



Automating Time Series Safety Analysis for Automotive Control Systems using Weighted Partial Max-SMT

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Contents

- Background
- Motivation
- Approach and method
- Case Study
- Concluding remarks

Background

- Applying STAMP^{*1}/STPA^{*2} to automotive safety analysis.

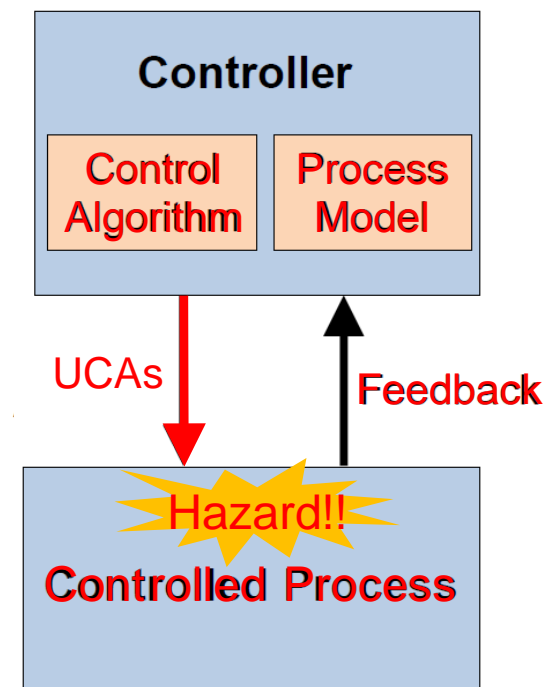
Preparation (Step 0)

- Identify Accidents and Hazards
- Construct a Control Structure

Step 1: Identify Unsafe Control Actions(UCAs)

Ex. System outputs a steering command while a driver doesn't do steering actions.

Step 2: Identify Causes of UCAs



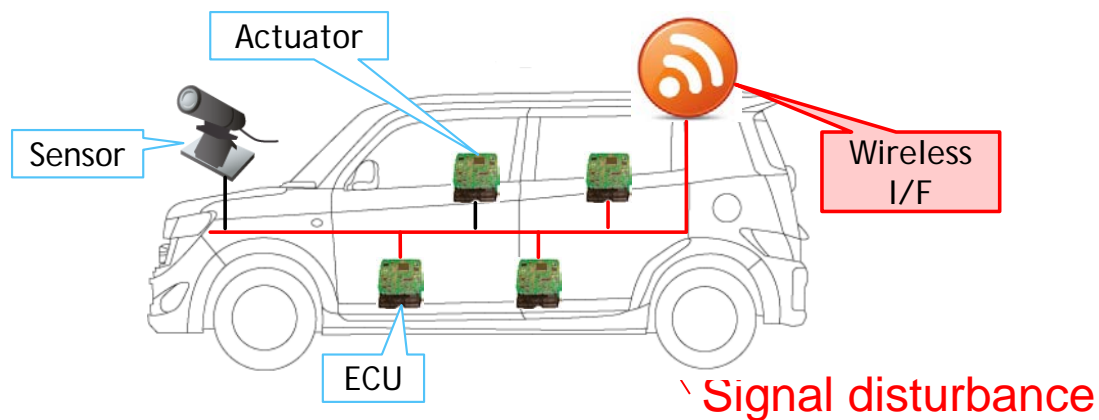
*1 System-Theoretic Accident Model and Process

*2 Systems-Theoretic Process Analysis

Motivation

(Intermittent) multi-signal disturbance that causes UCAs

Ex.



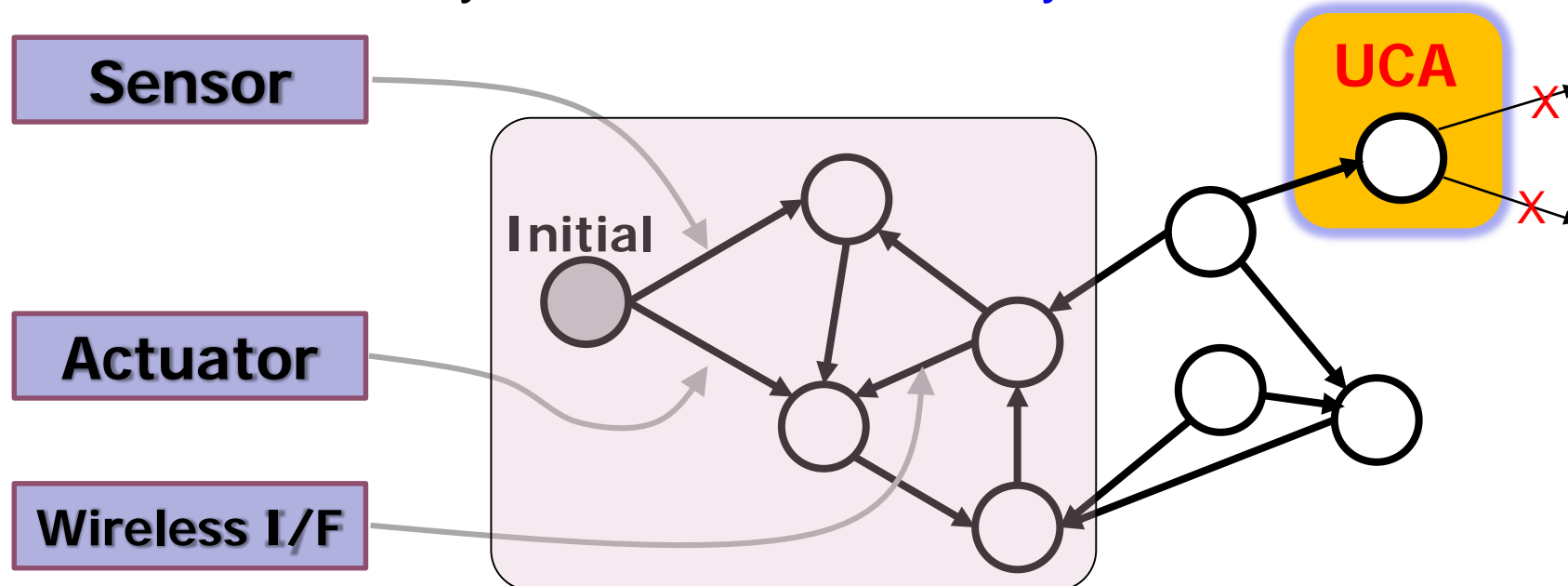
- **Challenge:**

Too many signal combinations and time series patterns in designing error/attack-proof systems

To detections of intermittent multi-signal disturbances.

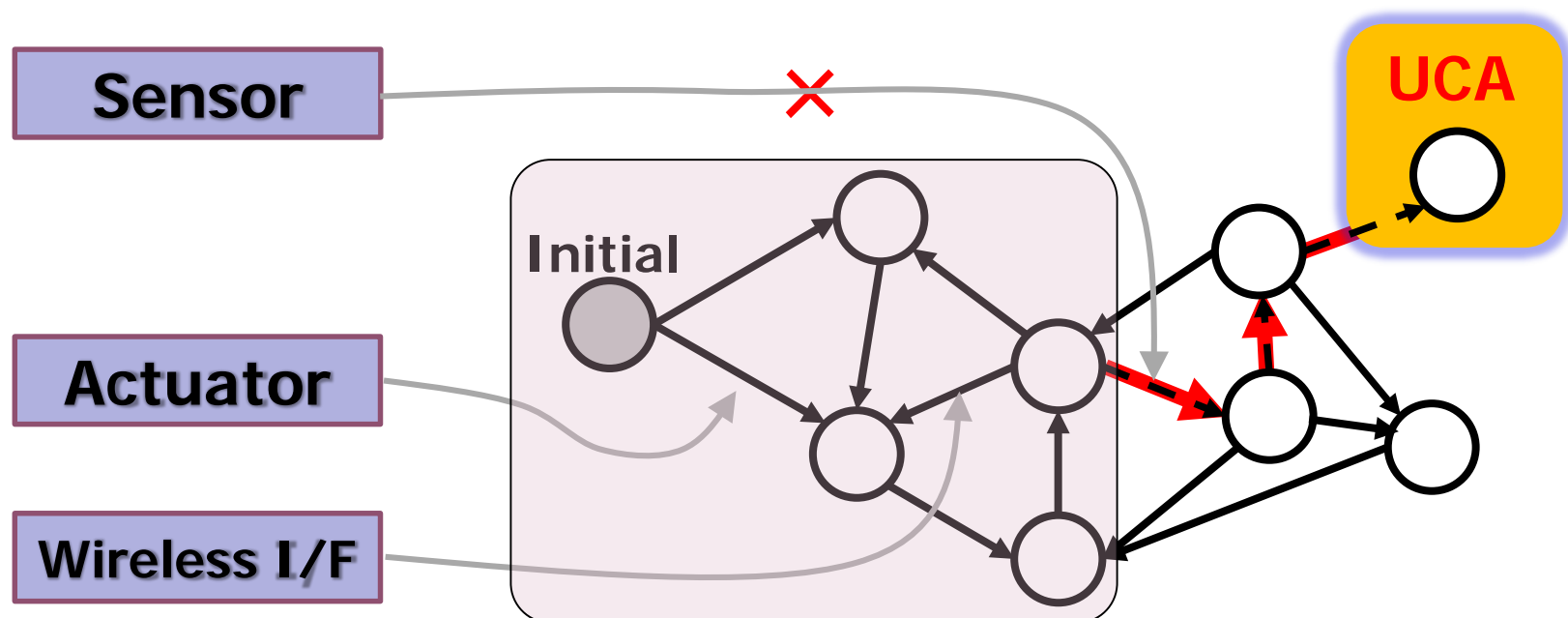
Behavioral Model

- Synchronous transition system with Boolean guard conditions.
Complete graph: Potentially ill transitions possible
- UCA states: states with transitions of UCAs unreachable by normal transition only.



Behaviour with Disturbance

If signals should be **disturbed**,
unexpected transitions should occur leading to an **UCA**.

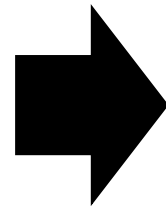


Analysis overview



Input:

- Transition system
- UCAs
- Possible disturbed signals



Output:

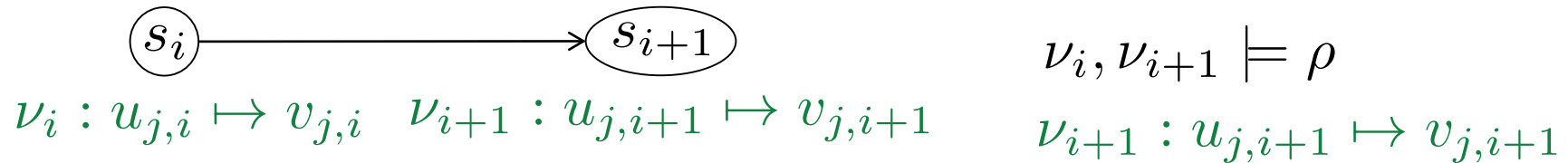
- Disturbed signal patterns



Approach

Transition System

- Transition system $M = (S, X, s_0, W)$
 - S : Control state X : State variable $s_0 \in S$: Initial control state
 - $W = \{ (s_i, \rho, s_{i+1}) \mid s_i, s_{i+1} \in S, \rho : \text{Constraints over } X \}$: Transitions



Deterministic transition system: s_{i+1} is unique to s_i $\nu_{i+1}(u_{j,i+1}) = f_{j,i}(\nu_i(u_{j,i}))$

- A trace of M : $\alpha = (s_0, \nu_0) (s_1, \nu_1) \cdots (s_n, \nu_n)$

$$s_i \in S, (s_i, \rho_i, s_{i+1}) \in W$$

where ν_i : Value assignment for X_i , $\nu_i, \nu_{i+1} \models \rho_i (X_i, X_{i+1})$



Bounded Trace Formula

- A trace formula $\text{TF}^{\leq K}$ of M (length: K) is a logical formula.

$$\rho_{s_0, s_1}(\vec{u}_0, \vec{u}_1) \wedge \rho_{s_1, s_2}(\vec{u}_1, \vec{u}_2) \wedge \cdots \wedge \rho_{s_{K-1}, s_K}(\vec{u}_{K-1}, \vec{u}_K)$$

$$\vec{u}_1 = f_0(\vec{u}_0) \wedge \vec{u}_2 = f_1(\vec{u}_1) \wedge \cdots \wedge \vec{u}_K = f_{K-1}(\vec{u}_{K-1})$$

$\text{TF}^{\leq K}$ is satisfied by value assignments $\nu_0, \nu_1, \dots, \nu_K$
 iff $\alpha = \nu_0, \nu_1, \dots, \nu_i, \dots$ is a trace in M

Straightforwardly constructed from M

Trace Formula of Transition System

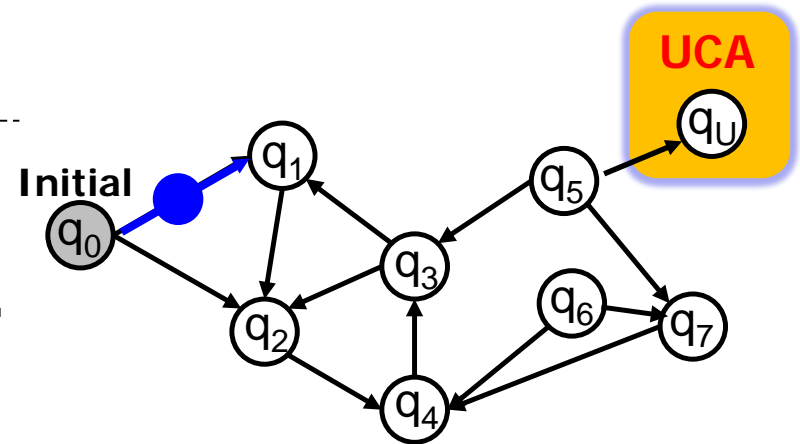
Trace (length K)

q_0 q_1 ... q_K

$$\begin{array}{lll}
 u_{1,0} = v_{1,init} & u_{1,1} = f_{0,1}(u_{1,0}) & u_{1,2} = f_{1,1}(u_{1,1}) \\
 u_{2,0} = v_{2,init} & u_{2,1} = f_{0,2}(u_{2,0}) & u_{2,2} = f_{2,1}(u_{2,1})
 \end{array}$$

Trace Formula: $TF^{\leq K}$

satisfied by the values along the trace



Trace Formula of Transition System

Trace (length K)

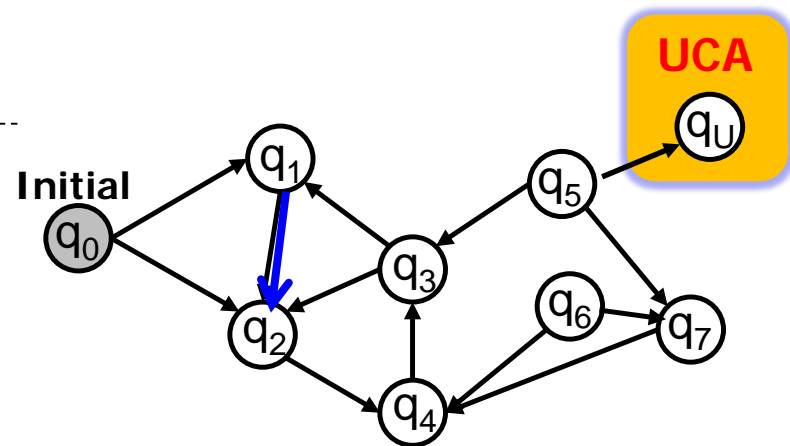
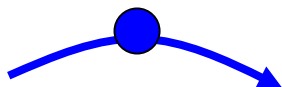
q_0 q_1 ... q_K

$$u_{1,0} = v_{1,init}$$

$$u_{2,0} = v_{2,init}$$

$$u_{1,1} = f_{0,1}(u_{1,0}) \quad u_{1,2} = f_{1,1}(u_{1,1})$$

$$u_{2,1} = f_{0,2}(u_{2,0}) \quad u_{2,2} = f_{2,1}(u_{2,1})$$



Trace Formula: $TF^{\leq K}$

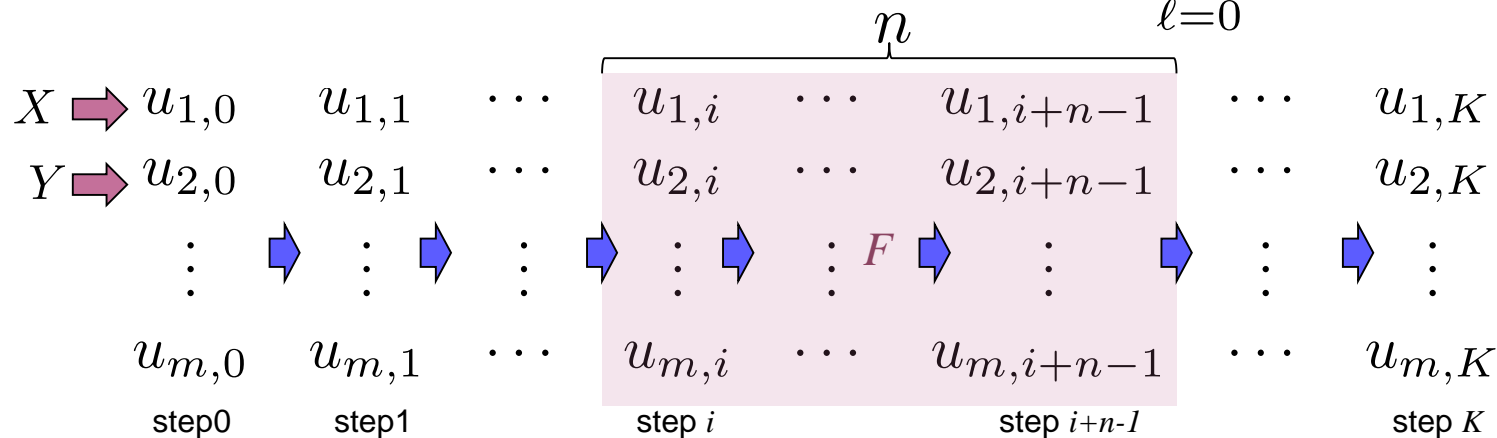
satisfied by the values along the trace

Unsafe Control Actions (UCAs)

- Reachability to hazardous states with unexpected values for a consecutive period of time (not expected in the design).

UCAs as constraint:

$$\underline{n - UCA_{\vec{F}}^{\leq K}} \equiv \exists i. i \leq K - n + 1 \wedge \left(\bigwedge_{\ell=0}^{n-1} f_{i+\ell-1}(\vec{u}_{i+\ell}) \right)$$



Signal Disturbance

$q_0 q_2 q_4 q_3$

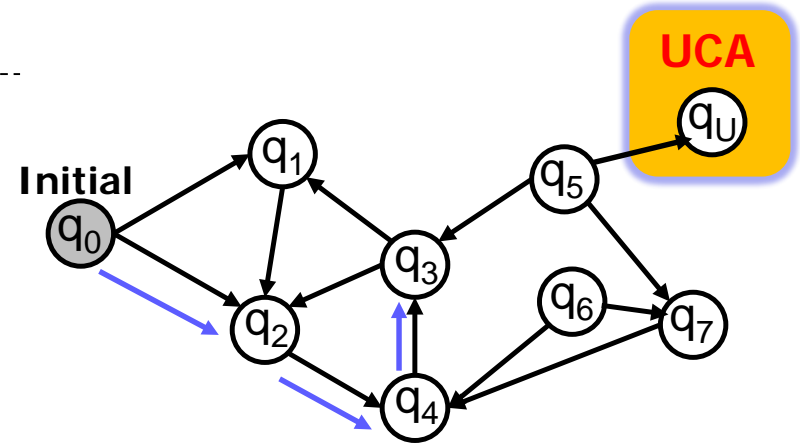
$(u_{1,3}, u_{2,3}) \neq g_{36}$

$$u_{1,0} = v_{1,init}$$

$$u_{1,3} = f_{4,1}(\vec{u}_2)$$

$$u_{2,0} = v_{2,init}$$

$$u_{2,3} = f_{4,2}(\vec{u}_2)$$



Signal Disturbance

$q_0 q_2 q_4 q_3 q_6$

$$(u_{1,3}, v_{bad}) \models g_{36}$$

$$u_{1,0} = v_{1,init}$$

$$u_{1,3} = f_{4,1}(\vec{u}_2)$$

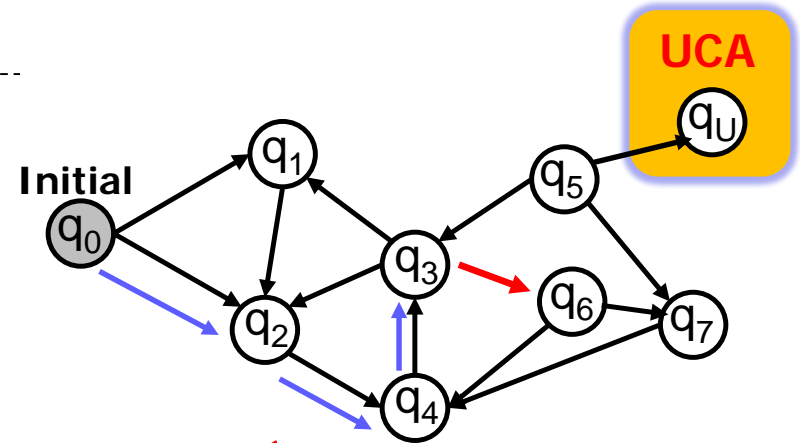
$$u_{1,4} = f_{3,1}(u_{1,3}, v_{bad})$$

$$u_{2,0} = v_{2,init}$$

$$u_{2,3} = v_{bad}$$

$$u_{2,4} = f_{3,2}(u_{1,3}, v_{bad})$$

$$(u_{1,4}, u_{2,4}) \not\models g_{65}$$



$u_{2,3} = v_{bad}$
Accidentally altered

Signal Disturbance

$q_0 q_2 q_4 q_3 q_6 q_5$

$$(u_{1,3}, v_{bad}) \models g_{36}$$

$$u_{1,0} = v_{1,init}$$

$$u_{1,3} = f_{4,1}(\vec{u}_2)$$

$$u'_{1,4} = v'_{bad}$$

$$u_{2,0} = v_{2,init}$$

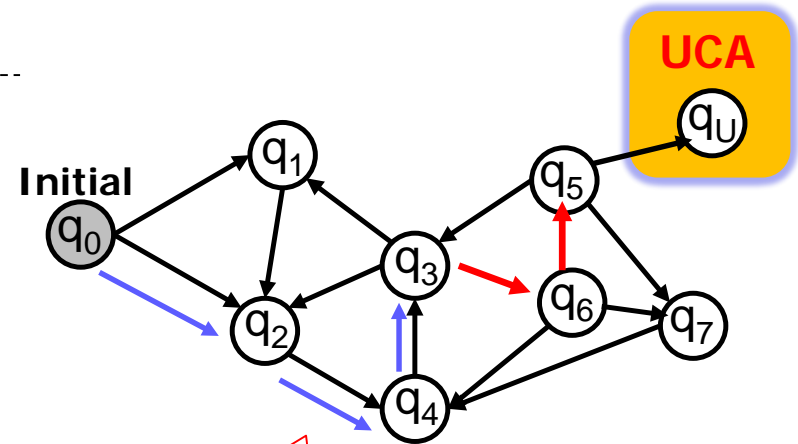
$$u_{2,3} = v_{bad}$$

$$u_{2,4} = f_{3,2}(u_{1,3}, v_{bad})$$

$$(v'_{bad}, u_{2,4}) \models g_{65}$$

$$u_{1,5} = f_{6,1}(v'_{bad}, u_{2,4})$$

$$u_{2,5} = f_{6,2}(v'_{bad}, u_{2,4})$$



$u_{1,4} = v'_{bad}$
Accidentally altered

Signal Disturbance

$q_0 q_2 q_4 q_3 q_6 q_5 q_u$

$$(u_{1,3}, v_{bad}) \models g_{36}$$

$$u_{1,0} = v_{1,init}$$

$$u_{1,3} = f_{4,1}(\vec{u}_2)$$

$$u'_{1,4} = v'_{bad}$$

$$u_{2,0} = v_{2,init}$$

$$u_{2,3} = v_{bad}$$

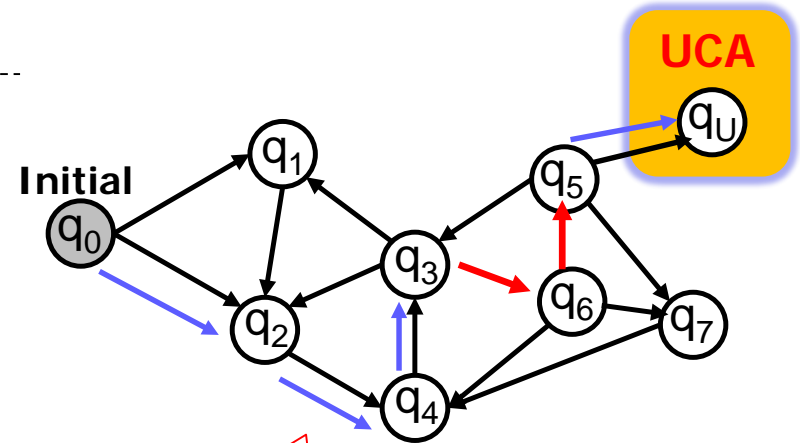
$$u_{2,4} = f_{3,2}(u_{1,3}, v_{bad})$$

$$(v'_{bad}, u_{2,4}) \models g_{65}$$

$$(u_{1,5}, u_{2,5}) \models g_{5u}$$

$$u_{1,5} = f_{6,1}(v'_{bad}, u_{2,4})$$

$$u_{2,5} = f_{6,2}(v'_{bad}, u_{2,4})$$



$u_{1,4} = v'_{bad}$
Accidentally altered



Disturbed Signal Pattern

Definition of disturbed signal pattern

$$DSP_U(\sigma) = \{u_{i,j} = u'_{i,j} \mid \underline{\sigma(u_{i,j}) \neq \sigma(u'_{i,j})}, i \in I, j \leq K\}$$

where

$U = \{u_{i_1}, \dots, u_{i_m}\}$: Set of variables

σ : Value assignment to variables

I : Time series of variables

K : Trace bound length

$u_{i,j}$: Original variables

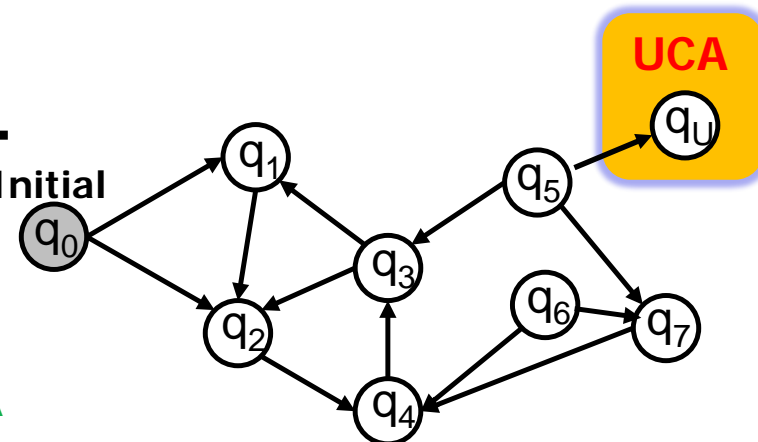
$u'_{i,j}$: Cushion variables



Modified Trace Formula with Cushion Variables

q_0 q_1 ... q_K

$$\underbrace{\begin{array}{l} u_{1,0} = v_{1,init} \quad u_{1,1} = f_{0,1}(u_{1,0}) \quad u_{1,2} = f_{1,1}(u_{1,1}) \dots \\ u_{2,0} = v_{2,init} \quad u_{2,1} = f_{0,2}(u_{2,0}) \quad u_{2,2} = f_{2,1}(u_{2,1}) \end{array}}_{TF \leq K}$$



Errors assign deferent values leading to UCA

Introduce “cushion variables u'_i ”.

Replace variables on RHS with cushion variables.

$$\underbrace{\begin{array}{l} u_{1,0} = v_{1,init} \quad u_{1,1} = f_{1,0}(u'_{1,0}, u'_{2,0}) \quad u_{1,2} = f_{1,1}(u'_{1,1}, u'_{2,1}) \\ u_{2,0} = v_{2,init} \quad u_{2,1} = f_{2,0}(u'_{1,0}, u'_{2,0}) \quad u_{2,2} = f_{2,1}(u'_{1,1}, u'_{2,1}) \end{array}}$$

Modified Trace Formula: $TF'_{U \leq K}$

U : Set of variables disturbed



Disturbed Signal Detection

$TF'_{\bar{U}}^{\leq K} \wedge \Omega_{\bar{U}}^K \wedge n-UCA_{\bar{F}}^{\leq K}$ is **not satisfiable**,

where $\Omega_{\bar{U}}^K \equiv \bigwedge_{u_i \in U} \bigwedge_{j \leq K} u_{i,j} = u'_{i,j}$,

($u_{i,j}$: Original variables $u'_{i,j}$: Cushion variables)

because $TF'_{\bar{U}}^{\leq K} \wedge \Omega_{\bar{U}}^K \Leftrightarrow TF^{\leq K}$.

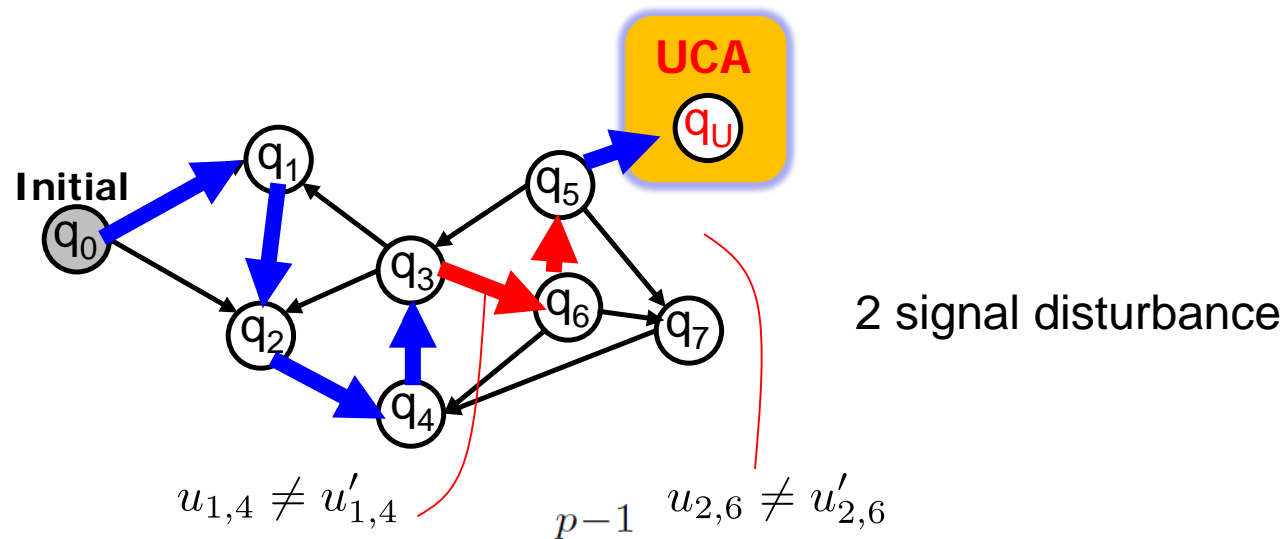
$TF'_{\bar{U}}^{\leq K} \wedge (\Omega_{\bar{U}}^K - \underline{DSP}_U(\sigma)) \wedge n-UCA_{\bar{F}}^{\leq K}$ is **satisfiable**.



Find a subset of $\Omega_{\bar{U}}^K$ to make ϕ satisfiable

Intermittent Signal Disturbance

Signal disturbances occur **no more than L times**
in **p execution steps**.



$$\Psi \equiv \forall i, j, i \in I, 1 \leq j \leq K - p + 1. \sum_{r=0}^{p-1} R(u_{i,j+r}, u'_{i,j+r}) \leq L$$

where

$$R(u_{i,j}, u'_{i,j}) = \begin{cases} 0 & \text{if } u_{i,j} = u'_{i,j} \\ 1 & \text{if } u_{i,j} \neq u'_{i,j} \end{cases} \quad \begin{array}{l} I : \text{Set of variable indexes of } U \\ U : \text{Set of variables} \end{array}$$



Constraints with signal disturbance

Trace formula with Cushions

Intermittent
constraint

Equality between original
and cushion variables

$$\Phi \equiv \underbrace{\text{TF}'_{U \leq K} \wedge n\text{-UCA}_{F \leq K} \wedge \Psi}_{\text{Hard}^{*1}} \wedge \underbrace{\Omega_U^K}_{\text{Soft}^{*2}}$$

*1 : Must be satisfied

*2 : Can be falsified

Apply Φ to pMax-SMT solver

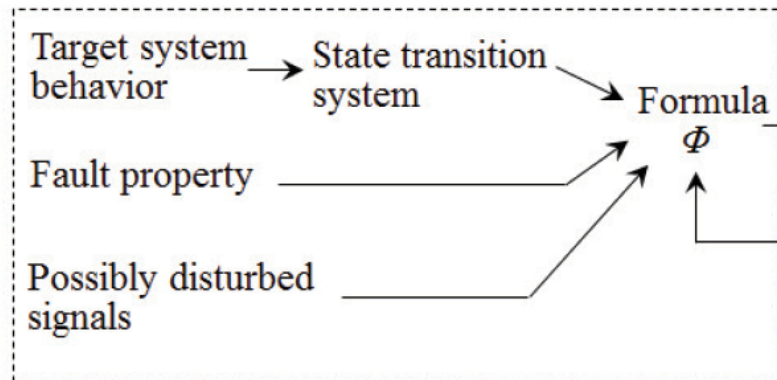
Weighted Partial Max-SMT solver finds $\Omega_U^K - DSP_U(\sigma)$
with minimum cost

Cost is heuristically assigned to Ω_U^K

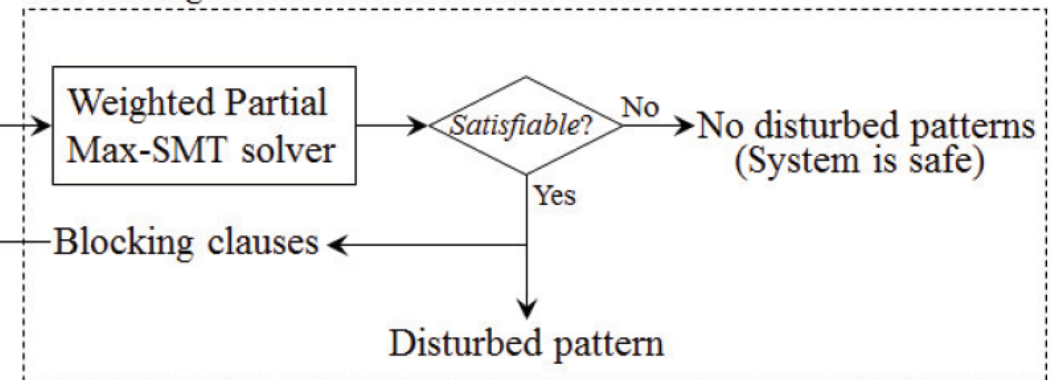
- Uniform
- As soon as possible: bigger costs for bigger step index

Design process overview

Phase 1:
Formula construction



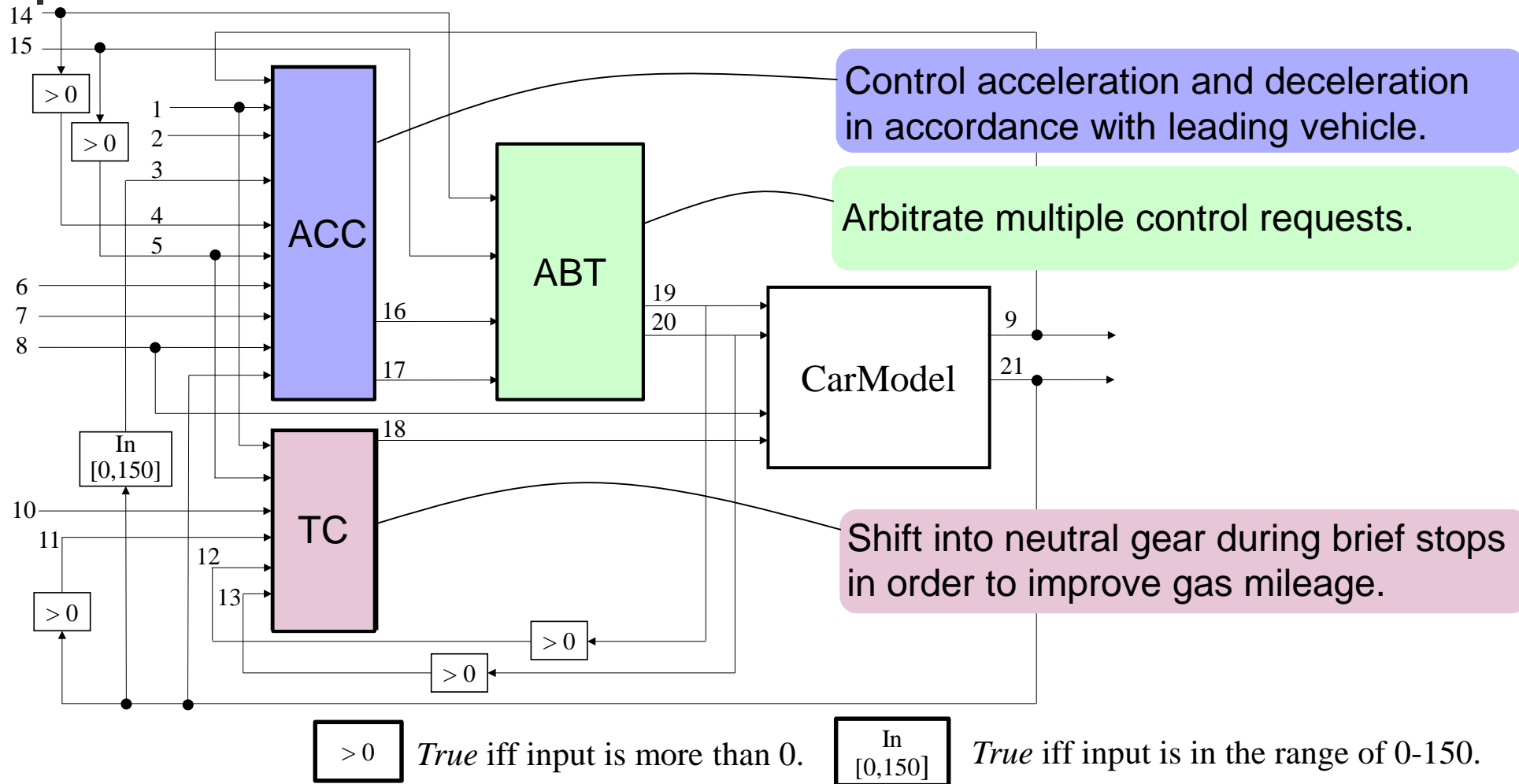
Phase 2:
Obtaining disturbed signal patterns
with a Weighted Partial Max-SMT solver





Case Study

Overview of Simplified Automotive Control System



UCA Example

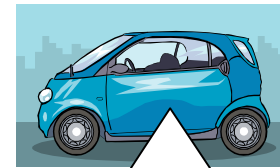
UCA:

Acceleration command is not provided for five consecutive clock cycles in the cruise control mode, even though the leading vehicle moves further away.

Move further away

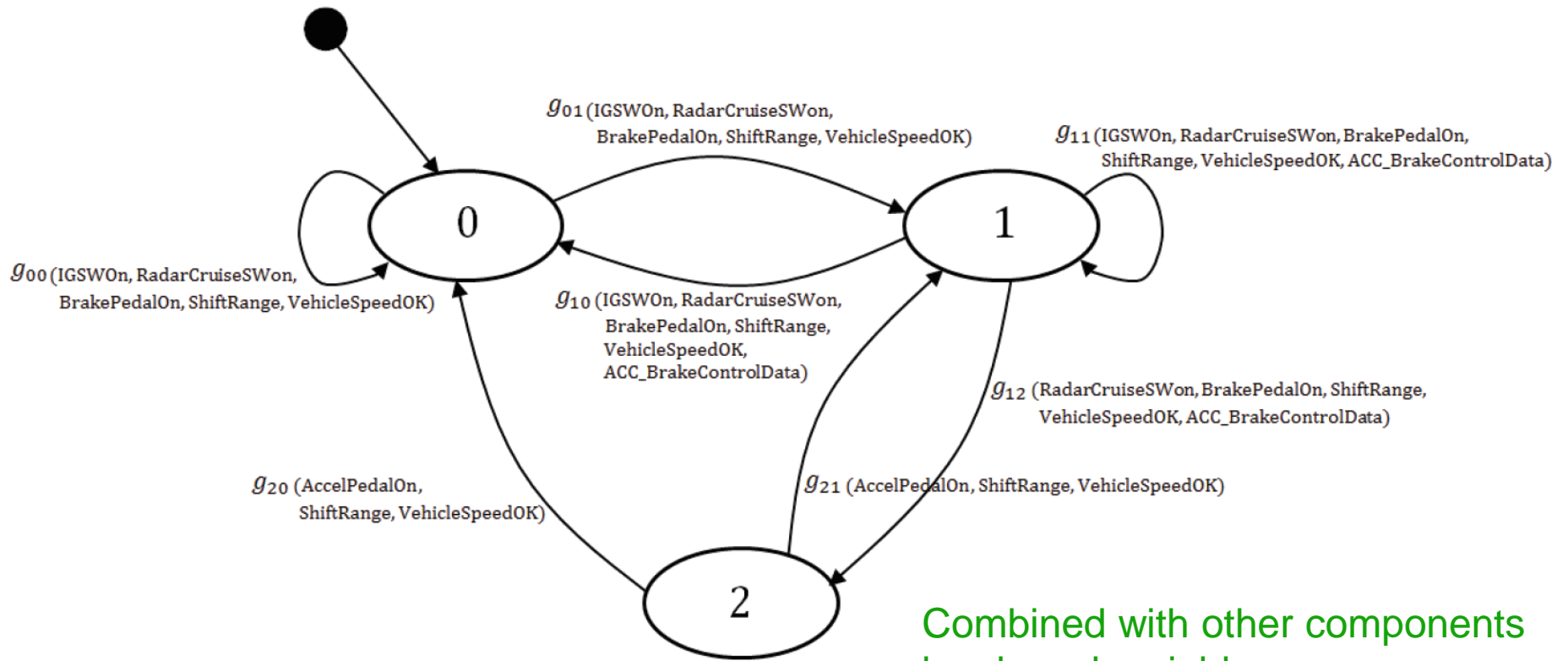


No acceleration commands



Cruise control mode

LTS (ACC-ECU component)



Combined with other components by shared variables



Derivation of failures

Following STAMP/STPA ...

Step 1: Identify Unsafe Control Actions

Step 2: Identify Causes of Unsafe Control Actions

apply our method in Step 2



UCA definition

LeadingVehicleSpeed > 0 \wedge Distance > C_d

\wedge BrakePedal = 0 \wedge AccelPedal = 0

\wedge RadarCruiseSWOn = *true*

\wedge ABT_AccelControlData = 0.

lasts for n-units of time in a row:

$n\text{-UDC}_{\frac{\leq K}{F}} \equiv \exists i. 1 \leq i \leq K - n + 1 \wedge$

$\bigwedge_{r=0}^{n-1} (\text{LeadingVehicleSpeed}^{(i+r)} > 0 \wedge \text{Distance}^{(i+r)} > C_d$

$\wedge \text{BrakePedal}^{(i+r)} = 0 \wedge \text{AccelPedal}^{(i+r)} = 0$

$\wedge \text{RadarCruiseSWOn}^{(i+r)} = \textit{true}$

$\wedge \text{ABT_AccelControlData}^{(i+r)} = 0).$

Result (1/2)

Signal names in each pattern

Signal Names	
<i>ShiftRange</i>	<i>VehicleSpeed</i>
<i>RadarCruiseSW</i>	<i>VehicleSpeed</i>
<i>VehicleSpeedOK</i>	<i>VehicleSpeed</i>
<i>BrakePedalOn</i>	<i>VehicleSpeed</i>

Example of obtained pattern

<i>t</i>	<i>VehicleSpeed</i>		<i>ShiftRange</i>	
	Normal Value	Disturbed Result	Normal Value	Disturbed Result
1	0	0	4	4
2	0	151	4	4
3	0	0	4	4
4	0	0	4	3
5	0	0	4	4

disturbed

Result (2/2)

Disturbed patterns under the condition *VehicleSpeed* is not disturbed. (Number of disturbed signals = 3)

Signal names in each pattern

<i>RadarCruiseSW</i>	<i>LeadingVehicleSpeed</i>	<i>ACC_AccelControlData</i>
<i>RadarCruiseSW</i>	<i>ShiftRange</i>	<i>LeadingVehicleSpeed</i>
<i>ShiftRange</i>	<i>LeadingVehicleSpeed</i>	<i>ACC_AccelControlData</i>
<i>RadarCruiseSW</i>	<i>VehicleSpeedOK</i>	<i>LeadingVehicleSpeed</i>
<i>VehicleSpeedOK</i>	<i>LeadingVehicleSpeed</i>	<i>ACC_AccelControlData</i>
<i>RadarCruiseSW</i>	<i>BrakePedalOn</i>	<i>LeadingVehicleSpeed</i>
<i>VehicleSpeedOK</i>	<i>ShiftRange</i>	<i>LeadingVehicleSpeed</i>
<i>VehicleSpeedOK</i>	<i>BrakePedalOn</i>	<i>LeadingVehicleSpeed</i>
<i>BrakePedalOn</i>	<i>LeadingVehicleSpeed</i>	<i>ACC_AccelControlData</i>
<i>BrakePedalOn</i>	<i>ShiftRange</i>	<i>LeadingVehicleSpeed</i>

Example of obtained pattern

<i>t</i>	<i>RadarCruiseSW</i>		<i>LeadingVehicleSpeed</i>		<i>ACC_AccelControlData</i>	
	Normal Value	Disturbed Result	Normal Value	Disturbed Result	Normal Value	Disturbed Result
1	on	on	30	30	0	0
2	on	on	60	-21	0	0
3	on	off	90	90	0	0
4	on	on	90	90	0	0
5	on	on	120	120	280	-1

disturbed

Result (2/2)

Disturbed patterns under the condition *VehicleSpeed* is not disturbed. (Number of disturbed signals = 3)

Signal names in each pattern

<i>RadarCruiseSW</i>	<i>LeadingVehicleSpeed</i>	<i>ACC_AccelControlData</i>
<i>RadarCruiseSW</i>	<i>ShiftRange</i>	<i>LeadingVehicleSpeed</i>
<i>ShiftRange</i>	<i>LeadingVehicleSpeed</i>	<i>ACC_AccelControlData</i>
<i>RadarCruiseSW</i>	<i>VehicleSpeedOK</i>	<i>LeadingVehicleSpeed</i>
<i>VehicleSpeedOK</i>	<i>LeadingVehicleSpeed</i>	<i>ACC_AccelControlData</i>
<i>RadarCruiseSW</i>	<i>BrakePedalOn</i>	<i>LeadingVehicleSpeed</i>
<i>VehicleSpeedOK</i>	<i>ShiftRange</i>	<i>LeadingVehicleSpeed</i>
<i>VehicleSpeedOK</i>	<i>BrakePedalOn</i>	<i>LeadingVehicleSpeed</i>
<i>BrakePedalOn</i>	<i>LeadingVehicleSpeed</i>	<i>ACC_AccelControlData</i>
<i>BrakePedalOn</i>	<i>ShiftRange</i>	<i>LeadingVehicleSpeed</i>

Example of obtained pattern

<i>t</i>	<i>RadarCruiseSW</i>		<i>LeadingVehicleSpeed</i>		<i>ACC_AccelControlData</i>	
	Normal Value	Disturbed Result	Normal Value	Disturbed Result	Normal Value	Disturbed Result
1	on	on	30	30	0	0
2	on	on	60	-21	0	0
3	on	off	90	90	0	0
4	on	on	90	90	0	0
5	on	on	120	120	280	-1

disturbed



Concluding remarks

- Faulty behavior caused by (intermittent) signal disturbance, in an automotive control system using Weighted Partial Max-SMT solvers.
 - Trace formulae with **cushion variables**.
 - Constraints for intermittent disturbance .
- Case study on a simplified automotive control system
- Finding clues to point out which signals are essential to avoid failures.