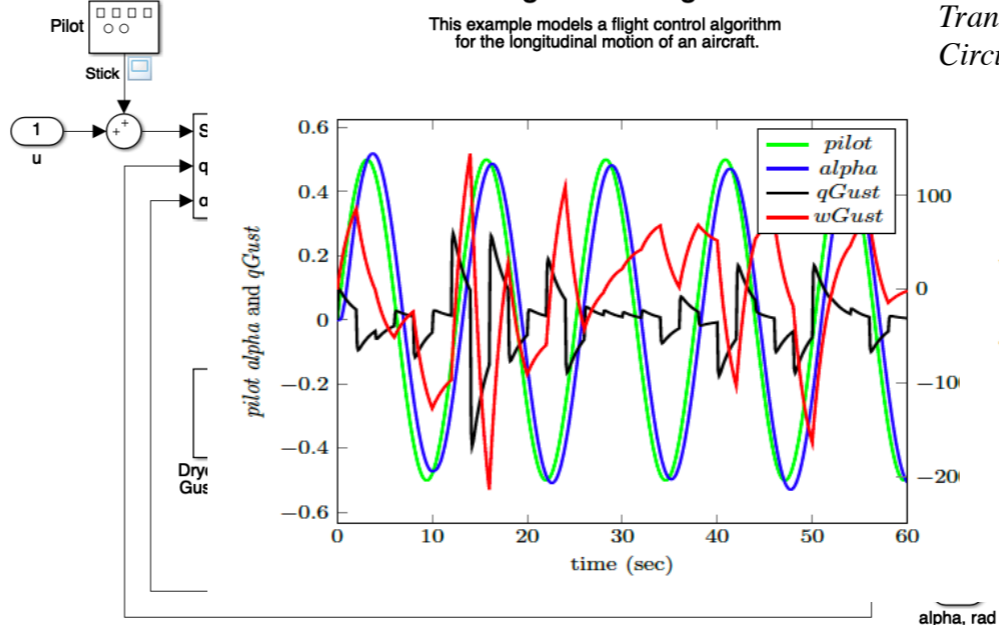
Power train control benchmark model by Toyota



Flight Control System Provider on Challenger 300

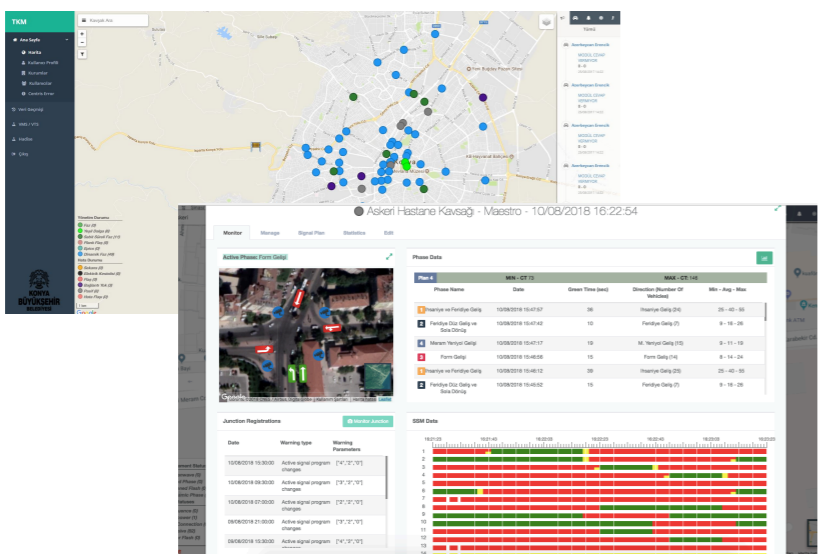
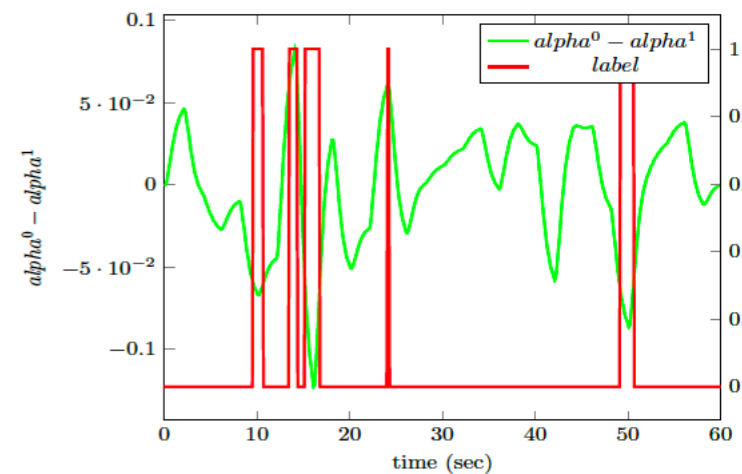
Aircraft Longitudinal Flight Control

This example models a flight control algorithm for the longitudinal motion of an aircraft.

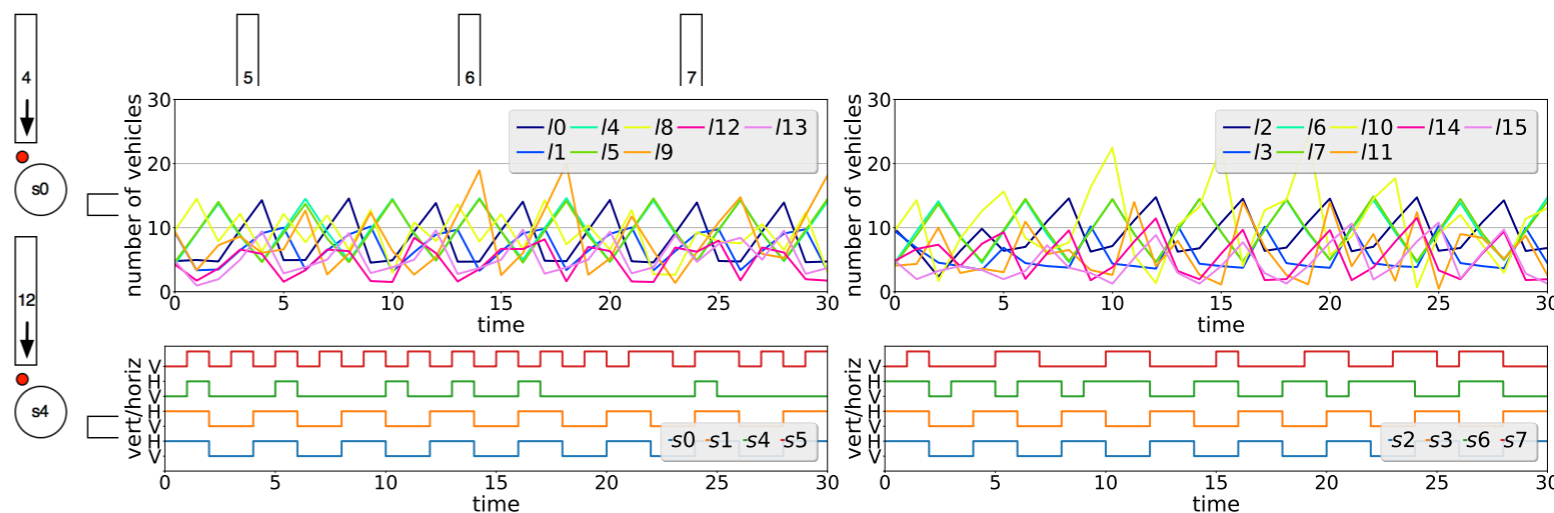


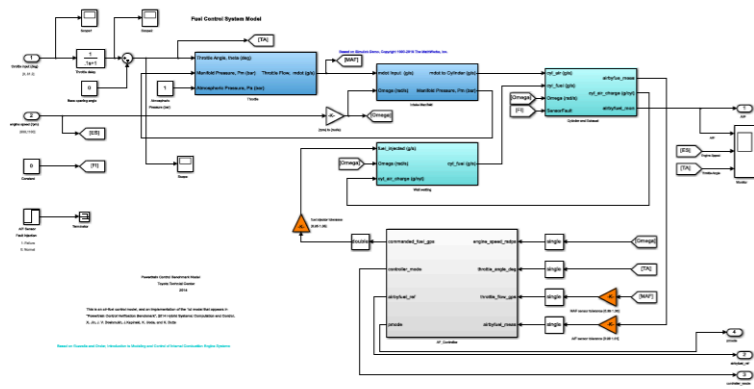
Copyright 2012-2015 The MathWorks, Inc.

X. Jin, A. Donzé, J. V. Deshmukh and S. A. Seshia, "Mining Requirements From Closed-Loop Control Models," in *IEEE Transactions on Computer-Aided Design of Integrated Circuits and Systems*

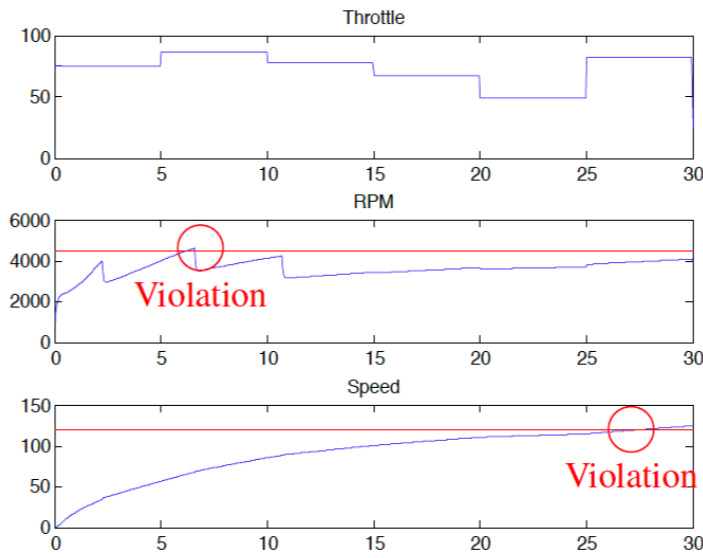


METIS

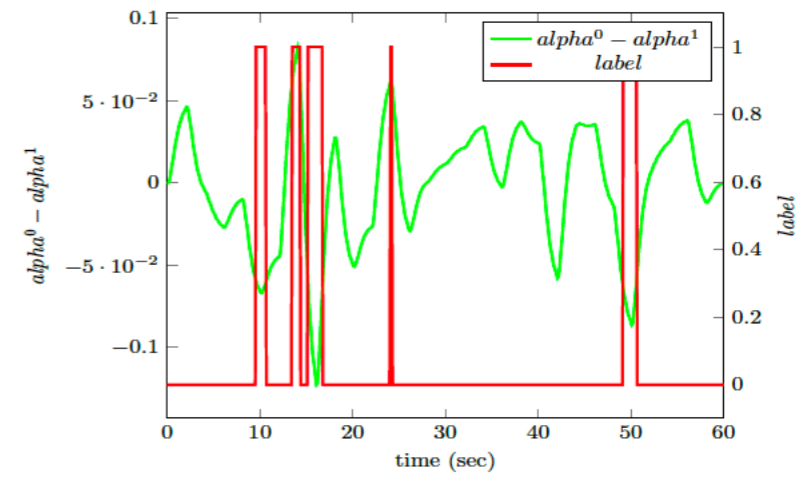
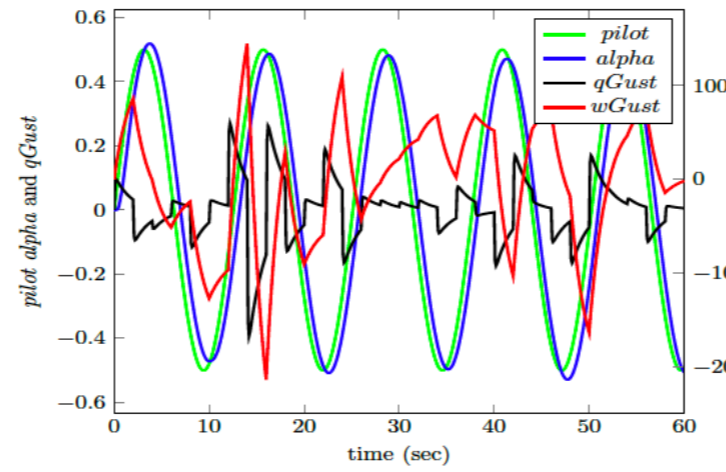
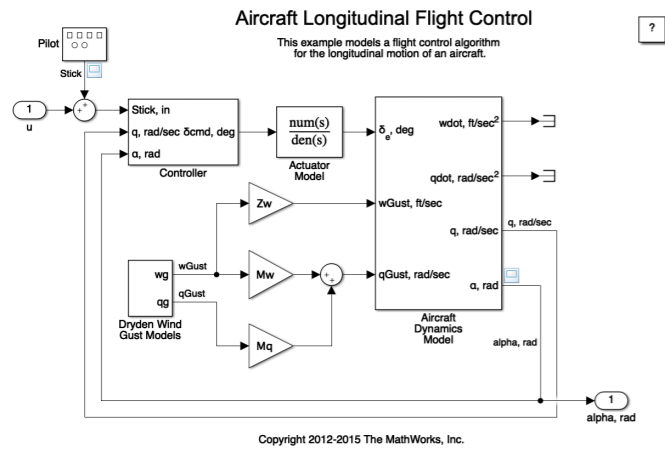




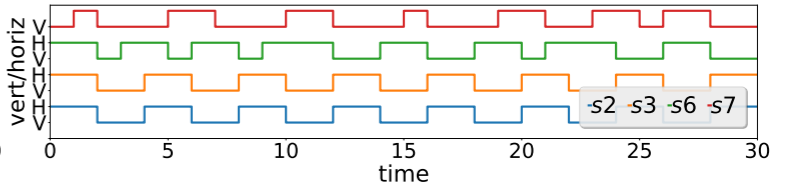
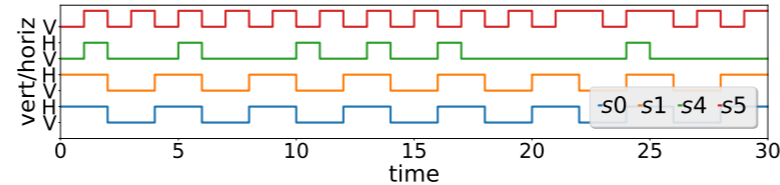
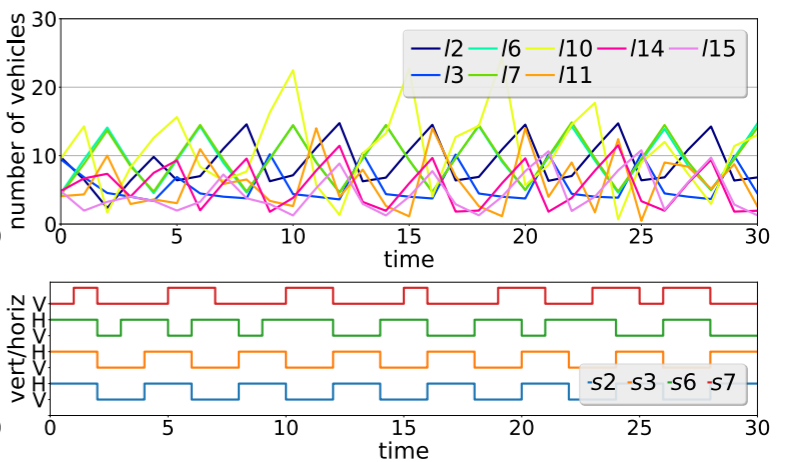
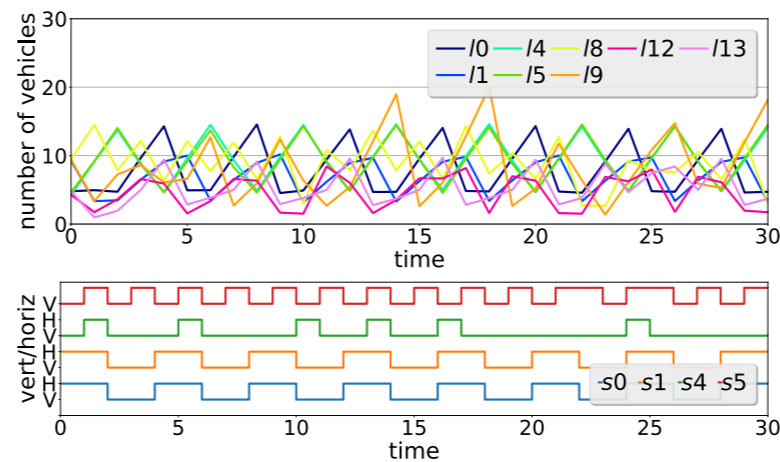
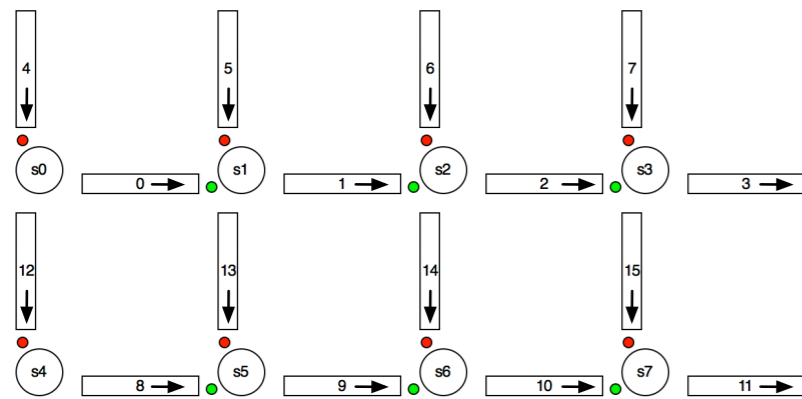
Power train control benchmark model by Toyota



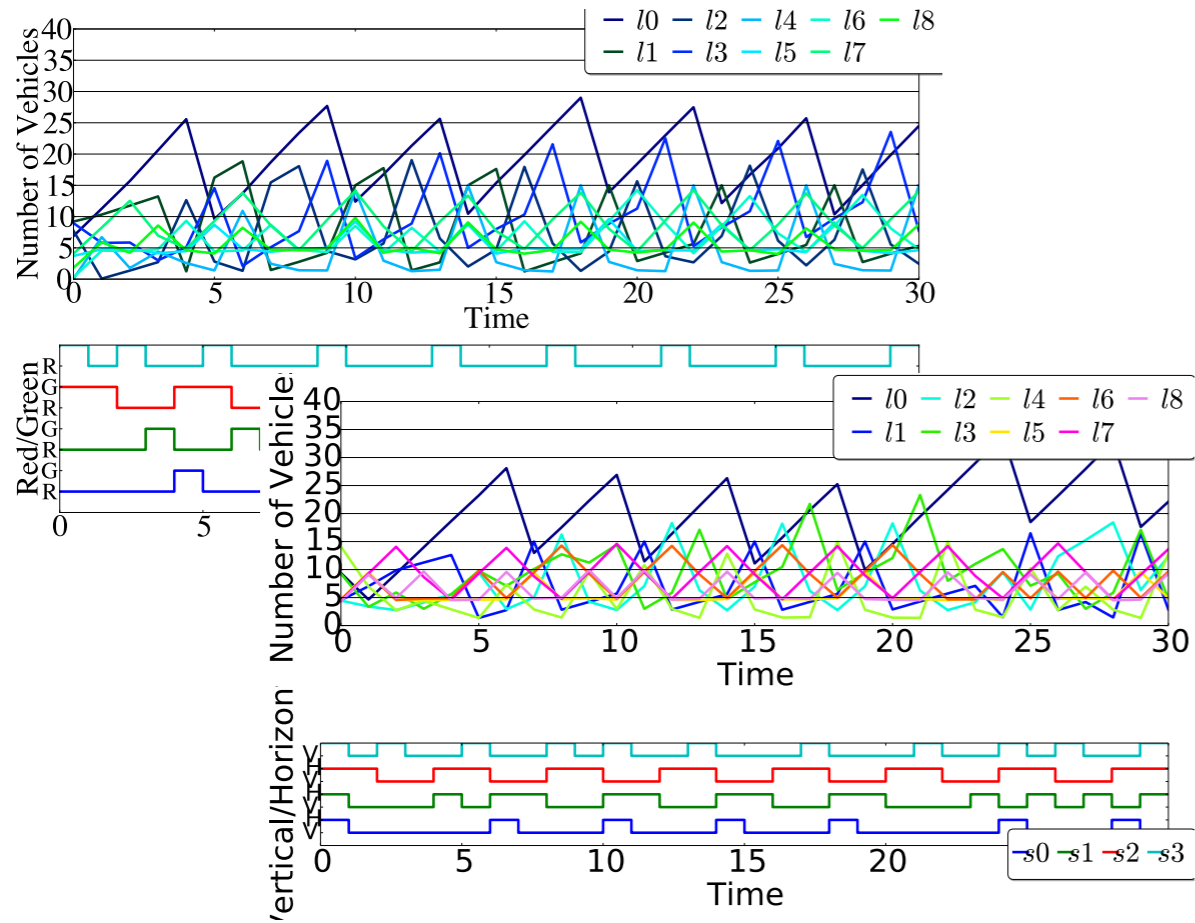
Human readable
System independent
Accurate representation



Can we describe the cause of the undesired event?



Our Approach in a Nutshell

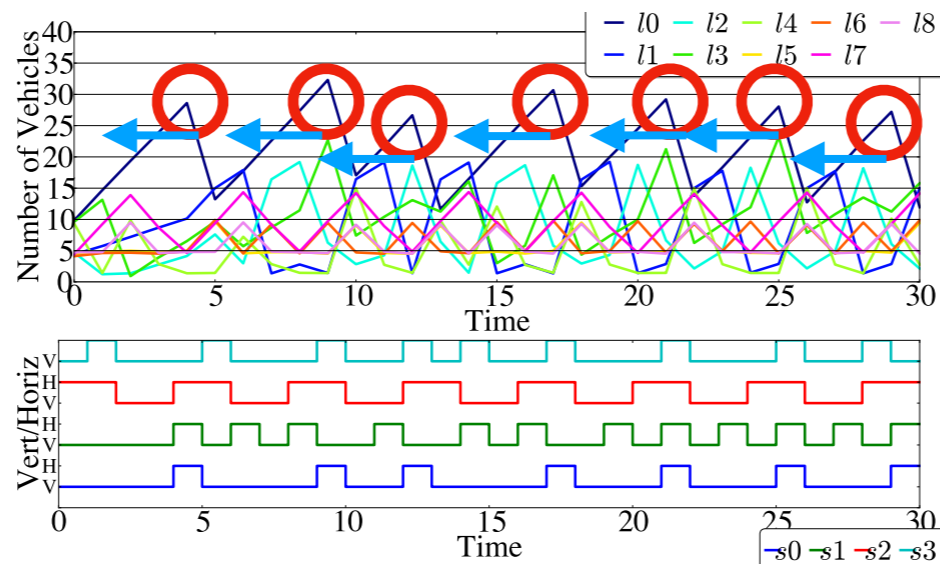


$$\phi = \phi_1 \vee \phi_2 \vee \phi_3$$

$$\phi_1 = \mathbf{P}_{[1,1]}((x^1 > 15) \wedge (s^1 = 1) \wedge (s^0 = 0))$$

$$\phi_2 = \mathbf{P}_{[1,1]}((x^1 > 25) \wedge (s^1 = 1))$$

$$\phi_3 = \mathbf{P}_{[1,1]}((x^4 < 10) \wedge (s^1 = 1) \wedge (s^0 = 0))$$

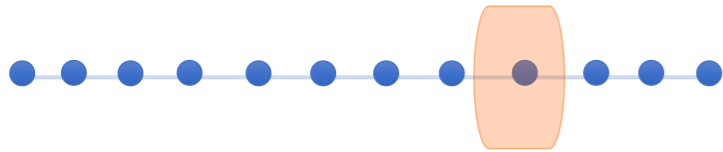


Outline

- Temporal logics
- Problem Definition
- Greedy Search for Formula Synthesis
- Iterative Search for Formula Synthesis
- Search for Controllable Formula
- Discussion

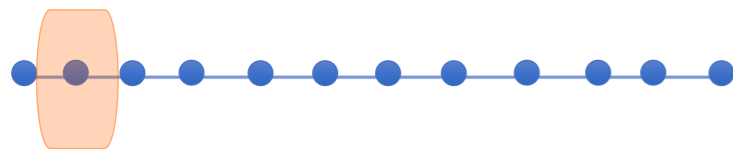
Linear Temporal Logic

Eventually a



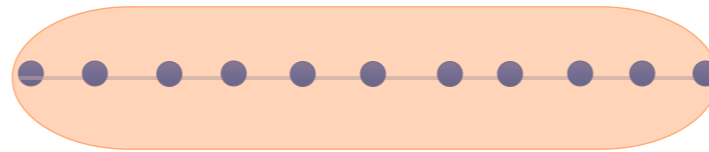
$F a$

Next a



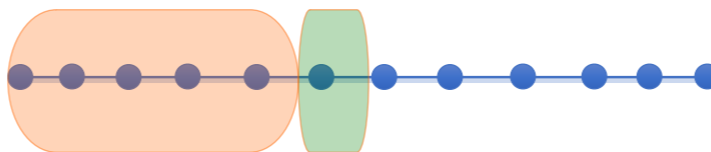
$X a$

Globally a



$G a$

a Until b



$a U b$

$G (\text{request} \rightarrow F \text{response})$

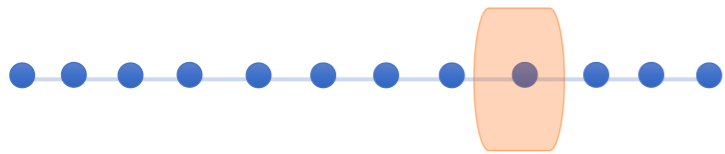
$$\phi = T \mid F \phi \mid G \phi \mid \phi U \phi \mid X \phi \mid \phi \wedge \phi \mid \phi \vee \phi \mid \neg \phi$$

Boolean operators: \wedge, \vee, \neg

Temporal operators: F, G, U, X

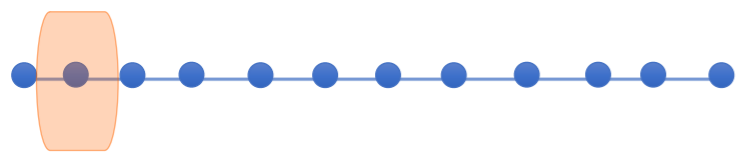
Linear Temporal Logic

Eventually a



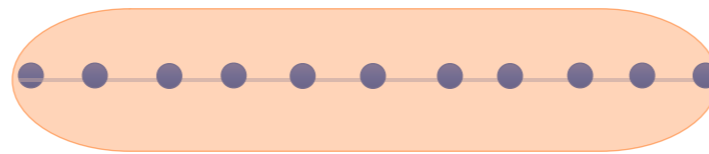
$F a$

Next a



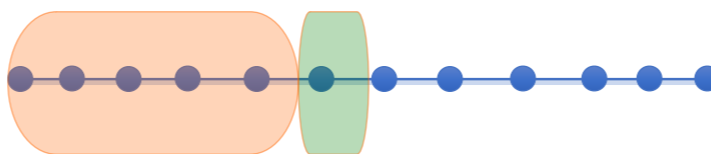
$X a$

Globally a



$G a$

a Until b



$a U b$

$G (\text{request} \rightarrow F \text{grant})$

$\phi = T \mid F \phi \mid G \phi \mid \phi U \phi \mid X \phi \mid \phi \wedge \phi \mid \phi \vee \phi \mid \neg \phi$

Boolean operators: \wedge, \vee, \neg

Temporal operators: F, G, U, X

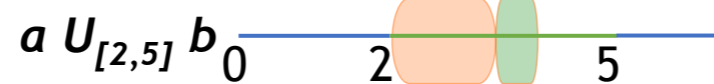
Metric Temporal Logic



$F_{[2,5]} a$



$G_{[2,5]} a$



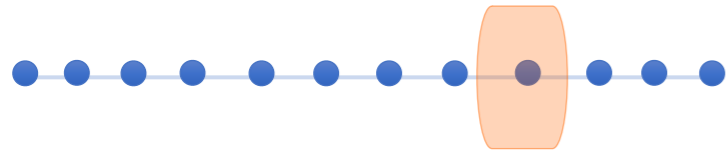
$a U_{[2,5]} b$

Real time, boolean predicates

$G_{[0,t]} (r \rightarrow F_{[0,c]} g)$

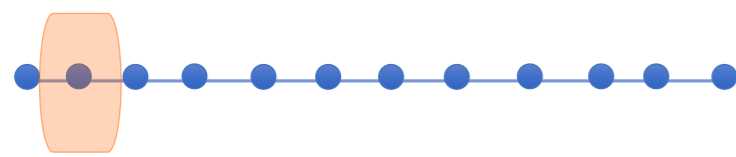
Linear Temporal Logic

Eventually a



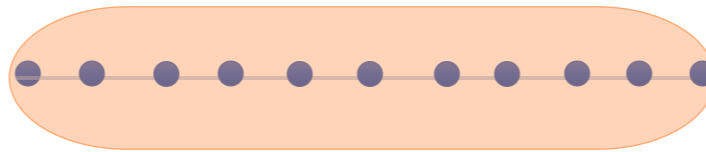
$F a$

Next a

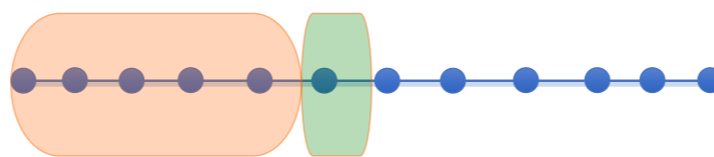


$X a$

Globally a



$G a$
 a Until b



$a U b$

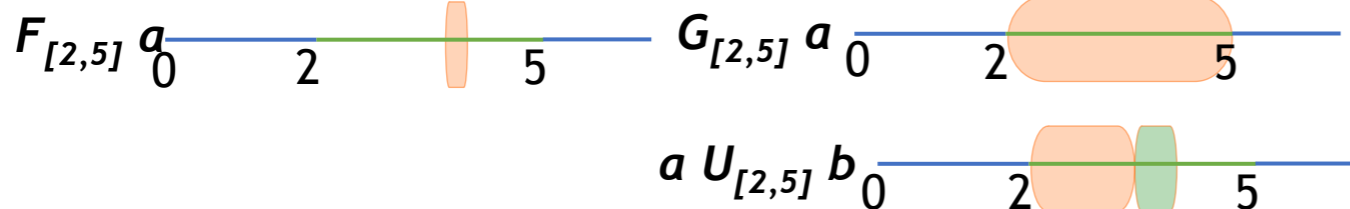
$G (\text{request} \rightarrow F \text{grant})$

$\phi = T \mid F \phi \mid G \phi \mid \phi U \phi \mid X \phi \mid \phi \wedge \phi \mid \phi \vee \phi \mid \neg \phi$

Boolean operators: \wedge, \vee, \neg

Temporal operators: F, G, U, X

Metric Temporal Logic



Real time, boolean predicates

$G_{[0,t]} (r \rightarrow F_{[0,c]} g)$

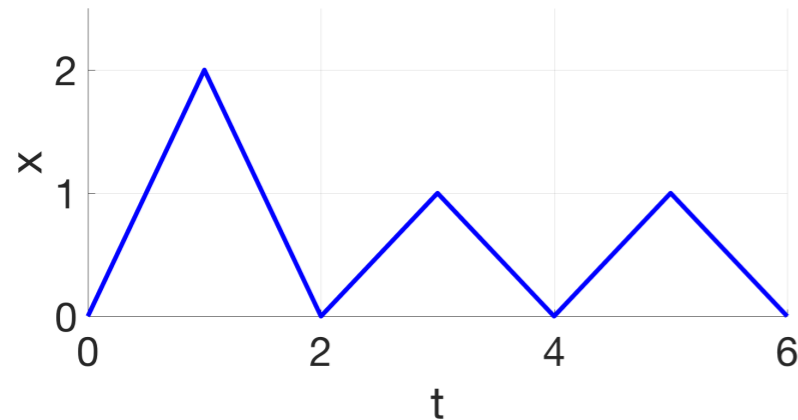
Signal Temporal Logic

Real time, real valued predicates

$G_{[0,T]} (r[t] > 0 \rightarrow F_{[0,D]} g[t] > 0)$

Signal Temporal Logic

- Predicates are over real values (signals), real time
- Allows for quantitative semantics



$$\phi = T \mid \phi_1 U_{[a,b]} \phi_2 \mid \phi_1 \wedge \phi_2 \mid \neg \phi \mid x < c$$

$$F_{[a,b]} \phi = T U_{[a,b]} \phi$$

$$G_{[a,b]} \phi = \neg (F_{[a,b]} \neg \phi)$$

Past Time Signal Temporal Logic

$$\phi = T \mid \phi_1 S_{[a,b]} \phi_2 \mid \phi_1 \wedge \phi_2 \mid \neg \phi \mid x < c$$

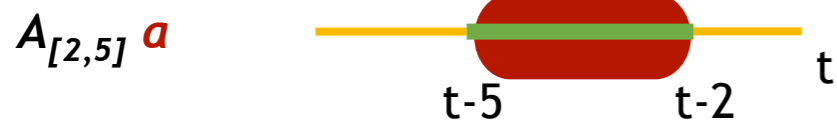
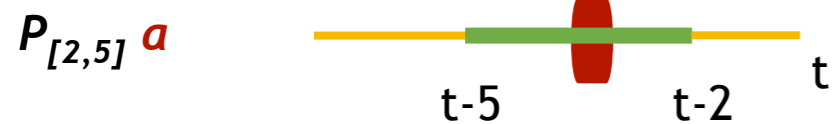
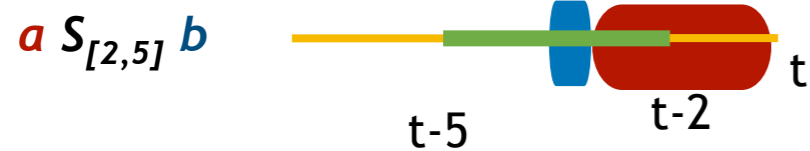
$$P_{[a,b]} \phi = T S_{[a,b]} \phi$$

$$A_{[a,b]} \phi = \neg(P_{[a,b]} \neg \phi)$$

$$\phi = T \mid \phi_1 U_{[a,b]} \phi_2 \mid \phi_1 \wedge \phi_2 \mid \neg \phi \mid x < c$$

$$F_{[a,b]} \phi = T U_{[a,b]} \phi$$

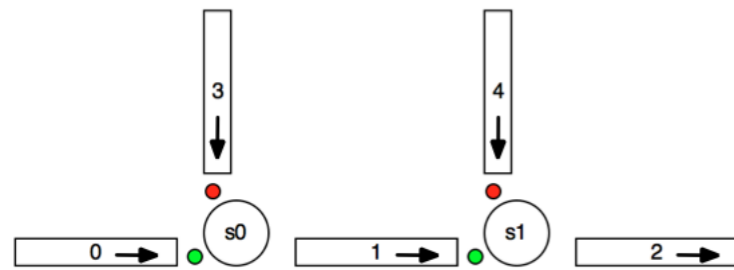
$$G_{[a,b]} \phi = \neg(F_{[a,b]} \neg \phi)$$



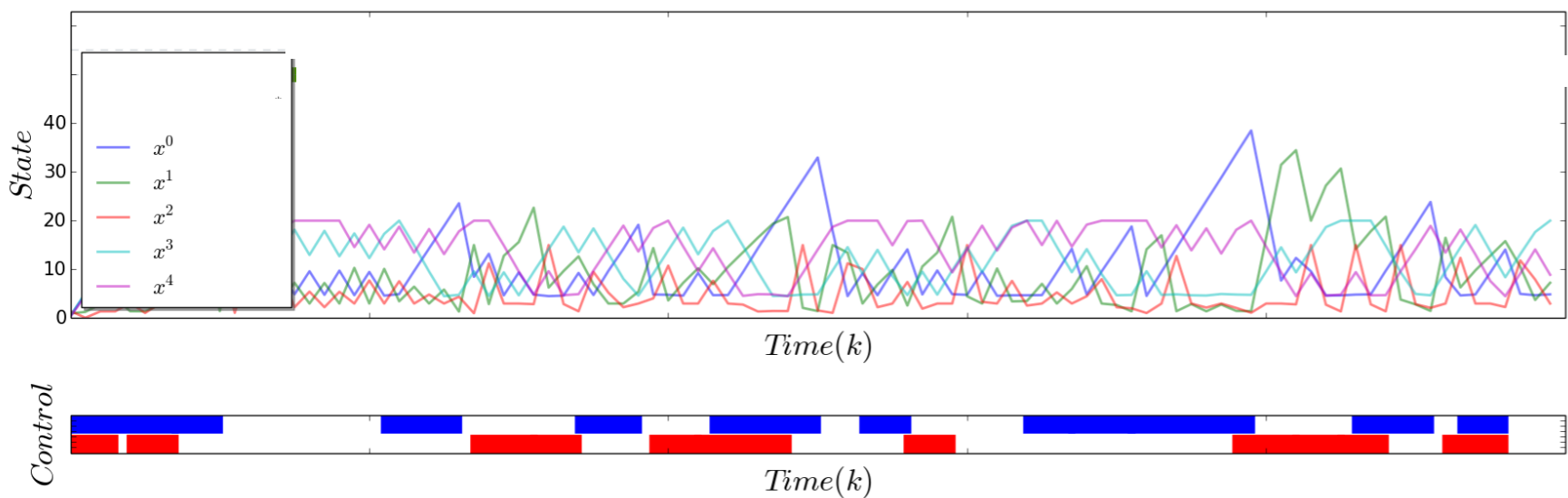
Problem Formulation

$$x_l[t + 1] = x_l[t] + d_l[t] - f_l^{out}(x_l[t]) + \sum_{k \in \mathcal{L}_v^{out}} \beta_{kl} f_k^{out}(x_k[t])$$

Given a system and a function over the signals for labeling unwanted events, find the cause of these events.



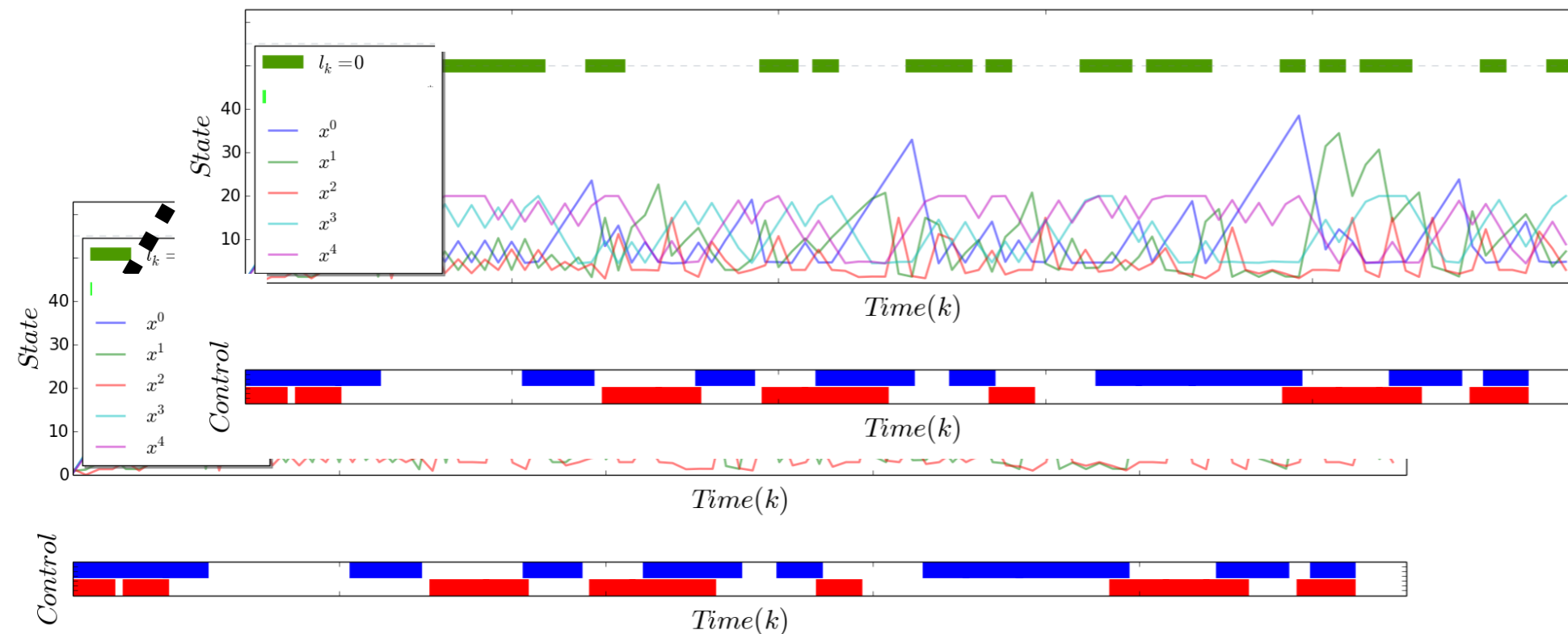
- 1 - Simulate
- 2 - Label the traces
- 3 - Find the reason



Given a set of labeled signals, find a ptSTL formula describing the labeled events

Problem Formulation

Given a set of labeled signals, find a ptSTL formula describing the labeled events

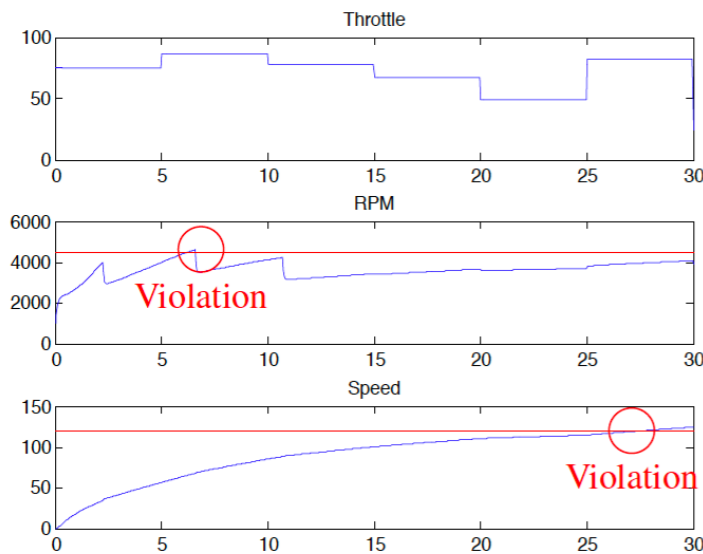


$$D = \{(T, L) \mid T = (t_0, x_0), \dots, (t_n, x_n), L = (t_0, l_0), \dots, (t_n, l_n)\}$$

$$(L, t) = 1$$

$$(T, t) \models \phi$$

Literature on Formula Synthesis



X. Jin, A. Donzé, J. V. Deshmukh and S. A. Seshia, "Mining Requirements From Closed-Loop Control Models," in *IEEE Transactions on Computer-Aided Design of Integrated Circuits and Systems*

"...find formulas defining signals as tight as possible..."

Susmit Jha, Ashish Tiwari, Sanjit A. Seshia, Tuhin Sahai, Natarajan Shankar, **TeLEx: learning signal temporal logic from positive examples using tightness metric.** *Formal Methods in System Design*, 2019

"...to infer signal temporal logic (STL) formulas that characterize the behavior of a dynamical system using only observed signal traces of the system ..."

E. Bartocci, L. Bortolussi, and G. Sanguinetti. **Data-driven statistical learning of temporal logic properties.** In *Formal Modeling and Analysis of Timed Systems*, pages 23-37. Springer, 2014.

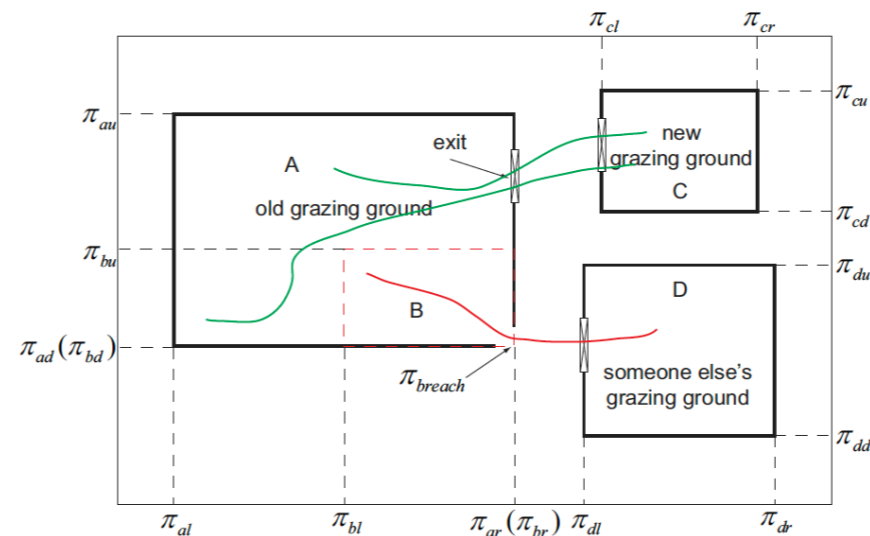


Figure 1: A herding example. The desired behaviors are shown in green, while the undesired ones are shown in red.

Zhaodan Kong, Austin Jones, Ana Medina Ayala, Ebru Aydin Gol and Calin Belta, **Temporal Logic Inference for Classification and Prediction from Data**, *Hybrid Systems: Computation and Control (HSCC)*, Berlin, Germany, 2014

"...formula that can discriminate between the desirable behaviors and the undesirable ones is constructed..."

Decision Tree Based approaches:

Giuseppe Bombara, Cristian Vasile, Francisco Penedo, Hirotohi Yasuoka, Calin Belta, **A Decision Tree Approach to Data Classification using Signal Temporal Logic**, *Hybrid Systems: Computation and Control (HSCC)*, Vienna, Austria, 2016

Ahmet Ketenci, Ebru Aydin Gol. **Synthesis of Monitoring Rules via Data Mining.** *American Control Conference (ACC)*, Philadelphia, PA. 2019.

Problem Formulation

Given a set of labeled signals, find a ptSTL formula describing the labeled events

$$D = \{(T, L) \mid T = (t_0, x_0), \dots, (t_n, x_n), L = (t_0, l_0), \dots, (t_n, l_n)\}$$

$$(L, t) = 1$$

$$(T, t) \models \phi$$

$$TP(D, \phi) = \sum_{(T,L) \in D} \sum_{t=0}^n \begin{cases} 1 & \text{if } l_i = 1 \text{ and } (T, t) \models \phi \\ 0 & \text{otherwise} \end{cases}$$

$$(L, t) = 1$$

$$(T, t) \models \neg \phi$$

$$FN(D, \phi) = \sum_{(T,L) \in D} \sum_{t=0}^n \begin{cases} 1 & \text{if } l_i = 1 \text{ and } (T, t) \models \neg \phi \\ 0 & \text{otherwise} \end{cases}$$

$$(L, t) = 0$$

$$(T, t) \models \neg \phi$$

$$TN(D, \phi) = \sum_{(T,L) \in D} \sum_{t=0}^n \begin{cases} 1 & \text{if } l_i = 0 \text{ and } (T, t) \not\models \phi \\ 0 & \text{otherwise} \end{cases}$$

$$(L, t) = 0$$

$$(T, t) \models \phi$$

$$FP(D, \phi) = \sum_{(T,L) \in D} \sum_{t=0}^n \begin{cases} 1 & \text{if } l_i = 0 \text{ and } (T, t) \models \phi \\ 0 & \text{otherwise} \end{cases}$$

Evaluation

| | | |
|-------|----|----|
| | 1 | 0 |
| Label | 1 | 0 |
| | TP | FN |
| | FP | TN |

Problem Formulation

Given a set of labeled signals, find a ptSTL formula describing the labeled events

$$D = \{(T, L) \mid T = (t_0, x_0), \dots, (t_n, x_n), L = (t_0, l_0), \dots, (t_n, l_n)\}$$

Evaluation

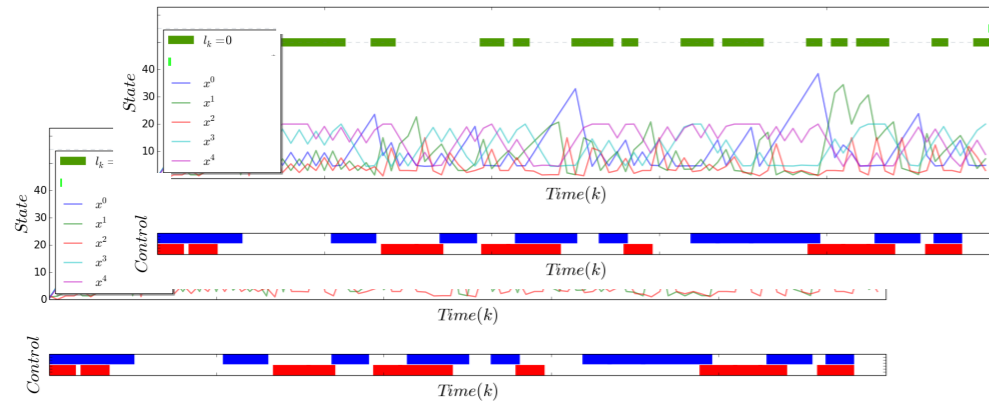
| | | |
|----------------|----|----|
| | 1 | 0 |
| Label 1 | TP | FN |
| 0 | FP | TN |

$$\text{FN} + \text{FP} \rightarrow 0$$

$$\phi$$

| Name | Abbreviation | Equation |
|-----------|--------------|-----------------------------|
| Mismatch | M | FP + FN |
| Precision | P | TP/(TP+FP) |
| Recall | R | TP/(TP+FN) |
| F beta | Fb | $(1+b^2) P R / (b^2 P + R)$ |

Greedy Search for Formula Synthesis



Find ϕ minimizing cost

$$\phi = T \mid \phi_1 S_{[a,b]} \phi_2 \mid \phi_1 \wedge \phi_2 \mid \neg \phi \mid P_{[a,b]} \phi \mid A_{[a,b]} \phi \mid x_i \leq c \mid x_i \geq c$$

$$A_{[a,b]} x_i \geq c$$

$$A_{[0,50]} x_1 \geq 20$$

$$P_{[a,b]} x_i \leq c$$

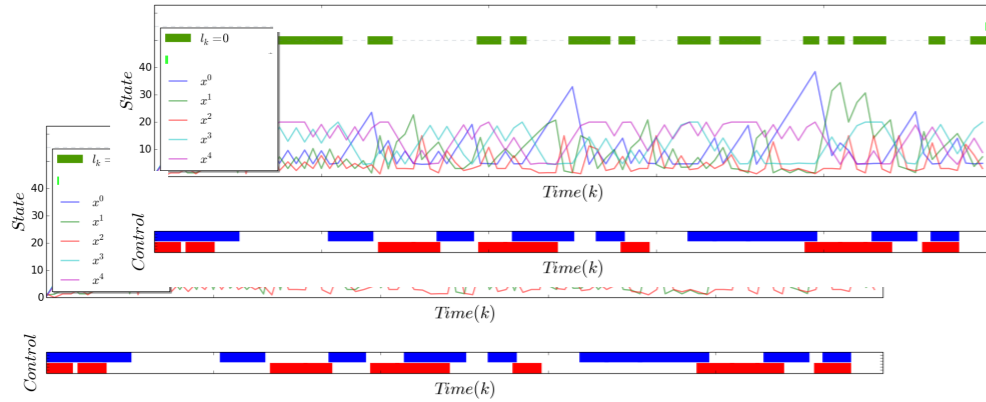
$$P_{[0,20]} x_2 \leq 0$$



Parameter synthesis

Who will write the
template formula?

Greedy Search for Formula Synthesis



Find ϕ minimizing cost

$$\phi = T \mid \phi_1 S_{[a,b]} \phi_2 \mid \phi_1 \wedge \phi_2 \mid \neg \phi \mid P_{[a,b]} \phi \mid A_{[a,b]} \phi \mid x^i \leq c \mid x^i \geq c$$

$$\mathcal{F}^0 = \{x^i \sim p_i \mid \sim \in \{<, >\}, i = 1, \dots, N\} \cup \{\mathbf{T}\}$$

$$\mathcal{F}^n = \{\neg \phi \mid \phi \in \mathcal{F}^{n-1}\}$$

$$\cup \{P_{[p_a, p_b]} \phi \mid \phi \in \mathcal{F}^{n-1}\}$$

$$\cup \{A_{[p_a, p_b]} \phi \mid \phi \in \mathcal{F}^{n-1}\}$$

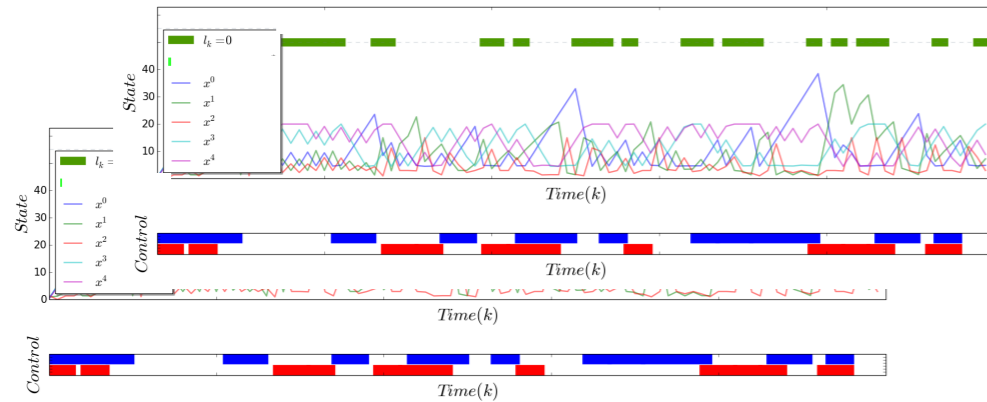
$$\bigcup_{i=1}^{n-1} \{\phi_1 \wedge \phi_2 \mid \phi_1 \in \mathcal{F}^i, \phi_2 \in \mathcal{F}^{n-i-1}\}$$

$$\bigcup_{i=1}^{n-1} \{\phi_1 \vee \phi_2 \mid \phi_1 \in \mathcal{F}^i, \phi_2 \in \mathcal{F}^{n-i-1}\}$$

$$\bigcup_{i=1}^{n-1} \{\phi_1 S_{[p_a, p_b]} \phi_2 \mid \phi_1 \in \mathcal{F}^i, \phi_2 \in \mathcal{F}^{n-i-1}\}$$

$$\mathcal{F}^{\leq n} = \bigcup_{i=0}^n \mathcal{F}^i$$

Greedy Search for Formula Synthesis



Find ϕ minimizing cost

$$\mathcal{F}^{\leq n} = \bigcup_{i=0}^n \mathcal{F}^i$$

Given an operator limit, run parameter optimization for each

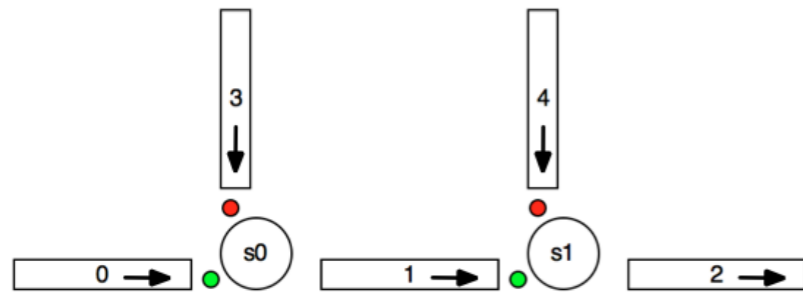
$$\phi^p \in \mathcal{F}^{\leq n}$$

$$\phi = T \mid \phi_1 S_{[a,b]} \phi_2 \mid \phi_1 \wedge \phi_2 \mid \neg \phi \mid P_{[a,b]} \phi \mid A_{[a,b]} \phi \mid x^i \leq c \mid x^i \geq c$$

| Parameter | Limits | |
|-----------|--------|--------|
| c^i | Lc^i | Uc^i |
| a | La | Ua |
| b | La | Ub |

Given a parametric formula ϕ^p , and parameter limits, run grid search.

Greedy Search for Formula Synthesis - Example



$$x^0, x^1, x^2, x^3, x^4, s^0, s^1$$

$$x^0, x^1, x^2 \in [0, 40]$$

$$x^3, x^4 \in [0, 20]$$

$$s^0, s^1 \in \{0, 1\}$$

Minimize F 0.3

Simulate, assign label 1 when a link has more vehicles than %75 of its capacity

$$x^0 < 30 \wedge x^1 < 30 \wedge x^2 < 30 \wedge x^3 < 15 \wedge x^4 < 15$$

Identify it, before it happens: $P_{[1,1]} \phi^P, \phi^P \in \mathcal{F}^{\leq n}$

Operator count limit 0 ($x^i \not</> c$), 14 formulas.

$$P_{[1,1]} s_0 = 0 \quad \text{fp: 307 fn: 256 tp: 599 tn: 638, f03: 0.664}$$

Operator count limit 1, 14 + 156 formulas.

DOES NOT SCALE

$$P_{[1,1]} (x^3 \geq 10.0 \wedge s^0 = 0) \quad \text{fp: 0 fn: 375 tp: 480 tn: 945, f03: 0.939}$$

Operator count limit 2, 14 + 156 + 5532 formulas.

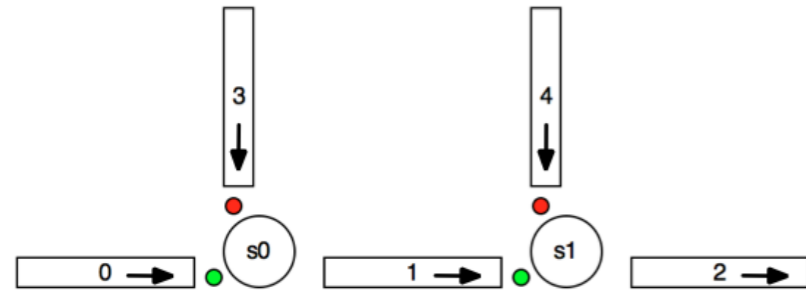
$$P_{[1,1]} (x^3 \geq 10.0 \wedge s^0 = 0) \quad \text{fp: 0 fn: 375 tp: 480 tn: 945, f03: 0.939}$$

Operator count limit 3, 14 + 156 + 5532 + **96414** formulas.

$$P_{[1,1]} ((x^4 \geq 10 \wedge s^1 = 0) \vee (x^3 \geq 10 \wedge s^0 = 0)) \quad \text{fp: 0 fn: 70 tp: 785 tn: 945, f03: 0.993}$$



Greedy Search for Formula Synthesis - Example



$$x^0, x^1, x^2, x^3, x^4, s^0, s^1$$

$$x^0, x^1, x^2 \in [0, 40]$$

$$x^3, x^4 \in [0, 20]$$

$$s^0, s^1 \in \{0, 1\}$$

Minimize F 0.3

Simulate, assign label 1 when a link has more vehicles than %75 of its capacity

$$x^0 < 30 \wedge x^1 < 30 \wedge x^2 < 30 \wedge x^3 < 15 \wedge x^4 < 15$$

$$P_{[1,1]}((x^4 \geq 10 \wedge s^1 = 0) \vee (x^3 \geq 10 \wedge s^0 = 0))$$

fp: 0 fn: 70 tp: 785 tn: 945, f03:0.993

misclassification rate: 3.9 %

- There can be multiple causes.
- Increasing the operator count does not scale.

Iterative Formula Search-Heuristic 1

- There can be multiple causes.
- Increasing the operator count does not scale.
- Iterative cause finding ?

THE IDEA

- Given upper and lower bounds on operator count
- Found formulas: $\Phi^* = False$
- Start with $n=lower\ bound$, until $n > upper\ bound$
 - For each $\phi^p \in \mathcal{F}^n$
 - Perform parameter optimization for $P_{[1,1]}(\phi^p \vee \Phi^*)$
 - Get the optimal one ϕ^*
 - If there is sufficient improvement, update the found formula $\Phi^* = \Phi^* \vee \phi^*$
 - Otherwise increment n

1 $n=0$, best formula $P_{[1,1]}s_0 = 0$ f03: 0.664

Insufficient, increment n

2 $n=1$, best formula $P_{[1,1]}(x^3 \geq 10.0 \wedge s^0 = 0)$ f03: 0.939

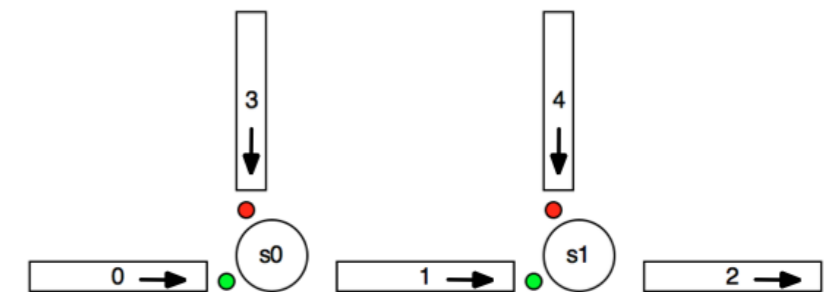
Update $\Phi^* = P_{[1,1]}(x^3 \geq 10.0 \wedge s^0 = 0)$

3 $n=1$, best formula $P_{[1,1]}(x^4 \geq 10.0 \wedge s^1 = 0)$ f03: 0.993

Update $\Phi^* = P_{[1,1]}((x^3 \geq 10.0 \wedge s^0 = 0) \vee (x^4 \geq 10.0 \wedge s^1 = 0))$

4 $n=1$, best formula $P_{[1,1]}(x^0 \geq 25 \wedge s^1 = 1)$ f03: 0.995

Insufficient, increment n



valuation of the combined formula

fp: 0 fn: 70 tp: 785 tn: 945

Iterative Formula Search-Heuristic 2

- There can be multiple causes.
- Increasing the operator count does not scale.
- Iterative cause finding ?

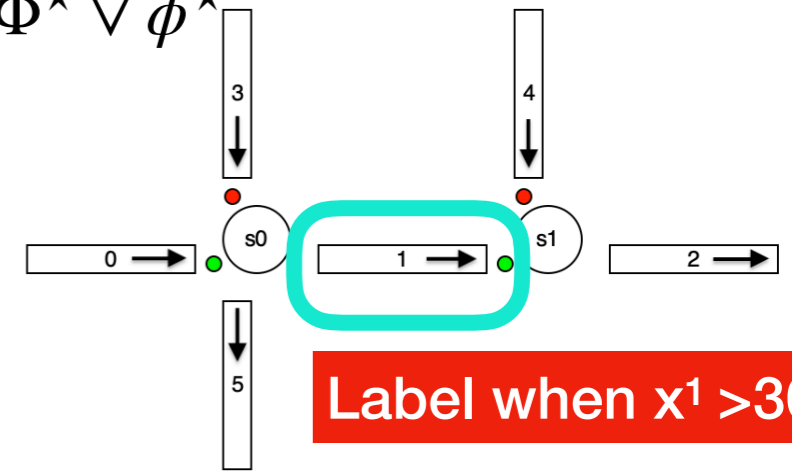
THE IDEA

- Given upper bound on operator count n
- Found formulas: $\Phi^* = False$
- For each $\phi^p \in \mathcal{F}^n$
 - Perform parameter optimization for $P_{[1,1]}\phi^p$
- While the sub-formula limit is not exceeded
 - Select ϕ^* maximizing $TP(\Phi^* \vee \phi^*)$ and set $\Phi^* = \Phi^* \vee \phi^*$
 - Stop when the improvement is insufficient

Optimization is performed once

Monotonic

Maximize TP limit FP



FP limit 20

1 First iteration $\phi_1 = P_{[1,1]}(x^1 > 15 \wedge s^0 = 0 \wedge s^1 = 1)$

2 Second iteration $\phi_2 = P_{[1,1]}(x^1 \geq 25 \wedge s^1 = 1)$

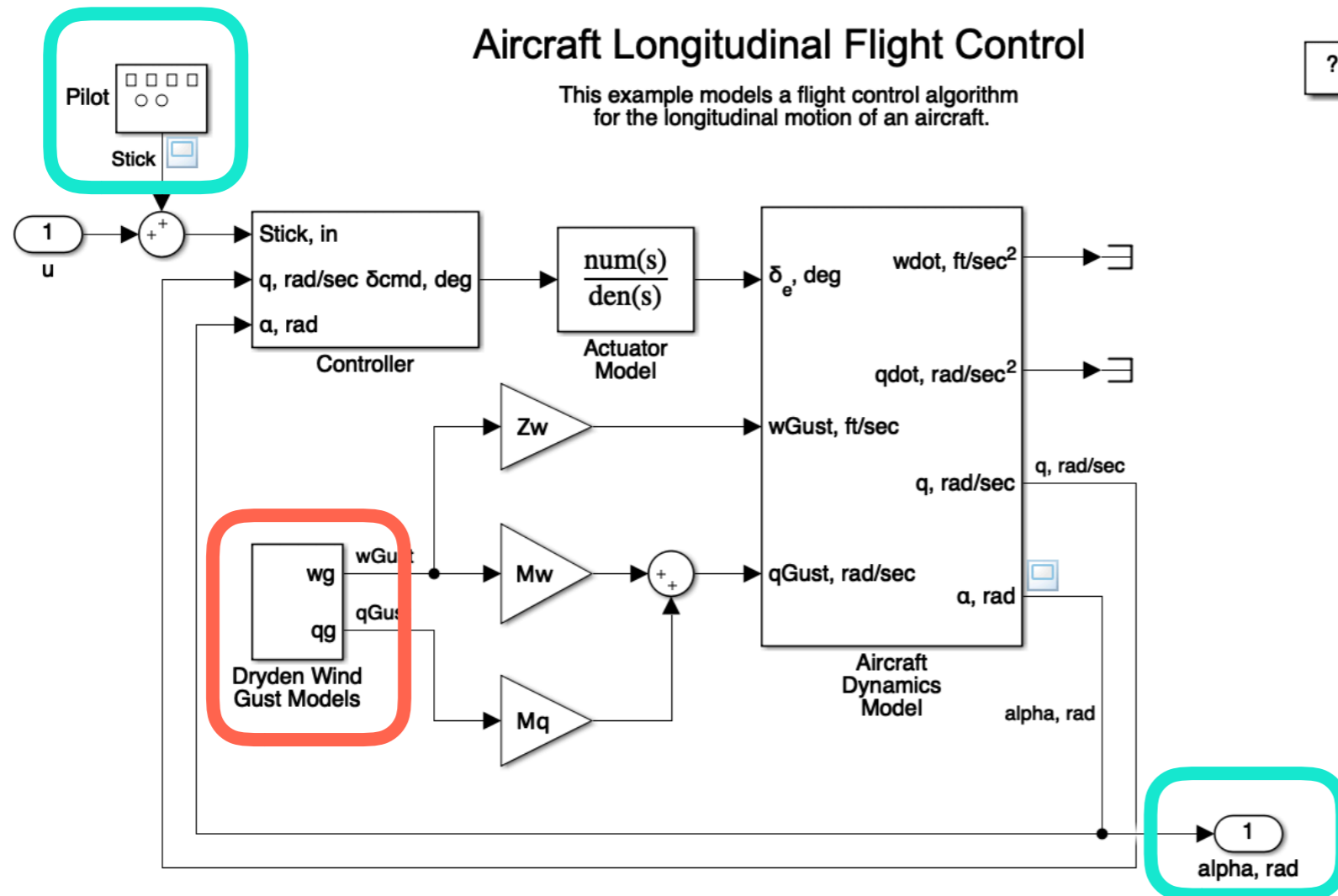
3 Third iteration $\phi_3 = P_{[1,1]}(x^4 \leq 10 \wedge s^0 = 0 \wedge s^1 = 1)$

$$\phi_1 \vee \phi_2 \vee \phi_3$$

fp: 30 fn: 2 tp: 454 tn: 1314, mr = 1.8%

Computation: a few minutes

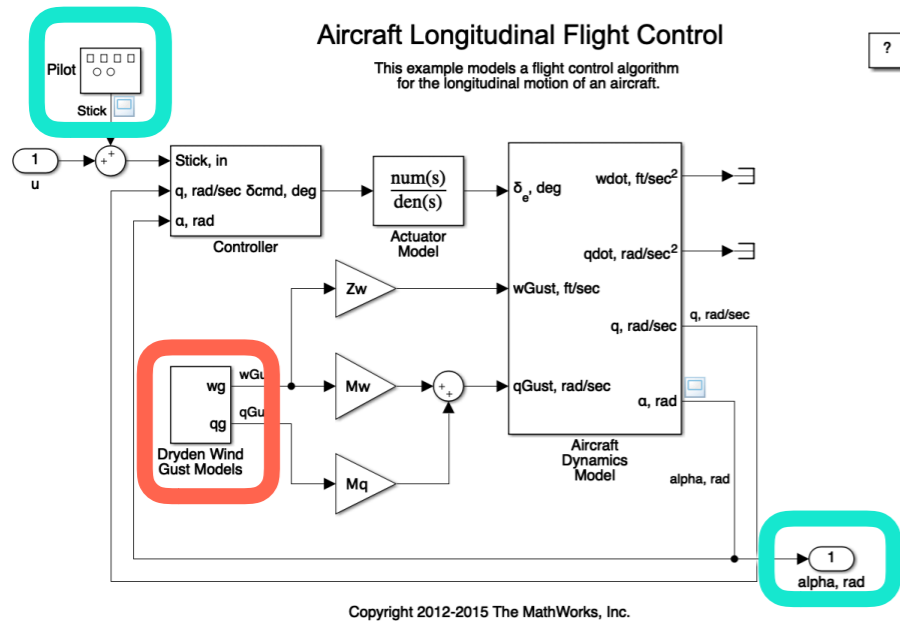
Iterative Formula Search-Heuristic 2 - Example



When the aircraft's longitudinal motion disturbs?

alpha⁰ : no wind
alpha¹ : wind (random)

Iterative Formula Search-Heuristic 2 - Example



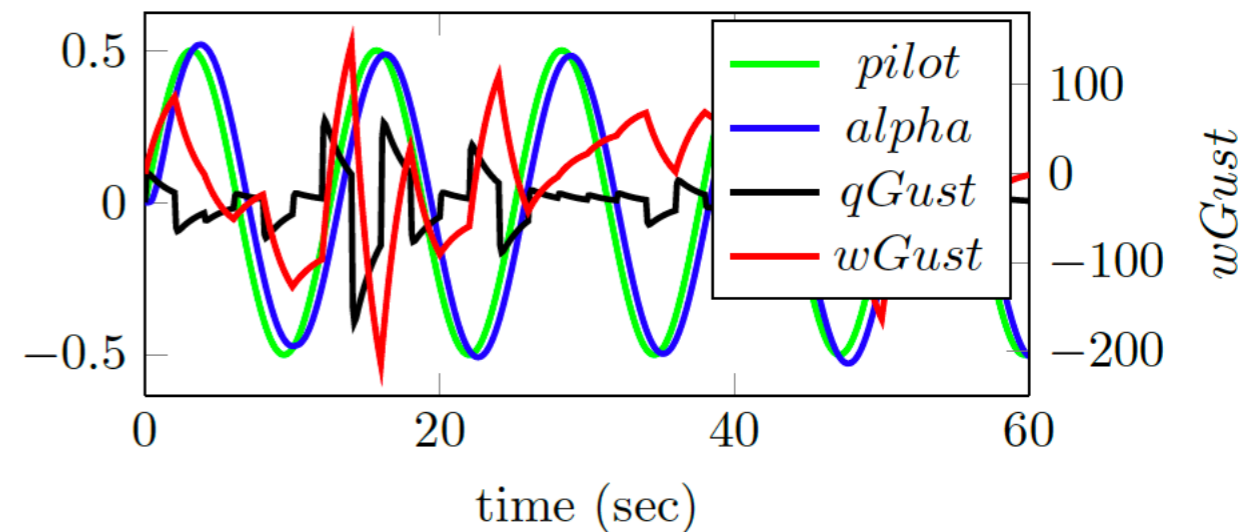
α^0 : no wind

α^1 : wind (random)

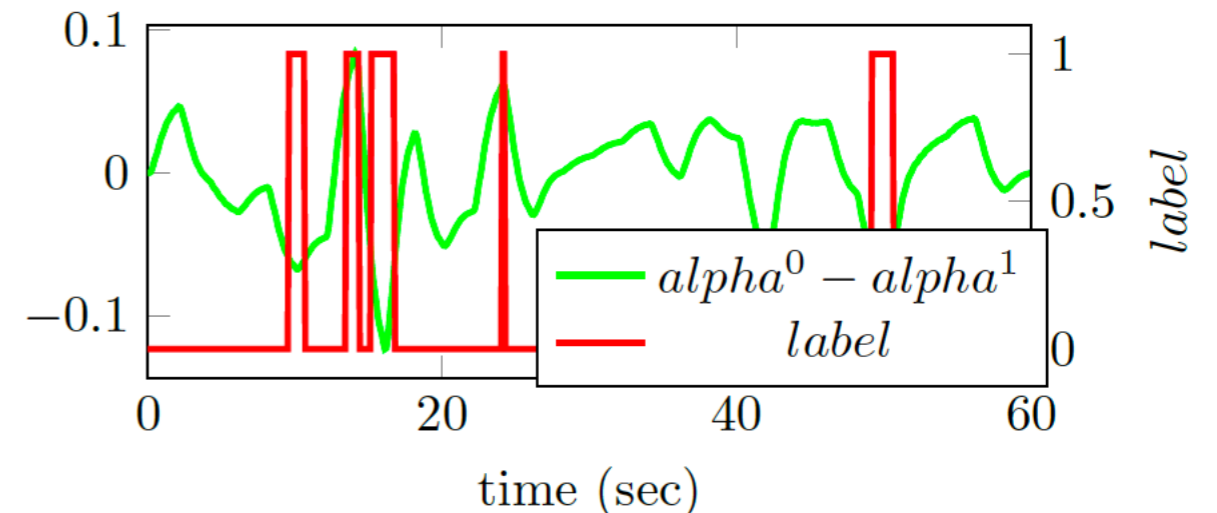
When the aircraft's longitudinal motion disturbs?

α^1

pilot alpha and qGust



alpha⁰ - alpha¹

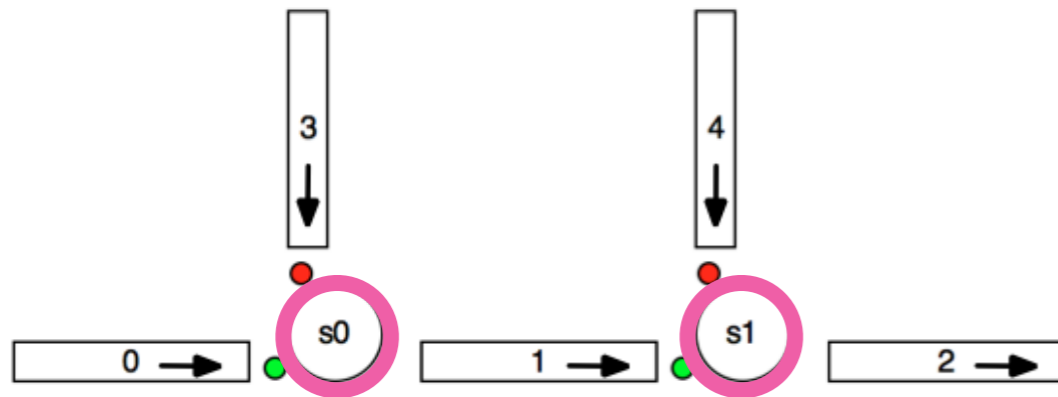


- 1 $\phi_1 = P_{[4,10]}(qGust \leq 0 \wedge wGust \leq -120)$
- 2 $\phi_2 = wGust \geq 120 \wedge A_{[14,14]}(pilot \geq -0.4)$
- 3 $\phi_3 = P_{[2,2]}(alpha \leq 0.3 \wedge wGust - \leq 120)$
- 4 $\phi_4 = (A_{[2,6]}qGust \geq 0.1) \wedge pilot \leq -0.4$

$$\phi_1 \vee \phi_2 \vee \phi_3 \vee \phi_4 \quad \text{fp: 18 fn: 58 tp: 419 tn: 2505, mr=2.5\%}$$

Controllable Formula Search (*ongoing work*)

Find the cause and update the system to avoid it in fully automated way.



s^0 and s^1 are controllable

$$\Phi_1 \vee \dots \vee \Phi_p$$
$$\Phi_i := (A_{[1,b_i]} u^j = c_i) \wedge (P_{[1,1]} \phi_i)$$

Controller: Select u that violates each cause

- 1: $\mathbb{U}^{cand} = \mathbb{U}$
- 2: **while** $\mathbb{U}^{cand} \neq \emptyset$ **do**
- 3: $u_k = \text{Random}(\mathbb{U}^{cand})$
- 4: **if** $(\mathbf{x}, (x_k, u_k), k) \models (G_{[0,b_i-1]}^- u^j = c_i) \wedge \phi_i$ for some Φ_i from Φ **then**
- 5: $\mathbb{U}^{cand} = \mathbb{U}^{cand} \setminus \{u_k\}$
- 6: **else return** u_k
- 7: **end if**
- 8: **end while**
- 9: **return** $\text{Random}(\mathbb{U})$

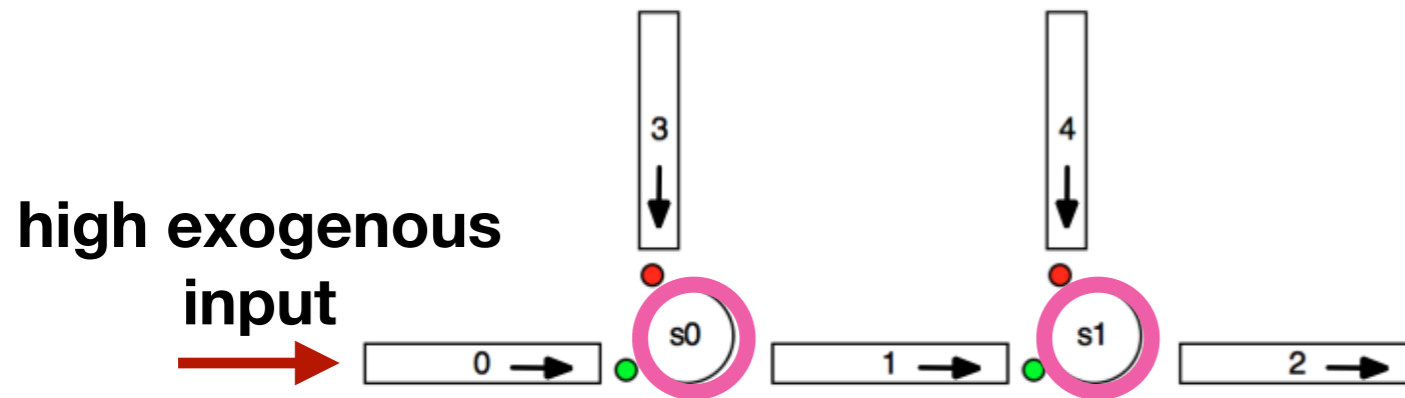
ITERATIVELY

Find cause

Synthesize controller

Simulate-label

Controllable Formula Search (*ongoing work*)



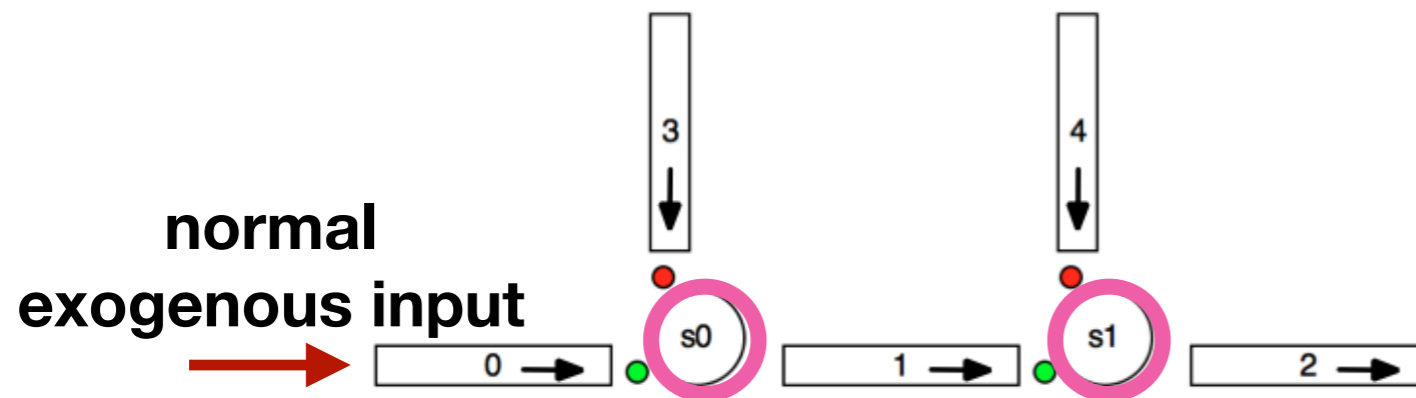
$$\Phi_1 \vee \dots \vee \Phi_p$$

$$\Phi_i := (A_{[1,b_i]} u^j = c_i) \wedge (P_{[1,1]} \phi_i)$$

%79 percent
congestion

| i | Viol Count | Φ_i | tp | fp |
|---|------------|---|-----|----|
| 1 | 1591 | $A_{[1,2]}(s^0 = 1) \wedge P_{[1,1]}(x^0 > 20)$ | 405 | 0 |
| 2 | 1549 | $A_{[1,2]}(s^0 = 0) \wedge P_{[1,1]}(x^3 > 10)$ | 576 | 0 |
| 3 | 1557 | $A_{[1,2]}(s^1 = 0) \wedge P_{[1,1]}(x^1 > 20)$ | 465 | 19 |
| 4 | 1763 | $A_{[1,2]}(s^1 = 1) \wedge P_{[1,1]}(x^4 > 10)$ | 599 | 3 |
| 5 | 2 | | | |

Controllable Formula Search (*ongoing work*)



$$\Phi_1 \vee \dots \vee \Phi_p$$

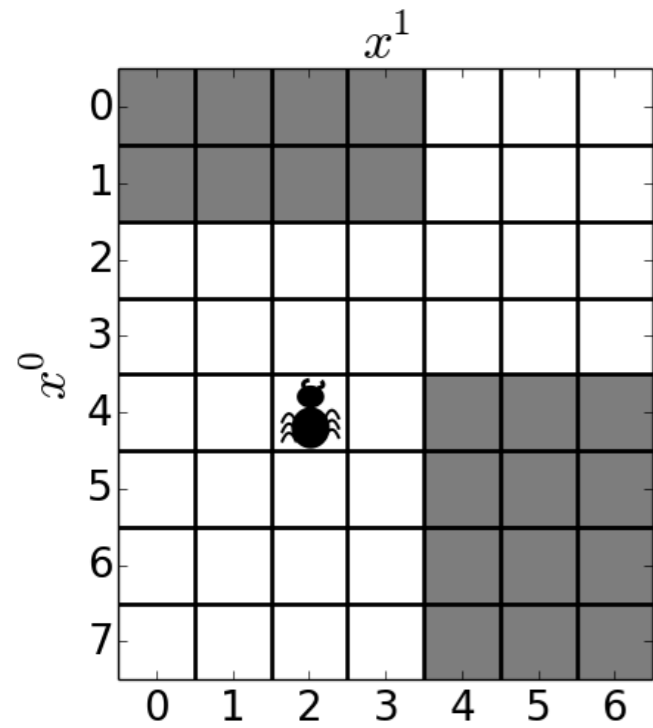
$$\Phi_i := (A_{[1,b_i]} u^j = c_i) \wedge (P_{[1,1]} \phi_i)$$

| <i>Ex#</i> | time | v_0 | v_1 | v_2 | v_3 | v_4 | v_5 | v_6 | v_7 |
|------------|--------|-------|-------|-------|-------|-------|-------|-------|-------|
| #1 | 630sec | 143 | 23 | 5 | 2 | 1 | 0 | - | - |
| #2 | 320sec | 911 | 530 | 265 | 5 | 6 | 2 | 0 | - |
| #3 | 115sec | 911 | 617 | 149 | 80 | 70 | 48 | 10 | 0 |

| <i>Ex#</i> | \underline{oc} | \overline{oc} | \bar{p} | \underline{val} |
|------------|------------------|-----------------|-----------|-------------------|
| #1 | 0 | ∞ | ∞ | 0.01 |
| #2 | 0 | ∞ | ∞ | 0.1 |
| #3 | 0 | 0 | 1 | 0 |

No formal guarantees, but much faster compared to [1], and applicable to any system

Controllable Formula Search - Robotic Example



Random walk, label - 1 when hits an obstacle

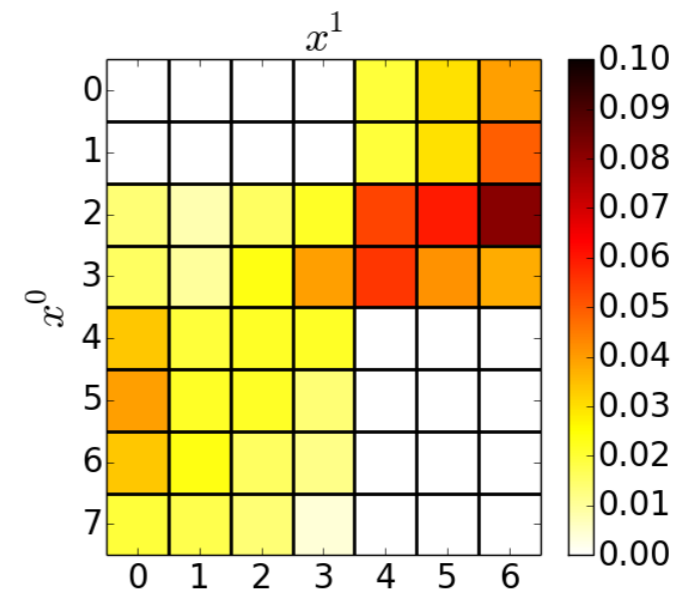
Control actions: S,N,E,W

$$\Phi_1 \vee \dots \vee \Phi_p$$

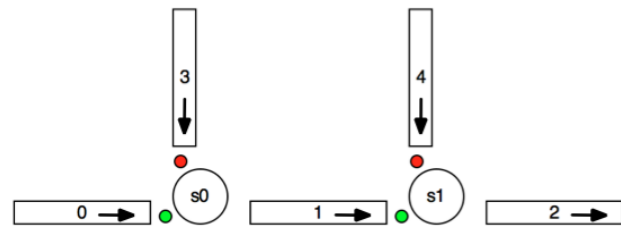
$$\Phi_i := (A_{[1,b_i]} u^j = c_i) \wedge (P_{[1,1]} \phi_i)$$

ongoing work: Generalize control formula with automata based controller.

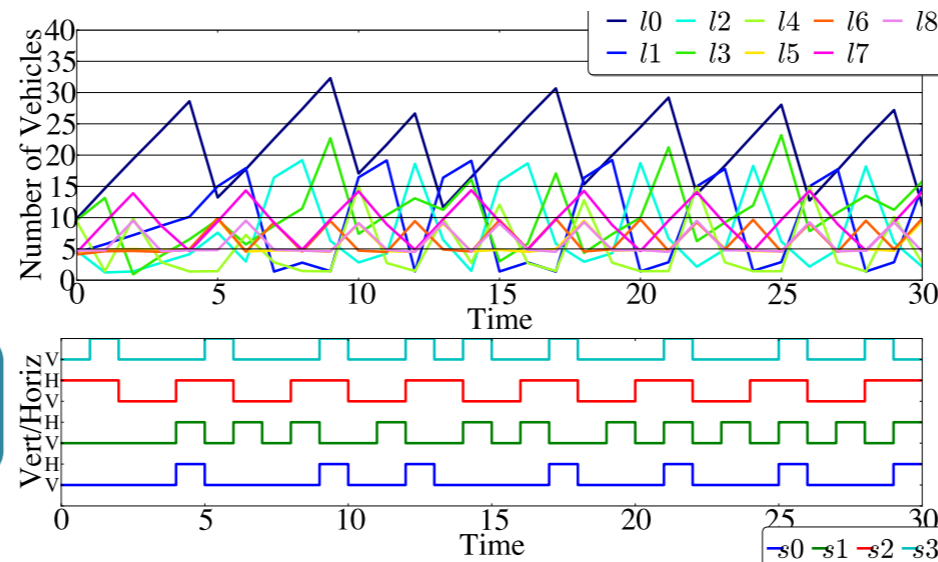
| i | v_i | Φ_i | tp | fp |
|-----|-------|--|------|------|
| 1 | 705 | $(G_{[1,1]}^- u = S) \wedge (F_{[1,1]}^-(x^1 > 3 \wedge x^0 > 2))$ | 126 | 0 |
| 2 | 429 | $(G_{[1,1]}^- u = N) \wedge (F_{[1,1]}^-(x^1 < 4 \wedge x^0 < 3))$ | 125 | 0 |
| 3 | 109 | $(G_{[1,1]}^- u = E) \wedge (F_{[1,1]}^-(x^1 > 2 \wedge x^0 > 3))$ | 42 | 0 |
| 4 | 77 | $(G_{[1,1]}^- u = W) \wedge (F_{[1,1]}^-(x^1 < 5 \wedge x^0 < 2))$ | 52 | 0 |
| 5 | 0 | - | - | - |



Summary: Cause mining with STL



$$x_l[t+1] = x_l[t] + d_l[t] - f_l^{out}(x_l[t]) + \sum_{k \in \mathcal{L}_l^{out}} \beta_{kl} f_k^{out}(x_k[t])$$



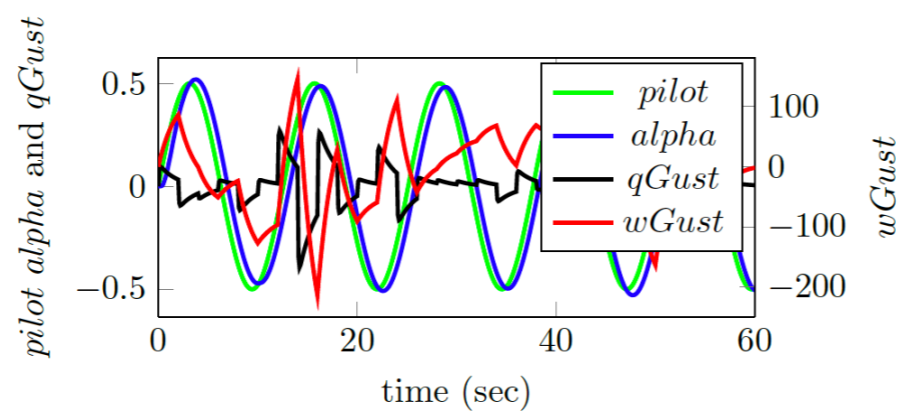
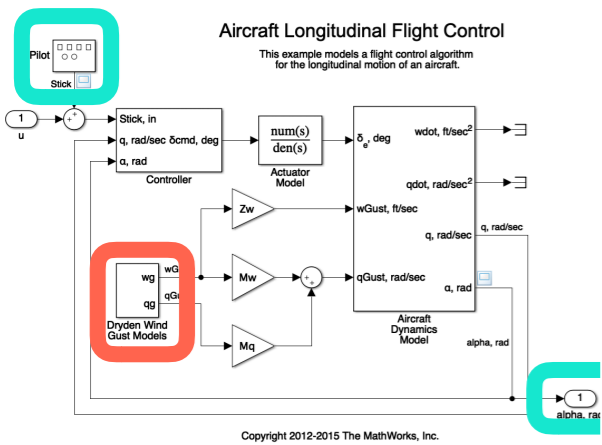
- 1 $\phi_1 = P_{[1,1]}(x^1 > 15 \wedge s^0 = 0 \wedge s^1 = 1)$
- 2 $\phi_2 = P_{[1,1]}(x^1 \geq 25 \wedge s^1 = 1)$
- 2 $\phi_3 = P_{[1,1]}(x^4 \leq 10 \wedge s^0 = 0 \wedge s^1 = 1)$

System model

Simulations

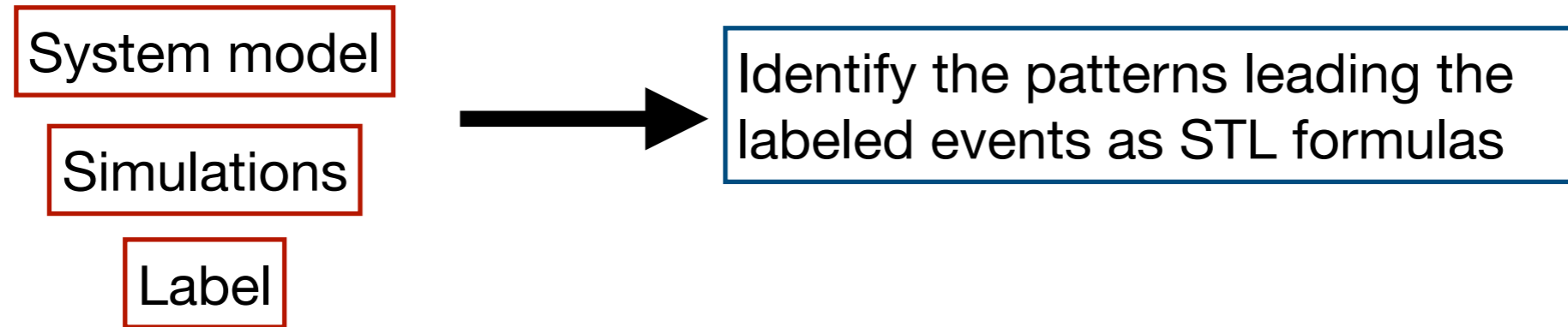
Label

Identify the patterns leading the labeled events as STL formulas



- 1 $\phi_1 = P_{[4,10]}(qGust \leq 0 \wedge wGust \leq -120)$
- 2 $\phi_2 = wGust \geq 120 \wedge A_{[14,14]}(pilot \geq -40)$
- 2 $\phi_3 = P_{[2,2]}(alpha \leq 30 \wedge wGust - \leq 120)$
- 2 $\phi_4 = (A_{[2,6]}qGust \geq 10) \wedge pilot \leq -40$

Cause mining with STL



- How can we ensure that these are actual causes ?
 - Underlying causes?
 - Symptoms?
- What if there is single label?
 - Somewhere along the simulation a problem occurred.
- Is there a class of systems for which this type of analysis can reveal the causes?

Further questions?